# Unsupervised Learning of Morphology and the Languages of the World 

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#### Abstract

This thesis presents work in two areas; Language Technology and Linguistic Typology.

In the field of Language Technology, a specific problem is addressed: Can a computer extract a description of word conjugation in a natural language using only written text in the language? The problem is often referred to as Unsupervised Learning of Morphology and has a variety of applications, including Machine Translation, Document Categorization and Information Retrieval. The problem is also relevant for linguistic theory. We give a comprehensive survey of work done so far on the problem and then describe a new approach to the problem as well as a number of applications. The idea is that concatenative affixation, i.e., how stems and affixes are stringed together to form words, can, with some success, be modelled simplistically. Essentially, words consist of highfrequency strings ("affixes") attached to low-frequency strings ("stems"), e.g., as in the English play-ing. Case studies show how this naive model can be used for stemming, language identification and bootstrapping language description.

There are around 7000 languages in the world, exhibiting a bewildering structural diversity. Linguistic Typology is the subfield of linguistics that aíms to understand this diversity. Many of the languages in the world today are spoken only by relatively small groups of people and are threatened by extinction and it is therefore a priority to record them. Language documentation, is and has been, an extremely decentralised activity, carried out not only by linguists, but also missionaries, travellers, anthropologists etc foremostly throughout the past 200 years. There is no central record of which and how many languages have been described. To meet the priority, we have attempted to list those languages which are the most poorly described which do not belong to a language family where some other languages is decently described - a task requiring both analysis and diligence. Next, the thesis includes typological work on one of the more tractable aspects of language structure, namely numeral systems, i.e., normed expressions used to denote exact quantities. In one of the first surveys to cover the whole world, we look at rare number bases among numeral systems. One major rarity is base-6-36 systems which are only attested in South/Southwest New Guinea and we make a special inquiry into its emergence.

Traditionally, linguists have had headaches over what counts as a language as opposed to a dialect, and have therefore been reluctant to give counts of the number of languages in a given area. One chapter of the present thesis shows that, contrary to popular belief, there is an intuitively sound way to count languages (as opposed to dialects). The only requirement is that, for each pair of varieties, we are told whether they are mutually intelligible or not.


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## Introduction

## 1 Language Technology

The work described in the first part of this thesis is in the area of Language Technology (LT), here defined as the study of computer-aided processing of natural languages. The ultimate goal of LT is to allow computers to deal with ("understand") natural language as humans do, which would make computers enormously more useful to humans. As of now, this goal is very far off, and we are happy if we can make progress on smaller subtasks, even if they do not achieve perfect accuracy. The problem studied in this thesis is one such subtask, and can be described as follows:

Given a large collection of written text in a given natural language, can a computer, without any specific knowledge about the language, extract a description of how words are conjugated in that language?

The problem is often referred to as Unsupervised Learning of Morphology, but also (Automatic) Induction of Morphology, Morpheme Discovery, Word Segmentation, Algorithmic Morphology, quantitative Morphsegmentierung (in German) and other variants have been used. Of these, Unsupervised Learning of Morphology (ULM) is fairly common and faces the least risk of misunderstanding, so it will be used throughout the present work.

In the Computer Science tradition, the solution to task such as this amounts to a) providing a formal description of the problem (in terms of sets, strings, logical conditions and the like) into which real-world instances are approximated, b) providing a step-by-step description of a method, i.e., an algorithm, to compute the desired output from the input and c) a proof or argument for the correctness and (if known) the optimality of the algorithm. Remarkably, in the 1940s, long before the Computer Science had matured as a field, and long before computers became practical to use, so-called structural linguists were asking for a solution of the exactly the same kind to the ULM and related problems, but from a different perspective. The interest was not so much putting computers to work as to learn how linguistic analysis could be understood, which has particular implications for linguistic theory and possibly child language acquisition. As with most work in Language Technology, the present work will draw on experiences from both Computer Science and Linguistics, and hopefully contribute to all.

The ULM problem is stated above in rather abstract terms. One might ask for specifics in terms of which languages are targeted, what (implicit) knowledge is allowed, how high accuracy is the aim, if there are speed requirements, how
much text input is needed, what is meant by a description of conjugating words, is a black-box solution adequate or do we have to understand the inner workings, what is assumed about the written form of a language and so on. All these aspects with be elaborated on in the thesis. However, in essence, we target a much wider range of languages than English, but if the input language is the English New Testament 11 the desired output is any kind of description that tells us that forms like played and playing are conjugations of the same stem, and that see and sea aren't, perhaps reaching $90 \%$ accuracy on such pairs. No knowledge at all of forms is to be supplied but a small number of parameters and assumptions about suffix-length can be tolerated, whereas running time is not a priority.

Word-form analysis, or morphological analysis (see below), is generally the first step in computational analysis of natural language, and as such has a wide variety of LT applications, including Machine Translation, Document Categorization and Information Retrieval. ULM can also serve to boost investigations in Linguistics, especially the subfields Quantitative Linguistics and Linguistic Typology, and potentially contribute to linguistic theory.

A legitimate question is about the stipulation that distributional criteria alone should serve as the only source of knowledge for the computer. Why cannot a little or a lot of human knowledge about a language be hard-wired in order to describe how words are conjugated? This is indeed an option, and has been the way to handle the matter for virtually all languages committed to computational treatment, but it normally requires a lot of human effort. Roughly the amount of work of an MA thesis is needed to computationally implement conjugational patterns and an unspecified but huge amount of work to list legal lexical items $2^{2}$ Therefore, the ULM-problem as specified, has an important role to play. First, it would be a great benefit to rid us of the human effort of implementing conjugational patterns for the next range of languages to receive computational treatment. Second, even for languages which have this already, along with huge lists of lexical items, open domain texts will always contain a fair share of (inflected) previously unknown words, that are not in the lexicon (Forsberg et al. 2006, Lindén 2008, Mikheev 1997, Bharati et al. 2001). There has to be strategy for such out-of-dictionary words - a ULM-solving algorithm is one possibility. It could also turn out that the ULM-problem cannot, in some sense, be solved without explicit human-derived linguistic knowledge. If such a proof, or a convincing argument, is found this constitutes a resolution to the ULM-problem as good as one which proves the existence of an ULM-solving algorithm.

[^0]
## 2 Languages of the World

The work described in the second part of this thesis is in the area of Linguistics, here defined as the study of natural languages. More specifically, the work in this thesis falls in the subfield of Linguistic Typology, or the systematic study of the unity and variation of the languages of the world.

Among all the normed speech varieties occurring among the world's peoples, linguistics have long become accustomed to the concept of a language as a maximal set of mutually intelligible varieties. (As is well-known, the everyday usage of the word language, does not precisely correspond to this delineation, as other factors, such as attitudes or political power, play a role in forming the everyday status.) Empirically and theoretically, there are problems with the notion of mutual intelligibility and a strict yes/no property. However, if we assume for a moment that there is no problem with the notion of mutual intelligibility, that is, for each pair of varities, we can decide yes/no if they are intelligible. Then it is logically possible that $A$ is mutually intelligible with $B$, $B$ is mutually intelligible with $C$, but $A$ is not mutually intelligible with $C$. The traditional manner in which linguists have approached this situation is to say that there is no way to assign languages over $A, B, C$, without somehow getting into contradictions, given the concept of language a maximal set of mutually intelligible varieties - $A, B, C$ cannot all be the same language, as $A$ and $C$ are not mutually intelligible. If $A, B$ is one language, then by the same token $B, C$ should also be one language, but if $A$ is the same as $B$ and $B$ is the same as $C$, then $A$ and $C$ must be the same, but they are not mutually intelligible! For this reason, linguistic have though the concept of language as being born with logical inconstiencies, and as a result, declared it impossible to count the number of languages in the world. This traditional view is too narrow, and to claim that there is no meaningful way to count the number of languages is wrong. In Chapter V we give a novel intuitively sound interpretation to show that it is possible to count the number of languages without any inconsistencies in any arrangement of speech varieties, as long as we assume that each pair of varieties can be decided mutual intelligible or not.

In Linguistic Typology, cross-linguistic facts are noted and non-random discrepancies are sought to be explained. Many different kinds of explanations could a priori be invoked, psycholinguistic, historical, cultural etc. In Chapter VII we present a rigid definition and a thorough survey of facts on one aspect of human language, namely number bases in the numeral system. It is presumably the first such survey that is explicitly known to cover languages from every language family attested in the world and thereby we are able to set the record straight in a number of open cases. One major rarity is base-6-36 systems which are only attested in South/Southwest New Guinea. In Chapter VI we attempt to trace the emergence of the base-6-36 system in this area. Although the data is somewhat incomplete, there is evidence that the 6-36 system came from yams counting. A cultural explanation, as the neighbouring non-base- 6 languages do not rely on tuber cultivation for subsistence.

Many of the languages in the world today are spoken only by relatively small
groups of people. Of these, many are on the path to extinction, in the sense that speakers, especially younger generations, are shifting to using another language, and consequently, as generations pass, no speakers at all will be left. Languages today die at a much faster rate than languages diverge to become new languages. Therefore the world's linguistic diversity is at risk of disappearing. For a scientific observer, the world's linguistic diversity is a unique gigantic experiment on human communication systems, which no laboratory can hope to achieve. For a small group of people, the language is part of their identity, and while a few are happy to shift, most groups would like to maintain their language, and, if anything, be bilingual in another, bigger, language. Languages documentation, i.e., to record languages (dictionary, grammar book, sound/video recordings), makes both scientists happy and helps the speaker community empower their language, and, if it dies anyway, allow descendants to see and hear their ancestral language.

Language documentation, is and has been, an extremely decentralised activity. It has been the outcome of linguists, missionaries, travellers, anthropologists, administrators etc stationed at missions, colonial establishments, universities in the first world and universities in the third world, over the past several centuries. There is no central record of which and how many languages have been described and to what level. From the perspective of science, the highest priority are languages otherwise poorly documented which are not genetically related to some other language which is not so poorly documented. In Chapter VIII we list those languages. Making such a list involves considerable bookkeeping work and a vast amount of analysing unclear cases, judging extinctness, and gauging relatedness of partly described, dubiously attested language varieties.

## 3 Publicatons and Contributions

The chapters in this thesis are based on the following publications.
a. Hammarström, H. (2005). A New Algorithm for Unsupervised Induction of Concatenative Morphology In Yli-Jyrä, A., Karttunen, L., and Karhumäki, J., editors, Finite State Methods in Natural Language Processing: 5th International Workshop, FSMNLP 2005, Helsinki, Finland, September 1-2, 2005. Revised Papers, volume 4002 of Lecture Notes in Computer Science, pages 288-289. Springer-Verlag, Berlin.
b. Hammarström, H. (2006a). A naive theory of morphology and an algorithm for extraction. In Wicentowski, R. and Kondrak, G., editors, SIGPHON 2006: Eighth Meeting of the Proceedings of the ACL Special Interest Group on Computational Phonology, 8 June 2006, New York City, $U S A$, pages 79-88. Association for Computational Linguistics.
c. Hammarström, H. (2006b). Poor man's stemming: Unsupervised recognition of same-stem words. In Ng, H. T., Leong, M.-K., Kan, M.-Y., and Ji, D., editors, Information Retrieval Technology: Proceedings of the Third

Asia Information retrieval Symposium, AIRS 2006, Singapore, October 2006, volume 4182 of Lecture Notes in Computer Science, pages 323-337. Springer-Verlag, Berlin.
d. Hammarström, H. (2007a). A fine-grained model for language identification. In Proceedings of iNEWS-07 Workshop at SIGIR 2007, 23-27 July 2007, Amsterdam, pages 14-20. ACM.
e. Hammarström, H. (2007b). A survey and classification of methods for (mostly) unsupervised learning of morphology. In NODALIDA 2007, the 16th Nordic Conference of Computational Linguistics, Tartu, Estonia, 25-26 May 2007. NEALT.
f. Hammarström, H., Thornell, C., Petzell, M., and Westerlund, T. (2008). Bootstrapping language description: The case of Mpiemo (Bantu A, Central African Republic). In Proceedings of LREC-2008, pages 3350-3354. European Language Resources Association (ELRA).
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h. Hammarström, H. (2009b). A Survey of Computational Morphological Resources for Low-Density Languages Submitted.
i. Forsberg, M., Hammarström, H., and Ranta, A. (2006). Lexicon extraction from raw text data. In Salakoski, T., Ginter, F., Pyysalo, S., and Pahikkala, T., editors, Advances in Natural Language Processing: Proceedings of the 5th International Conference, FinTAL 2006 Turku, Finland, August 23-25, 2006, volume 4139 of Lecture Notes in Computer Science, pages 488-499. Springer-Verlag, Berlin.
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k. Hammarström, H. (2008b). Counting languages in dialect continua using the criterion of mutual intelligibility. Journal of Quantitative Linguistics, $15(1): 34-45$.
l. Hammarström, H. (2009c). Whence the Kanum base-6 numeral system? Linguistic Typology, 13(2):305-319.
m. Hammarström, H. (2009d [to appear]). Rarities in numeral systems. In Wohlgemuth, J. and Cysouw, M., editors, Rara $\&$ Rarissima: Collecting and interpreting unusual characteristics of human languages, Empirical Approaches to Language Typology, pages 7-55. Mouton de Gruyter.
n. Hammarström, H. (2009e). The Status of the Least Documented Language Families in the World Submitted.

All the work in the present thesis is the sole and original work of the author, except Chapter III and the last section of Chapter 8 . In Chapter III, the present author conducted the experiment, took part in discussions, wrote the related work section and did the proof of NP-completeness, whereas the design, description and implementation of the extraction-tool was the work of Markus Forsberg and Aarne Ranta. In section [II] the present author did the design, implementation and write-up of the experiment, whereas Christina Thornell collected the text data in the field in the Central African Republic and Torbjörn Westerlund as well as Malin Petzell offered feedback and took part in discussions.

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## Part One: Computational Linguistics

## Chapter I Unsupervised Learning of Morphology: A Naive Model and Applications

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Edited synthesis of the following
papers, where Hammarström (2007b) has
been substantially updated:
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a. Hammarström, H. (2005). A New Algorithm for Unsupervised Induction of Concatenative Morphology In Yli-Jyrä, A., Karttunen, L., and Karhumäki, J., editors, Finite State Methods in Natural Language Processing: 5th International Workshop, FSMNLP 2005, Helsinki, Finland, September 1-2, 2005. Revised Papers, volume 4002 of Lecture Notes in Computer Science, pages 288-289. Springer-Verlag, Berlin.
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d. Hammarström, H. (2007a). A fine-grained model for language identification. In Proceedings of iNEWS-07 Workshop at SIGIR 2007, 23-27 July 2007, Amsterdam, pages 14-20. ACM.
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# Unsupervised Learning of Morphology: A Naive Model and Applications 

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## 1 Introduction

The problem addressed in the present chapter can be described as follows:
Input: An unlabeled corpus of an arbitrary natural language
Output: A (possibly ranked) set of prefixes and suffixes corresponding to true prefixes and suffixes in the linguistic sense, i.e., well-segmented and with grammatical meaning, for the language in question.

Restrictions: We consider only concatenative morphology and assume that the corpus comes already segmented on the word level.

The problem, in practice and in theory, is relevant for information retrieval, child language acquisition, and the many facets of use of computational morphology in general.

The reasons for attacking this problem in an unsupervised manner include advantages in elegance, economy of time and money (no annotated resources required), and the fact that the same technology may be used on new languages.

We begin with a survey on ULM in general, i.e., the problem as above, but without the restrictions.

Next, we describe two components in the broader line of attack on the ULMproblem. The first component extracts a list o salient prefixes and suffixes from an unlabeled corpus of a language. The underlying theory makes no assumptions on whether the language uses a lot of morphology or not, whether it is prefixing or suffixing, or whether affixes are long or short. It does however make the assumption that 1 . salient affixes have to be frequent, i.e., occur much more often that random segments of the same length, and that 2 . words essentially are variable length sequences of random characters, e.g., a character should not
occur in far too many words than random without a reason, such as being part of a very frequent affix. The second component, extract paradigms, i.e., sets of affixes, that tend to occur on the same stems. The underlying idea is that the members of a paradigmatic set of affixes alternate on a stem set in higher combined proportions than non-members. It is not necessary that the members pairwise occur with high absolute frequency on the same stems.

The two components are then used, with various additional measures, in four applications, which are given a separate section, and are empirically evaluated individually.

## 2 A Survey of Work on Unsupervised Learning of Morphology

For the purposes of the present survey, we use the following definition of Unsupervised Learning of Morphology (ULM).

Input: Raw (unannotated, non-selective) natural language text data
Output: A description of the morphological structure (there are various levels to be distinguished; see below) of the language of the input text

With: As little supervision, i.e., parameters, threholds, human intervention, model selection during development etc., as possible

Some approaches have explicit or implicit biases towards certain kinds of languages; they are nevertheless considered to be ULM for this survey.

Morphology may be narrowly taken as to include only derivational and grammatical affixation, where the number of affixations a root may take is finite and the order of affixation may not be permuted. This survey also subsumes attempts that take a broader view including clitics and compounding (and there seems to be no reasons in principle to exclude incorporation and lexical affixes). A lot of, but not all, approaches focus on concatenative morphology/compounding only.

All works considered in this survey are designed to function on orthographic words, i.e., raw text data in an orthography that segments on the word-level. Crucially, this excludes work the rather large body of work that only targets word-segmentation, i.e., segmenting a sentence or a full utterance into words. However, work that explicitly aims to treat both word-segmentation and morpheme-segmentation in one algorithm are included. Hence, subsequent uses of the term segmentation in the present survey is to be understood as morpheme-segmentation rather than word-segmentation. We prefer the term segmentation to analysis since, in general in ULM, the algorithm does not label the segments.

Work that requires selective input, such as 'singular-plural pairs', or 'all members of a paradigm' are excluded, unless such pairs/sets are extracted from raw text in an unsupervised manner as well. Similarly, we exclude work where some (small) amount of annotated data, some (small) amount of existing rule sets, or resources such as a parallel corpus, are mandatory.

One of the matters that varies the most between different authors is the desired outcome. It is useful to set up the implicational hierarchy shown in Table 1 (which need of course not correspond to steps taken in an actual algorithm). The division is implicational in the sense that if one can do the morphological analysis of a lower level in the table, one can also easily produce the analysis of any of the above levels. For example, if one can perform segmentation into stem and affixes, one can decide if two word are of the same stem. The converse need not hold, it is perfectly possible to answer the question of whether two words

| Affix list | A list of the affixes. |
| :---: | :--- |
| Same-stem decision | Given two words, decide if <br> they are affixations of the <br> same stem. |
| $\uparrow$Segmentation | Given a word, segment it into <br> stem and affix(es). |
| Paradigm list $_{\uparrow}^{\text {Lexicon+Paradigm }}$ | A list of the paradigms. |
|  | A list of the paradigms and a <br> list of all stems with informa- <br> tion of which paradigm each <br> stem belongs to. |

Table 1. Levels of power of morphological analysis. No distinction is made between probabilistic and non-probabilistic versions.
are of the same stem with high accuracy, without having to commit to what the actual stem should be.

Many recent articles fail to deal properly with previous and related work, some reinvent heuristics that have been sighted earlier, and there little modularization taking place. Previous surveys and overviews are Kurimo et al. 2007a, McNamee 2008, Kurimo and Variokallio 2008, Kurimo et al. 2007c. b, Hammarström 2007a, Kurimo et al. 2008, Kurimo and Turunen 2008, Powers 1998, Borin 1991, Clark 2001, Roark and Sproat 2007, Goldsmith pear, Borin 2009, Batchelder 1997:66-68 and the related-work sections of research papers. Nevertheless, there is no survey to date which is comprehensive and which discusses the ideas in the field critically.

We will not attempt a comparison in terms of accuracy figures as this is wholly impossible, not only because of the great variation in goals but also because most descriptions do not specify their algorithm(s) in enough detail. Furtunately, this aspect is better handled in controlled competitions, such as the Unsupervised Morpheme Analysis - Morpho Challeng ${ }^{11}$ which offers tasks of segmentation of Finnish, English, German, Arabic and Turkish.

### 2.1 Roadmap and Synopsis of Earlier Studies

A chronological listing of earlier work (with very short characterizations) is given in Table 244 Several papers are co-indexed if they represesent essetially the same line of work bu essentially the same author(s).

Given the number of algorithms proposed, it is impossible to go through the methods and ideas individually. However, the main trends are as follows.

[^1]|  | Model | Superv. | Experimentation | Learns what? |
| :---: | :---: | :---: | :---: | :---: |
| Harris 1955, 1968, 1970 | C | T | English | Segmentation |
| Andreev 1965, 1967: Chapter 2 | C | T | Hungarian/Russian <br> (I) | Unclear |
| Gammon 1969 | C | T | English | Segmentation |
| Lehmann 1973:71-93 | C | T | German (I) | Segmentation |
| de Kock and Bossaert 1969, 1974, 1978 | C | T | French/Spanish | Lexicon+Paradigms |
| Hafer and Weiss 1974 | C | T | English (IR) | Segmentation |
| Faulk and Gustavson 1990 | C | T | English (I) | Segmentation |
| Klenk and Langer 1989 | C | T | German | Segmentation |
| Langer 1991 | C | T | German | Segmentation |
| Redlich 1993 | C | T | English (I) | Segmentation |
| Klenk 1992, 1991 | C | T | Spanish | Segmentation |
| Flenner 1992, 1994, 1995 | C | T | Spanish | Segmentation |
| Janßen 1992 | C | T | French | Segmentation |
| Juola et al. 1994 | C | T | English | Segmentation |
| $\begin{array}{lll}\text { Brent } & 1993, & 1999, \\ \text { Snover } & 2002 & \text { Brent et al. } \\ \text { Snover et al. } & 1995, \\ 2002\end{array}$ | C | T | English/ChildEnglish/Polish/ | Segmentation |
| Snover and Brent 2001, 2003 |  |  | French |  |
| Deligne and Bimbot 1997, Deligne 1996 | C | T | English/French (I) | Segmentation |
| Yvon 1996 | C | T | French (I) | Segmentation |
| Kazakov 1997, | C | T | French/English | Segmentation |
| Kazakov and Manandhar 1998, 2001 |  |  |  |  |
| Jacauemin 1997 | C | T | English | Segmentation |
| Cromm 1997 | C | T | German | Unclear |
| Gaussier 1999 | C | T | French/ <br> English (I) | Lexicon+Paradigms |
| Déiean 1998a b | C | T | Turkish/English/ <br> Korean/French/ <br> Swahili/ <br> Vietnamese (I) | Affix Lists |
| Medina Urrea 2000, 2003, 2006 | C | T | Spanish | Affix List |
| Schone 2001 |  |  |  |  |
| Goldsmith 2000, 2001, 2006, | C | T | English (I) | Lexicon+Paradigms |
| Belkin and Goldsmith 2002, |  |  |  |  |
| Goldsmith et al. 2001, Hu et al. 2005b, |  |  |  |  |
| Xanthos et al. 2006 |  |  |  |  |
| Baroni 2000, 2003 | C | T | Child-English/ <br> English | Affix List |
| Cho and Han 2002 | C | T | Korean | Segmentation |
| Sharma et al. 2002, 2003, | C | T | Assamese | Lexicon+Paradigms |
| Sharma and Das 2002 |  |  |  |  |
| Baroni et al. 2002 | C/NC | T | English/German (I) | Related word pairs |
| Bati 2002 | C/NC | T | Amharic | Lexicon+Paradigms |

Table 2. Very brief roadmap of earlier studies [Page 1(3)]. Abbrevations in the Table: $\mathrm{C}=$ Concatenative, $\mathrm{NC}=$ Non-concatenative, $\mathrm{T}=$ Threshold(s) and Parameter(s) to be set by a human, $\mathrm{I}=$ Impressionistic evaluation, $\mathrm{IR}=$ Evaluation only in terms of Information Retrieval Performance. $\mathrm{RR}=$ Handwritten rewrite rules.

|  | Model | Superv. | Experimentation | Learns what? |
| :---: | :---: | :---: | :---: | :---: |
| Creutz 2003, 2006, Creutz and Lagus | C | T | Finnish/Turkish/ English | Segmentation |
| 2002, 2005c, 2004, 2005a b, 2007, |  |  |  |  |
| Creutz et al. 2005b, Hirsimäki et al. |  |  |  |  |
| 2003, Creutz et al. 2005a |  |  |  |  |
| Kontorovich et al. 2003 | C | T | English | Segmentation |
| Medina Urrea and Díaz 2003, | C | T | Chuj/Ralámuri/Czech | Affix List |
| Medina-Urrea 2006, 2008 |  |  |  |  |
| Mavfield and McNamee 2003, | - | - | 8 West European languages (IR) | Same-stem |
| McNamee and Mavfield 2007 |  |  |  |  |
| Zweigenbaum et al. 2003, Hadouche 2002 | C | T | Medical French | Segmentation |
| Pirrelli et al. 2004, Pirrelli and Herreros | C | T | Italian/English/Arabic | Unclear |
| 2007 |  |  |  |  |
| Johnson and Martin 2003 | C | T | Inuktitut | Unclear |
| Katrenko 2004 | C | T | Ukrainian | Lexicon+Paradigms |
| Cavar et al. 2004a b, Ćavar et al. 2005, <br> 2006 | C | T | Child-English | Unclear |
| Rodrigues and Ćavar 2005, 2007 | NC | T | Arabic | Segmentation |
| Monson 2004, 2009, Monson et al. 2007b, | C | T | English/Spanish/ | Segmentation |
| 2004, 2007a, 2008a b c |  |  | Mapudungun (I) |  |
| Yarowsky and Wicentowski 2000, | $\mathrm{C} / \mathrm{NC}$ | AP | 30-ish mostly European type languages | Segmentation |
| Wicentowski\| 2002, 2004 |  |  |  |  |
| Gelbukh et al. 2004 | C | - | English | Segmentation |
| Argamon et al. 2004 | C | T | English | Segmentation |
| Goldsmith et al. 2005, Hu et al. 2005 a | C/NC | T | Unclear | Unclear |
| Bacchin et al. 2005, 2002b a, | C | T | Italian/English | Segmentation |
| Nunzio et al. 2004 |  |  |  |  |
| Oliver 2004: Chapter 4-5 | C | T | Catalan | Paradigms |
| Bordag 2005b a, 2007b, a d | C | T | English/German | Segmentation |
| $\begin{aligned} & \text { Hammarström 2006a, 2005, 2006a, b, } \\ & 2007 \mathrm{~b}, 2009 \mathrm{a} \end{aligned}$ | C | - | Maori to Warlpiri | Same-stem |
| Bernhard 2005a b, 2006, 2007a b | C | T | Finnish/Turkish/English | Segmentation+Related sets of words |
| Keshava and Pitler 2005 | C | T | Finnish/Turkish/English | Segmentation |
| Johnsen 2005 | C | T | Finnish/Turkish/English | Segmentation |
| Atwell and Roberts 2005 | C | T | Finnish/Turkish/English | Segmentation |
| Dang and Choudri 2005 | C | T | Finnish/Turkish/English | Segmentation |
| ur Rehman and Hussain 2005 | C | T | Finnish/Turkish/English | Segmentation |
| Jordan et al. 2006, 2005 | C | T | Finnish/Turkish/English | Segmentation |
| Goldwater et al. 2005, Goldwater 2007, | C | T | English/Child-English | Segmentation |
| Naradowsky and Goldwater 2009 |  |  |  |  |
| Freitag 2005 | C | T | English | Segmentation |
| Golcher 2006 | C | - | English/German | Lexicon+Paradigms |
| Arabsorkhi and Shamsfard 2006 | C | T | Persian | Segmentation |
| Chan 2006 | C/NC | T | English | Paradigms |
| Demberg 2007 | C/NC | T | English/German/Finnish/ Turkish | Segmentation |
| Dasgupta and Ng 2006, 2007, | C | T | Bengali | Segmentation |
| Dasgupta and Ne. 2007, Dasgupta <br> 2007 |  |  |  |  |
| De Pauw and Wagacha 2007 | C/NC | T | Gikuyu | Segmentation |
| Tepper 2007, Tepper and Xia 2008 | $\mathrm{C} / \mathrm{NC}$ | T+RR | English/Turkish | Analysis |

Table 3. Very brief roadmap of earlier studies [Page 2(3)]. Abbrevations in the Table: $\mathrm{C}=$ Concatenative, $\mathrm{NC}=$ Non-concatenative, $\mathrm{T}=$ Threshold(s) and Parameter(s) to be set by a human, $\mathrm{I}=$ Impressionistic evaluation, $\mathrm{IR}=$ Evaluation only in terms of Information Retrieval Performance. $\mathrm{RR}=$ Handwritten rewrite rules.

|  | Model | Superv. | Experimentation | Learns what? |
| :---: | :---: | :---: | :---: | :---: |
| Xanthos 2007 | NC | T | Arabic | Lexicon+Paradigms |
| Majumder et al. 2007, 2008 | C | T | French/Bengali/French/ Bulgarian/Hungarian | Analysis |
| Zeman 2007, 2008a b | C | - | Czech/English/German/ Finnish | Segmentation+ Paradigms |
| Kohonen et al. 2008 | C | T | Finnish/Turkish/English | Segmentation |
| Goodman 2008 | C | T | Finnish/Turkish/English | Segmentation |
| Pandev and Siddiqui 2008 | C | T | Hindi | Segmentation+ <br> Paradigms |
| Johnson 2008 | C | T | Sesotho | Segmentation |
| Snyder and Barzilay 2008 | C/NC | T | Hebrew/Arabic/Aramaic/ English | Segmentation |
| Spiegler et al. 2008 | C | T | Zulu | Segmentation |
| Moon et al. 2009 | C | T | English/Uspanteko | Segmentation |
| Poon et al. 2009 | C | T | Arabic/Hebrew | Segmentation |

Table 4. Very brief roadmap of earlier studies [Page 3(3)]. Abbrevations in the Table: $\mathrm{C}=$ Concatenative, $\mathrm{NC}=$ Non-concatenative, $\mathrm{T}=$ Thresholds and Parameters to be set by a human, $I=$ Impressionistic evaluation, $I R=$ Evaluation only in terms of Information Retrieval Performance. $\mathrm{RR}=$ Hand-written rewrite rules.

There are basically three approaches to the problem:
a. Group and Abstract: In this family of methods, words are first grouped (clustered into sets, paired, shortlisted etc) according to some metric, which is typically string edit distance, but may include semantic features (Schone 2001), distributional similarity (Freitag 2005) or frequency signatures (Wicentowski 2002). The next step, is to abstract some morphological pattern that recurs among the groups. Such emergent patterns provide enough clues for segmentation and can sometimes be formulated as rules or morphological paradigms.
b. Frequency and Border: In this family of methods, frequent segments have a direct interpretation as candidates for segmentation. In addition, if a segment occurs with a variety of segments immediately adjacent to it, this is interpreted as evidence for a segmentation border. A typical implementation is to subject the data to a compression formula of some kind, where frequent long segments with clear borders offer the optimal compression gain. The outcome of such a compression scheme gives the segmentation and occasionally paradigm information can be gleaned from co-occurrence and border properties.
c. Features and Classes: In this family of methods, a word is seen as made up of features - n -grams in Mayfield and McNamee (2003), McNamee and Mayfield (2007), and initial/terminal/mid-segment in De Pauw and Wagacha (2007). Features which occur on many words have little selective power across
the words, whereas features which occur seldom, pinpoint a specific word or stem. To formalize this intuition, Mayfield and McNamee (2003) and McNamee and Mayfield (2007) use TF-IDF and De Pauw and Wagacha (2007) use entropy. Classifying an unseen word reduces to using its features to select which word(s) it may be morphologically related to. This decides whether the unseen word is a morphological variant of some other word, and allows extracting the "variation" by which they are related, such as an affix.

The first two, a. and b., enjoy a fair amount of popularity in the present collection of work, though b. is more common and was the only kind used up to about 1997. The last, c., is used only by two sets of authors (cited above). Xanthos (2007) falls outside either category as it attempts to first learn phonological categories and then uses these to infer intercalated morphology (with the observation that, empirically, intercalated morphology does seem to depend on vowel/consonant considerations). The work by de Kock and Bossaert 1969, 1974, 1978, Yvon 1996, Medina Urrea 2003 can favourably be seen as a midway between a . and b . as they rely on sets of four members with a particular affixation arrangement ("squares"), whose existence is governed much by the frequency of the affixes in question. There are, of course, many other lines of work that draw from both a. and b., but in a less cross-cut way.

An obvious advantage of the a. (and to some extent c.) family of methods is that they are capable of handling non-concatenative morphology.

### 2.2 Discussion

Within the a. family of methods, the main challenge is to avoid the use of thresholds to filter out spurious groupings that come with all of the so far employed grouping criteria.

In the b. family of methods, there are several open questions of interest.
Most (if not all) authors trace the inspiration for their border/frequency heuristics back to Harris (1955). Although Harris was far ahead in conceiving of an algorithm using such counts for segmentation, his description is vague on the role/need for thresholds $\Sigma^{2}$, and the exact formulation of his criterion, namely the size of a segment's successor character set, was shown (in various interpretations) as early as Hafer and Weiss (1974) not to be quite sound - even for English. Kazakov and Manandhar (2001) identify further theoretical shortcomings). More modern versions have considered the branching signature of a segment's character trie, with better empirical results, but we still do not have a theoretical understanding of the signs of segment combination and alternation.

Another way to use character sequence counts is that associated with Ursula Klenk and various colleagues (see, e.g., Klenk and Langer (1989) for a good explanation). For each character bigram $c_{1} c_{2}$, they record at what percentage there is a morpheme boundary before $\mid c_{1} c_{2}$, between $c_{1} \mid c_{2}$, after $c_{1} c_{2} \mid$, or none.

[^2]A new word can then be segmented by sliding a bigram window and taking the split which satisfies the corresponding bigrams the best. For example, given a word singing, if the window happens to be positioned at -gi- in the middle, the bigram splits $n g|, g| i$ and $\mid i n$ are relevant to deciding whether sing $\mid i n g$ is a good segmentation. Exactly how to do the split by sliding the window and combining such bigram split statistics is subject to a fair amount of discussion. However, it became apparent that, bigram-splithood is dependent on, e.g., the position in a word - -ed is likely at the end of a word, but hardly in any other position - and exception lists and cover-up rules had to be introduced, before the approach was abandoned altogether.

Several different authors in the b. paradigm have hailed Minimum Description Length (MDL) as the motivation for a given formula to compress input data into a morphologically analysed representation. The Minimum Description Length (MDL) principle is a general purpose method of statistical inference. It views the learning/inference process as data compression: for a given set of hypotheses $H$ and data set $D$, we should try to find the hypothesis in $H$ that compresses $D$ most (Grünwald 2007:3-40). Concretely, such a calculation can take the the following form. If $L(H)$ is the length, in bits, of the description of the hypothesis; and $L(D \mid H)$ is the length, in bits, of the description of the data when encoded with the help of the hypothesis, then MDL aims to minimize $L(H)+L(D \mid H)$. In principle, all of the works that have invoked MDL in the ULM-method act as follows. A fix way $Q$ of describing morphological regularities is conceived, which has two components which we may call patterns $H$ and data $D$. A coding scheme is devised to describe any $H$ and to describe any set of actual words with some specific $H$ and $D$. A greedy search is done for a local minimum of the sum $L(H)+L(D \mid H)$ to describe the set of words $W$ (in some approaches) or the bag of tokens $C$ (in other approaches) of the input text data ${ }^{3}$. In these cases, the label MDL, in at least the terminology of Grünwald (2007:37-38), seems to be ill-founded since, crucially, the $Q, H, D$ search is not among different description languages, but among parameters in a fix language. In this respect it is important to note that, compared to the schemes devised so far, Lempel-Ziv compression should yield a superior compression (as, in fact, conceded by Baroni 2000:146-147). However, MDL-inspired optimization schemes have achieved very competetive results in practice.

Lastly, several pieces of work in the b. tradition have attempted to address morphophonological changes in a principled way, though so far these have been developed in close connection with a particular segmentation method and target language.

A perhaps worrying tendency is that, despite extensive cross-citation, there is little transfer between different groups of authors and there is a fair amount of duplication of work. The lack of a broadly accepted theoretical understanding is possibly related to this fact. Few approaches have an abstract model of how words are formed, and thus cannot explain why (or why not) the heuristics

[^3]employed fail, what kind of errors are to be expected and how the heuristics can be improved. Nevertheless, a model for the simplest kind of concatenative morphology is emerging. Namely, that two sets of random strings, $B$ and $S$, combine in some way to form a set of words $W$. For Gelbukh et al. (2004), the segmentation task is to find minimal size $|X|+|Y|$ such that $W \subset\{x y \mid x \in$ $X, y \in Y\}$. For Bacchin et al. (2005) as well as in the word-segmentation version of Deligne (1996), the segmentation task is to find a configuration of splits for each $w=x y \in W$ such that each $x$ and $y$ occur in as many splits as possible (more precisely, the product, over all words, of the number number of splits for the parts $x$ and $y$ should be maximized). Hammarström (2006a) adds that the formation of $W$ from $B$ and $S$ should be such that each $s \in S$ should occur frequently, which has implications for the segmentation strategy. Brent (1999) devises a precise, but more elaborate, way of constructing $W$ from $B$ and $S$, but at the price of a large search space, and whose global maximum is hard to characterize intuitively. Kontorovich et al. (2003), Snyder and Barzilay (2008), Goldwater (2007) and Poon et al. (2009) should also be noted for containing generative models.

## 3 A Naive Theory of Affixation and an Algorithm for Extraction

In this section we present a naive theory on how the simplest kind of affixation in natural languages may behave. The theory allows us to devise an extraction algorithm, i.e., an algorithm that partially undoes the affixation. We discuss the assumptions and thinking behind the theory and algorithm, which actually requires only a few lines to define mathematically. Next, we present and discuss some experimental results on typologically different languages. Finally, we state some conclusions and ideas on future components of unsupervised morphological analysis.

### 3.1 A Naive Theory of Affixation

Notation and definitions:

- $w, s, b, x, y, \ldots \in \Sigma^{*}$ : lowercase-letter variables range over strings of some alphabet $\Sigma$ and are variously called words, segments, strings, etc.
- $s \triangleleft w: s$ is a terminal segment of the word $w$, i.e., there exists a (possibly empty) string $x$ such that $w=x s$
- $b \triangleright w: b$ is an initial segment of the word $w$, i.e., there exists a (possibly empty) string $x$ such that $w=b x$
- $W, S, \ldots \subseteq \Sigma^{*}$ : capital-letter variables range over sets of words/strings/segments
- $f_{W}(s)=|\{w \in W \mid s \triangleleft w\}|$ : the (suffix) frequency, i.e., the number of words in $W$ with terminal segment $s$
- $S_{W}=\{s \mid s \triangleleft w \in W\}$ : all terminal segments of the words in $W$
- $B_{W}=\{b \mid b \triangleright w \in W\}$ : all initial segments of the words in $W$
- $u f_{W}(u)=|\{(x, y) \mid x u y=w \in W\}|:$ the substring frequency of $u$, i.e., the number times $u$ occurs as a substring in the set of words $W$ ( $x$ and $y$ may be empty).
- $n f_{W}(u)=u f_{W}(u)-f_{W}(u)$ : the non-final frequency of $u$, i.e. the substring frequency minus those in which it occurs as a suffix.
- $|\cdot|:$ is overloaded to denote both the length of a string and the cardinality of a set
- ": denotes the empty string

Assume we have two sets of random strings over some alphabet $\Sigma$ :

- Bases $B=\left\{b_{1}, b_{2}, \ldots, b_{m}\right\}$
- Suffixes $S=\left\{s_{1}, s_{2}, \ldots, s_{n}\right\}$

Such that:
Arbitrary Character Assumption (ACA): The probability of each character $c$ in a word $w=x c y \in B, S$ does not depend on the strings $x, y$ around it

Note that $B$ and $S$ need not be of the same cardinality and that any string, including the empty string, could end up belonging to both $B$ and $S$. They need neither to be sampled from the same distribution; pace the requirement, the distributions from which $B$ and $S$ are drawn may differ in how much probability mass is given to strings of different lengths. For instance, it would not be violation if $B$ were drawn from a a distribution favouring strings of length, say, 42 and $S$ from a distribution with a strong bias for short strings.

Next, build a set of affixed words $W \subseteq\{b s \mid b \in B, s \in S\}$, that is, a large set whose members are concatenations of the form $b s$ for $b \in B, s \in S$, such that:

Frequent Flyer Assumption (FFA): The members of $S$ are frequent. Formally: Given any $s \in S: f_{W}(s) \gg f_{W}(x)$ for all $x$ such that $1 .|x|=|s|$; and 2. not $x \triangleleft s^{\prime}$ for all $\left.s^{\prime} \in S\right)$.

In other words, if we call $s \in S$ a true suffix and we call $x$ an arbitrary segment if it neither a true suffix nor the terminal segment of a true suffix, then any true suffix should have much higher frequency than an arbitrary segment of the same length.

One may legimately ask to what extent words of real natural languages fit the construction model of $W$, with the strong ACA and FFA assumptions, stated above. For instance, even though natural languages often aren't written phonemically, it is not difficult to find examples of languages that have phonotactic constraints on what may appear at the beginning or end of a word, e.g., Spanish *st- may not begin a word and yields est- instead. This is a violation of ACA because the probability of observing $s$ is much lower and that of $e$ significantly higher, depending on whether or not the empty string is on the left of it, i.e., when initial. Another violation of ACA is that (presumably all (Ladefoged 2005)) languages disallow or disprefer a consonant vs. a vowel conditioned by the vowel/consonant status of its predecessor. However, for the present extraction algorithm, if a certain element occurs with less frequency than uniform random (the best example would be click consonants which, in some languages, e.g., Eastern !Xóõ (Traill 1994), occur only initially), this is less of a problem in practice.

As for FFA, we may have breaches such as Biblical Aramaic (Rosenthal 1995) where an old $-\bar{a}$ element appears on virtually everywhere on nouns, making it very frequent, but no longer has any meaning synchronically. Also, one can doubt the requirement that an affix should need to be frequent; for instance, the Classical Greek inflectional (lacking synchronic internal segmentation) alternative medial 3p. pl. aorist imperative ending $-\sigma \theta \omega \nu$ (Blomqvist and Jastrup 1998), is not common at all.

Just how realistic the assumptions are is an empirical question, whose answer must be judged by experiments on the relevant languages. In the absense of fully

| Positions | Distance |
| :--- | :--- |
| $\left\\|p_{1}-p_{2}\right\\|$ | 0.47 |
| $\left\\|p_{1}-p_{3}\right\\|$ | 0.36 |
| $\left\\|p_{1}-p_{4}\right\\|$ | 0.37 |
| $\left\\|p_{2}-p_{3}\right\\|$ | 0.34 |
| $\left\\|p_{2}-p_{4}\right\\|$ | 0.23 |
| $\left\\|p_{3}-p_{4}\right\\|$ | 0.18 |

Table 5. Difference between character distributions according to word position.
annotated annotated test sets for diverse languages, and since the author does not have access to the Hutmegs/CELEX gold standard sets for Finnish and English (Creutz and Lindén 2004), we can only give some illustrative experimental data.

ACA: If the probability of a character does not depend on the segment preceding it, it follows that it should not depend on the length of the segment preceding it either. On a New Testament corpus of Basque (Leizarraga 1571) we computed the probability of a character appearing in the initial, second, third or fourth position of the word. Since Basque is entirely suffixing, if it complied to ACA, we'd expect those distributions to be similar. However, when we look at the difference of the distributions in terms of variation distance between two probability distributions $\left(\|p-q\|=\frac{1}{2} \sum_{x}|p(x)-q(x)|\right)$, it shows that they differ considerably especially the initial position proves more special - as shown in Table 5

FFA: As for the FFA, we checked a corpus of bible portions of Warlpiri (Summer Institute of Linguistics 2001). This was chosen because it is one of the few languages known to the author where data was available and which has a decent amount of frequent suffixes which are also long, e.g., case affixes are typically bisyllabic phonologically and five-ish characters long orthographically. Since the orthography employed marks segmentation, it is easy to compute FFA statistics on the words by removing the segmentation marking artificially. Comparing with the lists in Nash (1980:Chapter 2) it turns out that FFA is remarkably stable for all grammatical suffixes occuring in the outermost layer. There are, however, the expected kind of breaches; e.g., a tense suffix $-k u$ combined with a final vowel $-u$ which is frequent in some frequent preceding affixes making the terminal segment -uku more frequent than some genuine three-letter suffixes.

The language known to the author which has shown the most systematic disconcord with the FFA is Haitian Creole (also in bible corpus experiments (American Bible Society 1999)). Haitian creole has very little morphology of its own but owes the lion's share of its words to French. French derivational morphemes abound in these words, e.g., -syon, which have been carefully shown by Lefebvre (2004) not to be productive in

Haitian Creole. Thus, the little morphology there is in Haitian creole is very difficult to get at without also getting the French relics.

### 3.2 An Algorithm for Affix Extraction

The key question is, if words in natural languages are constructed as $W$ explained above, can we recover the segmentation? That is, can we find $B$ and $S$, given only $W$ ? The answer is yes, we can partially decide this. To be more specific, we can compute a score $Z_{W}$ such that $Z_{W}(x)>Z_{W}(y)$ if $x \in S$ and $y \notin S$. In general, the converse need not hold, i.e., if both $x, y \in S$, or both $x, y \notin S$, then it may still be that $Z_{W}(x)>Z_{W}(y)$. This is equivalent to constructing a ranked list of all possible segments, where the true members of $S$ appear at the top, and somewhere down the list the junk, i.e., non-members of $S$, start appearing and fill up the rest of the list. Thus, it is not said where on the list the true-affixes/junk border begins, just that there is a consistent such border.

Now, how should this list be computed? All terminal segments are contained in the set $S_{W}$, the question is just to order them. We shall now define three properties that we argue will be enough to put the $S$-belonging affixes at the top. For a terminal segment $s$, define:

Frequency The frequency $f_{W}(s)$ of $s$ (as a terminal segment).
Curve Drop First, for $s$, define its curve $C_{s}(c)$ which is a probability distribution on $\Sigma$ :

$$
C_{s}(c)=\frac{f_{W}(c s)}{f_{W}(s)}
$$

Next, more importantly, define its curve $\operatorname{drop} \bar{C}(s)$ which is a value in $[0,1]$ :

$$
\bar{C}(s)=\frac{1-\max _{c}\left(C_{s}(c)\right)}{1-\frac{1}{|\Sigma|}}
$$

Random Adjustment First, for $s$, define its probability as:

$$
P_{W}(s)=\frac{f_{W}(s)}{\sum_{s^{\prime}} f_{W}\left(s^{\prime}\right)}
$$

Second, equally straighfowardly, for an arbitrary segment $u$, define its non-final probability as:

$$
n P_{W}(u)=\frac{n f_{W}(u)}{\sum_{u^{\prime}} n f_{W}\left(u^{\prime}\right)}
$$

Finally, for a terminal segment $s$, define its random adjustment $R A(s)$ which a value in $Q^{+}$:

$$
R A(s)= \begin{cases}\frac{P_{W}(s)}{n P_{W}(s)} & \text { if } n P_{W}(s)>0 \\ 1.0 & \text { otherwise }\end{cases}
$$

It is appropriate now to show the intuition behind the definitions. There isn't much to comment on frequency, so we'll go to curve drop and random adjustment. All examples in this section come from the Brown corpus (Francis and Kucera 1964) of one million tokens $\left(|W|=47178\right.$ and $\left.\left|S_{W}\right|=154407\right)$.

The curve drop measure is meant to predict when a suffix is well-segmented to the left. Consider a suffix $s$, in all the words on which it appears, there is a preceding character $c$. Figure 1 shows examples of the frequency distribution on preceding character for example suffixes -ing and -ng. The reasoning is as follows. If $s$ is a true suffix and is well-segmented to the left, then its curve-drop value should be high. Frequent true suffixes that attach to bases whose last character is random should have a close to uniform curve. On the other hand, if the curve drop value is low it means there is a character that suspiciously often precedes $s$. However, if $s$ weren't a true suffix to begin with, perhaps just a frequent but random character, then we expect its curve drop value to be high too! To exemplify this, we have $\bar{C}(i n g) \approx 0.833, \bar{C}(n g) \approx 0.029$ and $\bar{C}(a) \approx 0.851$.

The random adjustment measure it precisely to distinguish what a "frequent but random segment" is, that is, discriminate, e.g., $-a$ versus -ing as well as -a versus -ng. Now, how does one know whether something is random or not? One approach would be to say the shorter the segment the more random. Although it is possible to get this to work reasonably well in practice, it has some drawbacks. First, it treats all segments of the same length the same, which may be too brutal, e.g., should $-s$ be penalized as much as -a? Second, it might be considered too vulnerable to orthography. For example if a language has an odd trigraph for some phoneme, we are clearly going to introduce an error source. Instead we propose that a segment is random iff it has similar probability in any position of the word. This avoids the "flat length"-problems but has others, which we think are less harmful. First, we might get sparse data which can either be back-off smoothed or, like here, effectively ignored (where we lack occurence we set the $R A$ to 1.0). Second, phonotactic or orthographic constraints may cause curiousities, e.g., English $y$ is often spelled $i$ when medial as in $f l y$ vs. flies.

To put it all together, we propose the characterization of suffixes in terms of the three properties as shown in Table 6. The terms high and low are of course idealized, as they are really gradient properties.

As seen from the table, we hold that true suffixes (and only true suffixes) are those which have a high value for all three properties. Therefore, we define our final ranking score, the $Z_{W}: S_{W} \rightarrow \mathbf{Q}$ :

$$
\begin{equation*}
Z_{W}(s)=\bar{C}(s) \cdot R A(s) \cdot f_{W}(s) \tag{1}
\end{equation*}
$$

Thus we are deliberate saying that if you have a not-so-high relative value for one of the properties, you can compensate to some extent by having very


Figure 1. The curve frequencies giving rise to the curves $C_{i n g}$ and $C_{n g}$ respectively.

| $f_{W}$ | $\bar{C}$ | $R A$ | Example | Label |
| ---: | ---: | ---: | ---: | :--- |
| high | high | high | - ing | True suffix |
| high | high | low | $-a$ | Frequent random segment |
| high | low | high | $-n g$ | Tail of true suffix |
| high | low | low | N/A | Second part of a digraph |
| low | high | high | - oholic | Infrequent true suffix |
| low | high | low | $-w e$ | Happenstance low RA-segment? |
| low | low | high | $-i c z$ | Tail of foreign personal name ending |
| low | low | low | -ebukadnessar | Infrequent segment |

Table 6. The logically possible condigurations of the three suffix properties, accompanied by an appropriate linguistically inspired label and an example from English.
high relative values for the other properties (relative here means relative to the corresponding values of other suffixes). It is instructive to look at what happens in a few interesting cases:

1. We have two suffixes such that one is an enlargement of the other by a random segment, e.g., -ting versus -ing, where the true suffix is the shorter one.
In this case, we expect both to have similar high $\bar{C}$, the longer one should have higher $R A$ and, by necessity, the shorter one should have signficantly higher frequency. Example values for -ing versus -ting are shown in Table 7

Here, we see that the shorter wins out and we can use that fact to weed out the longer one (cf. purging below). (One might think that in a "perfect" situation, the $f_{W}$ and $R A$ would cancel out, leaving the situation a tie. However, $R A$ will not cancel $f_{W}$ in a language which, like all languages we know of, has more non-final than final "positions of segments in words", and also, ceteris paribus, we expect a higher frequency to yield a more reliable curve drop value.)
2. We have two suffixes such that one is a tail of the other, but both are true suffixes, and they just happen to share a segment, e.g., -ly versus $-y$.
In this case, we succeed in keeping both if the longer wins out on a better curve-drop and random adjustment. In fact, as shown in Table 7 this is exactly what happens with $-l y$ versus $-y$.
3. We have two true suffixes which incidentally share an ending which is not a true suffix. Although easy to find in other languages, I failed to find an example of this in English without confounding factors, but we can imagine one, for example $-x z$ versus $-y z$. Given the assumption that $-z$ itself is not a true suffix, $f_{W}(z)$ should not be many times higher than $f_{W}(x z)+f_{W}(y z)$, thus its curve-drop not many percent, if at all, higher

| s | $f_{W}(s)$ | $\bar{C}(s)$ | $R A(s)$ | $Z_{W}(s)$ |
| ---: | ---: | ---: | ---: | ---: |
| - ing | 3258 | 0.83 | 19.6 | 53309.3 |
| -ting | 640 | 0.69 | 31.5 | 13929.5 |
| $-y$ | 3931 | 0.63 | 5.8 | 14402.7 |
| $-l y$ | 1532 | 0.76 | 23.4 | 27282.2 |
| $-t$ | 2796 | 0.74 | 0.50 | 1040.6 |
| $-s t$ | 561 | 0.64 | 0.68 | 246.3 |
| $-i s t$ | 202 | 0.81 | 1.29 | 213.9 |
| -est | 213 | 0.88 | 1.82 | 341.4 |
| $-s$ | 11220 | 0.80 | 2.49 | 22514.8 |
| -ings | 205 | 0.89 | 60.5 | 11034.2 |
| -ations | 215 | 0.86 | 110.9 | 20482.1 |

Table 7. Values for some borderline cases.
than 0.5 , and of course, $R A(z) \approx 1$. On the other hand, by assumption of being true suffixes, $-x z$ and $-y z$ should have high curve-drop values, and outperform $-z$ on $R A$.
Empirically, the prediction is wrong in the case -est versus -est, as shown in 7 But, on the other hand, -ist and -est can hardly be said to satisfy FFA.
4. We have two true stacked suffixes which share an ending and this ending is also true suffix, e.g., -ations versus -ings.
As opposed to the above case, $-s$ will appear in a lot of other places than after -ing and -ation, and is consequently given a higher score as shown in Table 7

As these considerations exemplify, the formal criterion mostly conforms to linguistic analysis, but as noted as noted in the third example, the outcomes occasionally disconcords with linguistic analysis.

A theoretical weakness with the $R A$-value as computed at present is when applied to languages which stack suffixes after each other. English does this to a small extent, as in -ing vs. -ings. In such cases, when calculating the non-final frequency of -ing one would like to count an occurence of -ing-in -ings as a final occurence. But this would require knowing beforehand that $-s$ is a true suffix as opposed to -ings. Fortunately, the impact of this drawback, for languages such as English where stacking is rather uncommon, appears not to be crucial. Even if suffixes occur when they are "almost" final, they still don't occur in the when initial or in the mid-span of the word.

As a last discussion note, it is tempting to leave out the $f_{W}$-component in the calculation of the ranking. The frequency is really only needed when deciding between suffixes which are tails of each other - it plays no crucial role in ranking between suffixes which don't share a tail. If frequencies are used only to purge out losers in tail-indexed sets of suffixes, the resulting list will also

Input: A text corpus $C$
Step 1. Extract the set of words $W$ from $C$ (thus all contextual and wordfrequency information is discarded)

Step 2. Calculate $f_{W}(s), \bar{C}(s)$ and $R A(s)$ for each $s \in S_{W}$
Step 3. Combine $Z_{W}(s)=\bar{C}(s) \cdot R A(s) \cdot f_{W}(s)$

Table 8. Summary of affix-extraction algorithm.
contain some non-FFA true suffixes but also too many spurious things, such as foreign personal name endings.

To sum up, the final $Z_{W}$-score in equation 1 is the one that purports to have the property that $Z_{W}(x)>Z_{W}(y)$ if $x \in S_{W}$ and $y \notin S_{W}$ - at least if purged (see below). We cannot give a formal proof that languages satisfying ACA and FFA should get a faultless ranking list because this is true only in a heuristic sense. To set bounds on the probability for it to hold is also depends on a lot of factors that are hard, or at least inelegant, to characterize. We hope, however, to have sketched the how the ACA and FFA assumptions are used.

A summary of the algorithm described in this section is displayed in Table 8.

The time-complexity bounding factor is the number of (final and non-final) segments, which is linear (in the size of the input) if words are bounded in length by a constant and quadratic in the (really) worst case if not.

### 3.3 Experimental Results

For an English bible corpus (King James 1977) we get the top 30 plus bottom 3 suffixes as shown in Table 9

English has little affixation compared to, e.g., Turkish which is at the opposite end of the typological scale (Drver 2005). The corresponding results for Turkish on a bible corpus (American Bible Society 1988) is shown in Table 10

The results largely speak for themselves but some comments are in order. As is easily seen from the lists, some suffixes are suffixes of each other so one could purge the list in some way to get only the most "competitive" suffixes. One purging strategy would be to remove $x$ from the list if there is a $z$ such that $x=y x$ and $Z_{W}(z)>Z_{W}(x)$ (this would remove, e.g., -ting if -ing is above it on the list). A more sophisticated purging method is the following, which does slightly more. First, for a word $w \in W$ define its best segmentation as: $\operatorname{Segment}(w)=\operatorname{argmax}_{s \triangleleft w} Z_{W}(s)$. Then purge by keeping only those suffixes which are the best parse for at least one word: $S_{W}^{\prime}=\left\{s \in S_{W} \mid \exists w \operatorname{Segment}(w)=\right.$ $s\}$.

Such purging kicks out the bulk of "junk" suffixes. Table 11 shows the numbers for English, Turkish and the virtually affixless Maori (Bauer et al. 1993). It should noted that "junk" suffixes still remain after purging - typically

| -ed | 15448.4 | $-s$ | 3407.3 |
| ---: | ---: | ---: | ---: |
| -eth | 12797.1 | -ions | 2684.5 |
| -ted | 11899.4 | -est | 2452.6 |
| -iah | 11587.5 | -sed | 2313.7 |
| -ly | 10571.2 | $-y$ | 2239.2 |
| -ings | 8038.9 | -leth | 2166.3 |
| -ing | 7292.8 | -nts | 2122.6 |
| -ity | 6917.6 | -ied | 1941.7 |
| -edst | 6844.7 | -ened | 1834.9 |
| -ites | 5370.2 | -ers | 1819.5 |
| -seth | 5081.6 | -ered | 1796.7 |
| -ned | 4826.7 | -ded | 1582.2 |
| -s, | 4305.2 | -neth | 1540.0 |
| -nded | 3833.8 | $\ldots$ | $\ldots$. |
| -ts | 3783.1 | -ig | 0.0 |
| -ah | 3766.9 | -io | 0.0 |
| -ness | 3679.3 | -ti | 0.0 |

Table 9. Top 30 and bottom 3 extracted suffixes for an English bible corpus. The high placement of English -eth and -iah are due to the fact that the bible version used has drinketh, sitteth etc and a lot of personal names in -iah.
common stem-final characters - and that there is no simple relation between the number of suffixes left after purging and the amount of morphology of the language in question. Otherwise we would have expected the morphology-less Maori to be left with no, or 28 -ish, suffixes or at least less than English.

A good sign is that the purged list and its order seems to be largely independent of corpus size (as long as the corpus is not very small) but we do get some significant differences between bible English and newspaper English.

We have chosen to illustrate using affixes but the method readily generalizes to prefixes as well and even prefixes and suffixes at the same time. As an example of this, we show top-10 purged prefix-suffix scores in the same table also for some typologically differing languages in Table 12, Again, we use bible corpora for cross-language comparability (Swedish (Svenska Bibelsällskapet 1917) and Swahili (British \& Foreign Bible Society 1953)). The scores have been normalized in each language to allow cross-language comparison - which, judging from the table, seems meaningful. Swahili is an exclusively prefixing language but verbs tend to end in $-a$ (whose status as a morpheme is the linguistic sense can be doubted), whereas Swedish is suffixing, although some prefixes are or were productive in word-formation.

A full discussion of further aspects such as a more informed segmentation of words, peeling of multiple suffix layers and purging of unwanted affixes requires, is beyond the scope of this paper.

| -larına | 71645.4 | -adılar | 16587.9 |
| ---: | ---: | ---: | ---: |
| -larindan | 47941.9 | -lerinden | 15201.1 |
| -lerinin | 43917.3 | -nden | 14082.2 |
| -lerden | 36294.0 | -sinin | 13493.9 |
| -inden | 35258.2 | - nin | 12340.9 |
| -iyorlardı | 28716.2 | -yorsunuz | 12135.0 |
| -arak | 27774.1 | - -larla | 12069.7 |
| -iyorsunuz | 25403.1 | $-e n$ | 11513.5 |
| -inin | 25045.5 | - ten | 11424.0 |
| -dılar | 20718.7 | - siniz | 11043.0 |
| -lere | 20718.2 | -madılar | 10958.9 |
| -ip | 20431.2 | -lardan | 10428.1 |
| -dan | 19468.4 | - -siniz | 10391.1 |
| -ndan | 18556.3 | $-\ldots$ | $\ldots$ |
| -indan | 18226.3 | - -ist | 0.0 |
| -yorlardl | 18097.1 | $-i y$ | 0.0 |
| -acaksiniz | 16751.1 | $-y o$ | 0.0 |

Table 10. Top 30 and bottom 3 extracted suffixes for Turkish. Most of these are really compounds of two suffixes, showing that some adaptation to multi-layer suffixing languges is appropriate.

|  | Corpus | Tokens | $\|W\|$ | $\left\|S_{W}\right\|$ | $\left\|S_{W}^{\prime}\right\|$ |
| :--- | :--- | ---: | ---: | ---: | ---: |
| Maori | British \& Foreign Bible Society | 1101665 | 8354 | 23007 | 78 |
| English | $\mathbf{1 9 9 6}$ | King James 1977 | 917634 | 12999 | 39845 |
| Turkish | American Bible Society 1988 | 574592 | 56881 | 175937 | 122 |

Table 11. Figures for different languages on the effects on the size of the suffix list after purging.

### 3.4 Conclusion

We have presented a new theory of affixation and a parameter-less efficient algorithm for collecting affixes from raw corpus data of an arbitrary language. Depending on one's purposes with it, a cut-off point for the collected list is still missing, or at least, we do not consider that matter here. The results are promising and competitive but at present we lack formal evaluation in this respect. Future directions also include a more specialized look into the relation between affix-segmentation and paradigmatic variation and further exploits into layered morphology.

## Acknowledgements

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| Swedish |  | English |  | Swahili |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| för- | 0.097 | -ed | 0.132 | - $a$ | 0.100 |
| -en | 0.086 | -eth | 0.109 | wa- | 0.095 |
| -na | 0.036 | -iah | 0.099 | ali- | 0.065 |
| - ade | 0.035 | -ly | 0.090 | nita- | 0.059 |
| - $a$ | 0.034 | -ings | 0.068 | aka- | 0.049 |
| -ar | 0.033 | -ing | 0.062 | ni- | 0.046 |
| -er | 0.033 | -ity | 0.059 | ku- | 0.044 |
| -as | 0.032 | -edst | 0.058 | ata- | 0.042 |
| -s | 0.031 | -ites | 0.046 | ha- | 0.032 |
| -de | 0.031 | $-s$ ' | 0.036 | $a$ - | 0.031 |
|  |  |  |  |  |  |

Table 12. Comparative figures for prefix vs. suffix detection.
in an earlier version of this paper. We also wish to extend special thanks to ASEDA for granting access to electronic versions of the Warlpiri bible texts.

## 4 Affix Alternation

An important generalization concerns that of how affixes and stems may and may not combine. In many languages, not all affixes can occur on all stems, rather, one finds that affixes form groups, where each group is associated with a subset of stems on which any affix from the group may occur. We may call such a group of affixes a paradigm. For example, according to linguistic analysis of English morphology, the suffix set $\left\{-i n g,-e d,-s,-{ }^{\prime \prime},-e r,-e r s\right\}$ can be argued to form a valid paradigm which occurs on stems such as 'play' and 'ask' but not 'bus', whereas $\{-x t,-i n g,-b l u r b,-a t i o n\}$ is not a valid paradigm.

In the present section we develop a method to find morphological paradigms given raw text data. First we go through some key properties of paradigms which have immediate bearing on how to formally characterize paradigms and explain why baseline approaches such as $k$-means clustering on Hamming distance are less attractive. Next we introduce a metric that takes a candidate paradigm and gives a score between 0 and 1 indicating "how much" the affixes in the paradigm occur on the same stems, i.e., how "good" the paradigm is. This metric can then be used for greedy searching through the paradigm space to find locally optimal paradigms. The resulting paradigms, with their scores, can be used in various applications (as in the coming sections of this chapter) and are evaluated indirectly this way. We have not yet conceived a final "extraction"phase to extract all the salient paradigms (or the like), wherefore there is no evaluation simpliciter against some gold standard of paradigms.

### 4.1 Paradigms

## The Nature of Paradigms

For our purposes, the definition of a paradigm is a maximally large set of affixes whose members systematically occur on an open class of stems. There are a few things to note:

- The number of theoretically possible paradigms is exponential in the number of affixes (as paradigms are sets of affixes).
- Empirically, languages tend to have a small number of paradigms.
- Empirically, languages tend to have only small paradigms, i.e., the number of affixes in each paradigm is small. Languages which have several layers of affixes can be said to obey generalization in the sense that each layer has few members, whereas, conversely, the full paradigm achieves considerable size combinatorially.
- Paradigms do not need to be disjoint (in real languages they are typically not)


## The Evidence for Paradigms

Without any language specific knowledge, basically the only evidence at hand is co-occurrence of stems and affixes (i.e., when a word occurs in the corpus it evidences the co-occurrence of a (hypothetical) stem and suffix making up that word). Seen like this, the problem at hand bears obvious similarities to other areas of computational linguistics, e.g., word/document co-occurrence models in Information Retrieval (Baeza-Yates and Ribeiro-Neto 1997) or word/word co-occurrence in Part-of-Speech clustering (Redington et al. 1998, Pereira et al. 1993, Schütze 1993), and belongs more generally within a vector space pattern classification framework (Duda et al. 2001, Gordon 1999).

Paradigm induction would be an easy problem if all affixes that could legally appear on a word did appear on each such word in a raw text corpus. This is, as is well-known, far from the case. A typical corpus distribution is that a few lexemes appear very frequently but by far most lexemes appear once or only a few times (Baayen 2001). What this means for morphology is that most lexemes will appear with only one or a minority of their possible affixes, even in languages with relatively little morphology.

More formally, consider a morphological paradigm (set of suffixes) $P$ that is a true paradigm according to linguistic analysis. If $k$ lexemes that are conjugated according to $P$ occur in a corpus, each of the $k$ lexemes will occur in $1 \leq i \leq|P|$ forms. The number of forms $i$ that a lexeme occurs in will not be normally distributed. Most lexemes will occur in only one form, and only very few, if any, lexemes will occur in all $|P|$ forms. It appears that for most languages and most paradigms, the number of lexemes that occur in $i$ forms tends to decrease logarithmically in $i$.

The second challenge is segmentation noise. In general, an unsupervised learner has no lexical resource to distinguish between lookalikes, i.e., words that happen to end in one of the paradigm's members, and lexemes that are truly $P$-conjugated. For example, a word such as 'bilen' looks just as much *'bile-n' as the correct 'bil-en'. Segmentation ignorance will obviously introduce a lot of spurious stem-affix pairs into consideration.

### 4.2 Paradigm Induction Techniques

## Binary Vector Similarity Measures

It is instructive to look at the most straightfoward approach to the problem at hand. Consider the co-occurrence matrix $M: S_{W} \times B_{W}$ engendered by the set of words $W$ in some input corpus.

$$
M_{x y}=1 \text { iff } x y \in W\left(\text { and } M_{x y}=0 \text { otherwise }\right)
$$

For example, such a matrix could begin as in Table 13
The rows in the matrix make up binary vectors in the $\left|B_{W}\right|$-dimensional stem space. Thus one potential line of attack is to characterize each suffix by its stemoccurrence binary vector. This is especially attractive given the long history and

|  | play- | drink- | s- | $\ldots$ |
| :--- | :--- | :--- | :--- | :--- |
| -ing | 1 | 1 | 1 |  |
| -ed | 1 | 0 | 0 |  |
| -s | 0 | 1 | 0 |  |
| -axophone | 0 | 0 | 1 |  |
| $\ldots$ |  |  |  |  |

Table 13. Contrived example fragment of a plausible co-occurrence matrix.

| $(\mathrm{x}, \mathrm{y})$ | $\operatorname{Sim}_{1}(x, y)$ | $\operatorname{Sim}_{2}(x, y)$ |
| :--- | ---: | ---: |
| (s, t) | 0.9052 | 0.0005 |
| (ing, ng) | 0.9608 | 0.0000 |
| (ation, ed) | 0.9678 | 0.0004 |
| (ed, ing) | 0.9708 | 0.0107 |
| (ed, nrighteousness) | 0.9803 | 0.0000 |
| (ebuchadnezzar, ing) | 0.9807 | 0.0000 |
| (ebuchadnezzar, nrighteousness) | 0.9999 | 0.0000 |

Table 14. Sample similarity values using Hamming distance, computed from an English bible corpus (King James 1977). $\operatorname{Sim}_{1}(x, y)$ counts the number of matches between $x$ and $y$ :s vectors and $\operatorname{Sim}_{2}(x, y)$ counts only the number of positive matches only. Both are normalized to $\left|B_{W}\right|$.
success of binary vector similarity approaches for other pattern classification problems (see Hyuk-Cha et al. (2005) for one of many surveys). One obvious approach to the problem at hand would then be to do $k$-means clustering on the set of suffixes using a vector distance such as Hamming distance.

Let us first consider Hamming distances. As explained in Hyuk-Cha et al. (2005), for other problems, the outstanding issue has been whether to count negative matches or not (or, alternatively to use supervised learning to train corresponding weights). Table 14 exemplifies the Hamming distance between a selection of suffixes from an English bible corpus (King James 1977). $\operatorname{Sim}_{1}(x, y)$ counts the number of matches between $x$ and $y$ :s vectors. $\operatorname{Sim}_{2}(x, y)$ counts only the number of positive matches, i.e., matching occurrences of 1. Both are normalized to $\left|B_{W}\right|$.

Clearly, in our situation, counting negative matches will favour matches between suffixes that are very uncommon (especially since we do not here consider the matter of well-segmentedness to counteract). On the other hand, counting only positive matches will favour matches between suffixes that are common, e.g., two one-character suffixes, even if they do not actually contrast in the language. The only solution seems to be to use proportions, but this does not without effort result in a distance metric. Thus in the next section we introduce a metric which has a lot in common in Mutual Information. Various tf-idf-related (Baeza-Yates and Ribeiro-Neto 1997) measures could also be considered.

Crucially, $k$-means clustering on most simple vector distances yields very
poor results. What tends to happen is that two suffixes of some true $P$ form a tight pair and won't let the other members of $P$ in, which are instead sucked into large clusters of junk. Therefore, except for languages where all paradigms are of cardinality 2 (if such languages exist), we have less faith in developing an approach based on strictly binary distances.

### 4.3 Formalizing Same Stem Co-Occurrence

As explained above, from the word distributions characteristic of natural language corpora, it is not straightforward to come up with a measure of how much a set of suffixes show up on the "same stems" that is not such that it favours the inclusion of any simply frequent, rather than truly contrasting, terminal segment. The measure we present here is valid for an arbritrary set of suffixes, including pairs (size two sets) but not restricted to pairs.

First, for each suffix $x$, define its quotient function $H_{x}(y): S_{W} \rightarrow[0,1]$ as:

$$
\begin{equation*}
H_{x}(y)=\frac{\mid \operatorname{Stems}(x) \cap \operatorname{Stems}(y)\} \mid}{|\operatorname{Stems}(x)|} \tag{2}
\end{equation*}
$$

where $\operatorname{Stems}(x)=\{z \mid z x \in W\}$. The formula is conveying the following. We are given a suffix $x$, and we want to construct a quotient function which is a function from any other suffix to a score between 0 and 1 . The score is calculated as: look at all the stems of $x$, other suffixes $y$ will undoubtedly also occur on some of these stems. For each other suffix $y$, find the proportion of $x$ :s stems on which $y$ also appears. This proportion will be the quotient associated with $y$. Two examples of quotient functions (sorted on highest value) are given in Table 15.

Now, given a set of affixes $P$, construct a rank by summing the quotient functions of the members of $P$ :

$$
\begin{equation*}
V_{P}(y)=\sum_{x \neq y \in P} H_{x}(y) \tag{3}
\end{equation*}
$$

The $x \neq y$ is just there so that the $y:$ s that are also in $P$ do not get an "extra" 1.0 , since $H_{x}(x)=1.0$ for any data. The rank is just $y$ sorted on highest $V_{P}(y)$.

As an example, take $W$ from the Swedish PAROLE-Corpus (Borin 1997). We can compare in Table 16 the very common paradigm $\{a, a n, a s, a n s$, or, orna, ors, ornas $\}$ with the nonsense paradigm $\{u n g e n, i g, a r, t s, s, d e, e n d e, e r\}$ consisting only of individually frequent suffixes. In Table 16, the ranks of the members of $P$ to the left are $[0,1,2,4,6,8,22,31]$, and for $P$ to the right, the ranks are [115044, 127, 17, 28, 4, 10, 100236, 14].

Now, if we can generalize from these cases it seems that we can rank different hypotheses of paradigms (of the same size) by looking at their quotient ranks. If the members of $P$ "turn up high in" the quotient rank then the members of $P$ tend to turn up on the same stems. There are several issues in formalizing the notion of "turn up high in". The places in the ranked list alone? Also incorporate the scores? Average place or total sum of places? For now we will

| $y$ | $H_{\text {ing }}(y)$ | $y$ | $H_{e d}(y)$ |
| :--- | ---: | :--- | ---: |
| ing | 1.00 | ed | 1.00 |
| ed | 0.59 | ing | 0.42 |
| $\prime \prime$ | 0.41 | $\prime \prime$ | 0.33 |
| $s$ | 0.25 | $e$ | 0.21 |
| $e$ | 0.24 | $s$ | 0.20 |
| es | 0.19 | es | 0.17 |
| er | 0.12 | er | 0.08 |
| ers | 0.10 | ion | 0.07 |
| ion | 0.07 | ers | 0.05 |
| $y$ | 0.05 | $y$ | 0.04 |
| ings | 0.05 | ions | 0.03 |
| ions | 0.03 | ation | 0.03 |
| in | 0.03 | able | 0.02 |
| ation | 0.03 | ings | 0.02 |
| 's | 0.03 | 's | 0.02 |
| ingly | 0.03 | or | 0.02 |
| or | 0.02 | in | 0.01 |
| able | 0.02 | ly | 0.01 |
| ive | 0.02 | ive | 0.01 |
| ors | 0.02 | ingly | 0.01 |
| ations | 0.01 | al | 0.01 |
| er's | 0.01 | ment | 0.01 |
| ment | 0.01 | ors | 0.01 |
| ly | 0.01 | ations | 0.01 |
| $\ldots$ | $\ldots$ | $\ldots$ | $\ldots$ |

Table 15. Sample quotient functions/lists for ing and ed on the Brown Corpus. $H_{\text {ing }}$ and $H_{e d}$ have 68337 and 75853 nonzero values respectively.

| y | $V_{P}(y)$ | y | $V_{P}(y)$ |
| :--- | ---: | :--- | ---: |
| a | 3.93 | $"$ | 3.32 |
| an | 2.82 | t | 1.48 |
| or | 2.71 | a | 1.19 |
| " | 1.91 | r | 1.18 |
| orna | 1.76 | s | 1.15 |
| ar | 1.13 | en | 1.14 |
| as | 1.06 | iga | 0.86 |
| ade | 1.05 | d | 0.80 |
| ans | 0.94 | igt | 0.73 |
| at | 0.89 | as | 0.66 |
| en | 0.82 | de | 0.59 |
| s | 0.76 | des | 0.57 |
| t | 0.73 | ade | 0.55 |
| e | 0.71 | ung | 0.49 |
| er | 0.66 | er | 0.49 |
| ad | 0.61 | at | 0.48 |
| ande | 0.52 | n | 0.46 |
| ades | 0.47 | ar | 0.45 |
| ats | 0.40 | an | 0.44 |
| i | 0.36 | e | 0.42 |
| $\ldots$ | $\ldots$ | $\ldots$ | $\ldots$ |
| ors | 0.35 |  |  |
| $\ldots$ | $\ldots$ |  |  |
| ornas | 0.27 |  |  |
| $\ldots$ | $\ldots$ |  |  |

Table 16. Example ranks for $P=$ \{a, an, as, ans, or, orna, ors, ornas $\}$ (left) and $P=\{u n g e n, i g, a r, t s, s, d e, e n d e, e r\}$ (right).

| $P$ | $V I(P)$ |  | $P$ | $V I(P)$ |
| :--- | ---: | :--- | ---: | ---: |
| \{'ation'\} | 0.00 |  | \{'xt'\} | 0.00 |
| \{'ated', 'ation'\} | 0.14 |  | \{'xt','n'\} | 0.04 |
| \{'ate', 'ated', 'ation'\} | 0.40 |  | \{'xt', 'n', 'ns'\} | 0.12 |
| \{'ate', 'ated', 'ating', 'ation'\} | 0.75 |  | \{'n','ns'\} | 0.55 |
| \{'ate', 'ated', 'ating', 'ation', 'ations'\} | 1.00 | $\ldots$ | $\ldots$ |  |

Table 17. Example iterations of $G^{*}\left({ }^{\prime}\right.$ ation') and $G^{*}\left({ }^{\prime} x t^{\prime}\right)$.
just do a simple sum of places in the ranked list, divide by the optimum sum (which depends on $|P|$ and is $0+\ldots+|P|-1$ ), and take the inverse. This gives a score between 0 and 1 where a high score means the members of $P$ tend to appear on the same stems:

$$
\begin{equation*}
V I(P)=\frac{|P|(|P|-1)}{2 \sum_{x \in P} \operatorname{place}\left(x, V_{P}\right)} \tag{4}
\end{equation*}
$$

The $V I$-score from the last section may be used for a greedy hill-climbing search through the affix set space. For example, we may start with an affix, a one member set, and see whether we can improve the affix score by including another member, and perhaps another after that until we cannot improve the score anymore. One such ever-expanding search through the affix set space is bounded by the total number of affixes and is thus polynominal in the number of affixes. A bolder alternative is to also entertain the possibility of kicking some member out if that improves the score. Then, in the worst case, we may have to step through the whole affix set space before convergence. In practice, however, searches are not at all close to exploring large parts of the affix set space before converging, so allow expulsions is not prohibitive. Formally, define the growing function of a set $P$ of affixes as:

$$
\begin{gather*}
G(P)=\operatorname{argmax}_{p \in\{P\} \cup\left\{P \cup\{s\} \mid s \in S_{W}\right\} \cup\left\{P \backslash\{s\} \mid s \in S_{W}\right\}} V I(p)  \tag{5}\\
G^{*}(P)= \begin{cases}P & \text { if } G(P)=P \\
G^{*}(G(P)) & \text { if } G(P) \neq P\end{cases} \tag{6}
\end{gather*}
$$

Two growth-examples are shown in Table 17, one which attains a perfect 1.0 score and one in which the original member is expelled in a later iteration.

### 4.4 Discussion

Impressionistically, the growing algorithm makes sense. Where one as a linguist has sure intentions, the score tends to agree. For example, $G^{*}(i n g)=$ $\left\{{ }^{\prime \prime}, e, e d, e s, i n g, s\right\}$, and $G^{*}(i e d)=\{i e d, i e s, y, y i n g\}$. However, the $V I(P)$-score knows nothing about well-segmentatedness, so, e.g., VI(\{'xcellent',' xcellently' $\})=$ 1.0. It is clear that scores for well-segmentedness could come from a different component, such as the affix extraction algorithm in Section3, and, indeed, such combinations are variously explored in the applications sections of the present

| $s_{1^{-}}$ | $s_{2^{-}}$ | $s_{3^{-}}$ | $s_{4^{-}}$ | $s_{5^{-}}$ | $s_{6^{-}}$ | $s_{7^{-}}$ | $s_{8^{-}}$ | $s_{9^{-}}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $s_{1} a$ | $s_{2} a$ | $s_{3} a$ | $s_{4} b$ | $s_{5} b$ | $s_{6} b$ | $s_{7} c$ | $s_{8} c$ | $s_{9} c$ |
| $s_{1} x$ | $s_{2} x$ | $s_{3} x$ | $s_{4} y$ | $s_{5} y$ | $s_{6} y$ | $s_{7} z$ | $s_{8} z$ | $s_{9} z$ |
|  |  |  |  |  |  |  |  |  |
|  |  |  | $s_{10^{-}}$ | $s_{11^{-}}$ | $s_{12^{-}}$ |  |  |  |
|  |  |  | $s_{10} a$ | $s_{11} a$ | $s_{12} d$ |  |  |  |
|  |  |  | $s_{10} b$ | $s_{11} b$ | $s_{12} b$ |  |  |  |
|  |  |  | $s_{10} c$ | $s_{11} c$ | $s_{12} c$ |  |  |  |

Table 18. Definition of a set $W(|W|=27)$ of strings arranged according to prefix for readability.
chapter. However, we have not yet conceived a final "extraction"-phase to extract all the salient paradigms (or the like), wherefore there is no evaluation simpliciter against some gold standard of paradigms.

Since paradigms tend to be small, growing from a single paradigm is a better heuristic than shrinking from the whole affix set space. However, it still happens frequently for large $|P|(10-20)$ that the growing sticks in a local maximum. And for languages, e.g., Turkish, with paradigms that number hundreds of members (because they are really combinatorial in nature) the approach is not sufficient alone.

The paradigm-growing approach, as opposed to many fixed-cluster approaches, has the positive side-effect that one affix can readily be the member of several locally maximal paradigms. Though for each paradigm, there needs to be at least one starting-affix that grows towards it.

In practice, growing paradigms take a long time because of sorting and summing with very long lists (typically 100000-ish items).

It is important to note the set-oriented (rather than pair-oriented) nature of this measure. Let us say $x$ is at the top of $y$ :s quotient list $H_{y}$ (except for $y$ itself) and $y$ is at the top of $H_{x}$ (except for $x$ self). Even so, $V I(\{x, y\})$ might get a smaller score than $V I(\{x, y, z\})$ with the inclusion of another member $z$. This depends, of course, but crucially $z$ may get a lot of "points" both from $H_{x}(z)$ and $H_{y}(z)$ whereas $x$ doesn't get points from $H_{x}$ nor $y$ from $H_{y}$.

The $V I(P)$-measure cannot be reduced to a monotone function of the set of $V I(P)$-values for the set of suffix-pairs in $P$ as the following counterexample shows. (Unfortunately I do not know of a smaller counterexample.). Let $W$ be the strings in the cells of the tables in [18, arranged according to stems $s_{i}$ for readability.

The set of $W$ so defined yields the quotient lists for the suffixes $a, b, c$ and $d$ as shown in Table 19

Now $V I(\{a, b, c\})=1.00$ since $a, b, c$ get $[0.66,0.90,0.90]$ respectively in the summed list $V_{P}$, which is more than any other suffix. Further, the $\operatorname{VI}(\{x, y\})$ scores for each pair $(x, y)$ in set $\{a, b, c\}$ are:
$V I(\{a, b\})=0.14$
$V I(\{a, c\})=0.14$

| $H_{a}$ |  | $H_{b}$ |  | $H_{c}$ |  | $H_{d}$ |  |
| :--- | :--- | :--- | :--- | :--- | ---: | :--- | :--- |
| $a$ | 1.00 | $b$ | 1.00 | $c$ | 1.00 | $d$ | 1.00 |
| $x$ | 0.60 | $c$ | 0.50 | $b$ | 0.50 | $b$ | 1.00 |
| $b$ | 0.40 | $y$ | 0.50 | $z$ | 0.50 | $c$ | 1.00 |
| $c$ | 0.40 | $a$ | 0.33 | $a$ | 0.33 | $\ldots$ | 0.00 |
| $\ldots$ | 0.00 | $\ldots$ | 0.00 | $\ldots$ | 0.00 |  |  |

Table 19. Given $W$ as in Table 18, quotient lists for $a, b, c$ and $d$.
$V I(\{b, c\})=0.14$
On the other hand, $\operatorname{VI}(\{b, c, d\})=0.5$ since the places for $b, c, d$ are $[0,1,5]$ and the optimal sum is $3(=[0,1,2])$. But the $V I(\{x, y\})$-scores for each pair $(x, y)$ in set $\{b, c, d\}$ are higher than in the previous case:
$V I(\{b, c\})=0.14$
$V I(\{b, d\})=0.20$
$V I(\{c, d\})=0.20$
This shows that the pair $V I$-scores for $\{b, c, d\}$ are higher than for $\{a, b, c\}$, yet $V I(\{a, b, c\})>V I(\{b, c, d\})$.

### 4.5 Conclusion

For three reasons, finding morphological paradigms from raw text data is an exceedingly difficult problem. First, paradigms - being sets of affixes - are exponentially many in the number of affixes. Second, almost all stems occur in one or only a few of the forms of their paradigm, making the evidence slight. Third, since raw text data does not mark the segmentation boundary between the true stem and its affix, all possibilities must be consídered the same, introducing noise in the stem-affix co-occurrence analysis. We present a metric that takes a paradigm and gives a score of "how good" the paradigm is, i.e., how much the members tend to occur on the same stem and how much non-members do not occur on those stems. The metric has the novelty that it is not the aggregation of a pair-wise defined metric. Using the metric there is a natural greedy search algorithm that finds locally optimal paradigms, which also takes advantages of the domain specific actuality that paradigms tend to be small. It is also wellbehaved with respect to event that one affix may belong to several different paradigms. Impressionistically, the metric produces sensible results, at least on languages without combinatorial paradigms, but there remain many issues to discuss. It also remains to work out how to make use of the metric to extract a fix list of paradigms and thereafter to evaluate.

## 5 Application 1: A Fine-Grained Model for Language Identification


#### Abstract

Existing state-of-the-art techniques to identify the language of a written text most often use a 3-gram frequency table as basis for 'fingerprinting' a language. While this approach performs very well in practice ( $99 \%$-ish accuracy) if the text to be classified is of size, say, 100 characters or more, it cannot be used reliably to classify even shorter input, nor can it detect if the input is a concatenation of text from several languages. The present paper describes a more fine-grained model which aims at reliable classification of input as short as one word. It is heavier than the classic classifiers in that it stores a large frequency dictionary as well as an affix table, but with significant gains in elegance since the classifier is entirely unsupervised. Classifying a short input query in multilingual information retrieval is the target application for which the method was developed, but also tools such as spell-checkers will benefit from recognising occasional interspersed foreign words. It is also acknowledged that a lot of practical applications do not need this fine level of granularity, and thus remain largely unbenefited by the new model. Not having access to real-world multi-lingual query data, we evaluate rigorously, using a 32-language parallel bible corpus, that accuracy is competitive on short input as well as multi-lingual input, and not only for a set of European languages with similar morphological typology.


### 5.1 Introduction

The language identification problem is to decide for a natural language text which language it is written in. The usual setting is to assume that one has access to training corpora beforehand for the languages to be considered. Some language fingerprint model is built from the training corpora and then classification of unseen text (belonging to one of the languages at hand) is performed through this model.

Existing state-of-the-art techniques rely on a surprisingly simple model, namely, a frequency table of character 3-grams for each language, read off directly from the training corpora. The corresponding 3 -gram frequency table for the text to be classified is then compared to each stored language by some rank-frequency metric. In practice, this approach performs very well (99\%-ish accuracy) if the text to be classified is of size, say, 100 characters or more (Juola 2006). Thus the language identification problem is a solved problem for most practical applications.

However, the crude 3-character gram method has a certain drawback (which may or may not be practical problem), in that it is not monotone. That is, if two texts $s_{1}, s_{2}$ are classified as $l_{1}, l_{2}$ respectively, then it is not certain that the concatenation of $s_{1}$ and $s_{2}$ is classified as either $l_{1}$ or $l_{2}$.

We will present an alternative model which aims at reliable classification of new text as short as one word. This model combines a frequency dictionary from
each training corpus and a component that tries to recognize completely unseen words by looking at affixes (which would, e.g., identify a word like jihading 'fighting the jihad' correctly as English). This latter component is crucial, not only for languages which make more use of affixes than English, but because there will always pop up completely novel words for any natural language no matter what size the training data. The affix detection technique implemented also builds from the same training corpora and requires no extra supervision or work by a human.

There are certainly practical applications which do require reliable classification of small segments and autodetection of language switches. These include spell checkers that wish to disregard interspersed foreign words, text-to-speech systems that make intermediate use of grapheme-to-phoneme conversion likewise wish to indentify interspersed foreign words, and multilingual information retrieval systems would benefit from knowing the language(s) of the words of a short query. For a lot of other practical applications, the granularity of the proposed new model is superfluous. For these applications, the only advantage of the proposed model is elegance and absolute lack of training supervision.

The resultant language identifier is evaluated using bible corpora for 32 languages, spanning the full range of morphological typology of languages of the world (Dryer 2005). Both its ability to classify short segments into one language and to autodetect short segments that may be composed of several languages, are evaluated. However, we do not compare these figures to existing systems, because they were not designed for classifying short segments accurately (and thus perform very poorly) $\sqrt[4]{4}$. On longer segments, i.e., 100 characters, performance is near perfect, and it is presumed that the state-of-the-art systems would also perform near perfect if tested on the same set.

With the improved accuracy on short segments and wide typological testing range, we hope to have met the challenges for written language identification set out in a recent survey article by Hughes et al. (2006).

All the training corpora used in this paper are bible corpora, since they are the only sufficiently large corpora available for a reasonably varied set of languages.

### 5.2 Previous Work

Our full bibliography of works dealing narrowly with written language identification spans over 100 articles, a handful of technical reports and one PhD thesis (Ziegler 1991) - it is therefore not possible to review them all here. Many pointers to older work and language identification of speech signals are given in Muthusamy and Spitz (1997) and Caseiro (1999). Sibun and Reynar (1996) is an excellent review and comparison of techniques used in early work.

[^4]For the language identification problem in the setting as in this paper, namely, written language identification trained on reference language data, two different feature models have been prevalent. One that looks at common words and one based on character $n$-grams (Grefenstette 1995, Cavnar and Trenkle 1994, Damashek 1995, Dunning 1994) and see Martin et al. (2006), Kruengkrai et al. (2005) for refinements of the $n$. The classification can then be done by comparing input text features to reference language features using rank-order statistics. More recent work in this direction has aimed at trimming overweight feature models Poutsma 2002, Takci and Sogukpinar 2004) or at combining $n$-gram and whole word features (Prager 2000). See, however Biemann and Teresniak (2005) for a novel, completely different approach based on words clustered on sentence-co-occurrence. (The accuracy of this identifier is comparable to the older approaches, but it is not, as claimed therein, unsupervised, because there is a very large number of manually set parametres/thresholds and word-frequency statistics are gathered from curated corpora.) There is also more recent work targeting web pages specifically (Xafopoulos et al. 2004, Martins and Silva 2005, Lins and Gonçalves 2004), that address the proper treatment of HTML tags.

Whereas the language identification problem has variously been labelled 'easy' and 'solved' (McNamee 2005), it depends on whether one sets the goal higher than distinguishing non-minimal noise-free samples of European languages. Some recent articles (Murthy and Kumar 2006, da Silva and Lopes 2006b, a) identify practical problems where this is not so. For instance, as far as we can ascertain, the best systems in van Noord's Online Summary 5 minimally require some 20 characters of text to make a judgment at all. Nor are they capable of realizing that a sample text is a concatenation of two languages. For example, The Xerox MLTT Language Identifier ${ }^{6}$ classifies the sentence 'good fish prefer their snake' correctly as English, the sentence 'fina fiskar sprattlar inte ofta' correctly as Swedish, but the concatenation of the two is classified as Norwegian (even though there is actually no legal Norwegian word in either sentence).

As indicated already, the present method seeks to tackle also smaller sample texts, which is crucial in order to be able to track whether a text is a composition of words from several languages. While the classic n-gram approaches have found that a good $n=3$, i.e., that salient morphemes can be approximated as being exactly 3 characters, a more elegant alternative is to hold this variable, so that salient affixes can have any length in any language. Furthermore, we wish to extend the testing scope, as present published testing has been only on a rather small set of European languages.

[^5]
### 5.3 Definitions and Preliminaries

Start with a finite non-empty alphabet $\Sigma$. The following terminology and notation will be used.
word: a non-empty finite string over $\Sigma$. Thus the set of all possible words can be denoted $\Sigma^{+}$. Lowercase $w$ with subscripts will be used for variables over words. A word will be enclosed in quotes if confusion could arise otherwise.
sentence: a finite non-empty tuple of words $\left\langle w_{1}, w_{2}, \ldots, w_{n}\right\rangle$. Commas and brackets will be omitted when no confusion can arise. However, variables that range over tuples, e.g. $\langle l\rangle$, will always be written with brackets.
$S_{\Sigma}$ : let $S_{\Sigma}=\left\{\left\langle w_{1} w_{2} \ldots w_{n}\right\rangle \mid w_{i} \in \Sigma^{+}, n \in \mathbf{N}\right\}$ denote the set of all possible sentences.
language: a probability distribution over sentences $L: S_{\Sigma} \rightarrow[0,1]$, i.e., such that $\sum_{\langle s\rangle} L(s)=1$.
training corpus: a finite sequence of sentences. However, we will never make use of the order of sentences, or order or words in the sentences, so a training corpus may be equated with its bag of words. Thus, if $T$ is a training corpus, let $f_{T}(w)$ denote the frequency of the word $w$ in $T$. Also, use $W_{T}=\left\{w \mid f_{T}(w) \geq 1\right\}$ for the set of words in the training corpus.
names and variables: Unless we are talking about existing natural languages, e.g., English, natural numbers $1,2, \ldots$ will be used for language names. $\Sigma_{1}, \Sigma_{2}, \ldots$ will be used for their corresponding alphabets, with $\Sigma=\bigcup_{i} \Sigma_{i}$ for the mother alphabet. $L_{1}, L_{2}, \ldots$ will be used for languages, i.e., probability distributions, and coindexed $T_{1}, T_{2}, \ldots$ for training corpora (where $T_{i}$ is assumed to be sampled from $L_{i}$ ).

The idea is of course that sentences which are illegal or ill-formed in some natural language will have zero probability and legal sentences will have a nonzero probability corresponding to their relative frequency. A natural way to see how a natural language should correspond to such a formal probabilistic language is to consider ever increasing amounts of natural language text and let the probability of each sentence be its limiting relative frequency. This correspondence requires that this limit actually exists for all sentences. If there are natural languages that do not live up to this, or which cannot be modelled so with an acceptable level of discrepancy, they should not be thought of as languages in our terminology.

Our notion of language is a generalization of the more common formalization of natural language as a set of sentences. We actually need this greater flexibility in order for language identifiers to exploit the fact that some words (and thus some sentences) which are legal in several natural languages may be distinguished by their different levels of frequency. It also provides a framework for gracious treatment of new words and proper names which are so ubiquitous
in open domain natural language text (such as newspaper text) that they should not be "abstracted away". With the probability model we have the power to say that any word is possible in any language, for example as a proper name, but it is more probable that an instance of, e.g., 'the' is from English than in some other language where it may have occurred as a proper name.

### 5.4 A Fine-Grained Model of Language Identification

From the input of a training corpus, the proposed model characterizes a language using the following two components:

Frequency dictionary: Stores each seen word and its (relative) frequency. The frequency of seen words is a very powerful predictor of a language.

Unsupervised affix detection: Salient affixes are extracted (in an unsupervised manner), which form the basis for a probabilistic guessing of previously unseen words.

These two components are combined into a word emission probability distribution that aims to predict how likely a language is to have emitted a given word. In principle, a collection of such probability distributions are sufficient to make up a standard case of language identifier that always outputs exactly one language. However, we shall also use another component, a language holdback bias, to enable intuitively correct identification of text that is concatenated from several languages.

## Word Emission Probability

A frequency dictionary $F D_{l}$ is built simply as:

$$
F D_{l}(w)=\frac{f_{T_{l}}(w)}{\sum_{w^{\prime} \in \Sigma} f_{T_{l}}\left(w^{\prime}\right)}
$$

Following Hammarström (2006a) - recounted in Section 3-we use an unsupervised algorithm to gather information on the salient affixes for a given language. The algorithm uses $W_{l}$ as its input and outputs a probability distribution on character strings that aims to say whether a given segment is likely to be a characteristic prefix or suffix for the language at hand. To be more precise, the probability distribution aims to capture the notion of morpheme probability that one arrives at if: 1. A linguist does a morphemic segmentation of the word types (not words tokens) occurring in a corpus, 2 . The frequencies of the individual morphemes, in prefix or suffix position, are interpreted as probabilities. For example, -qvj would likely get zero probability in an English corpus. An example output, adapted from Hammarström (2006a), is given in Table 20, sorted on highest probability. The outcome of the algorithm for languages which do not have any morphology at all is a fairly even spread of probability mass over initial and final characters of the words of the language in question. For reasons

| Swedish |  | English |  | Swahili |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| för- | 0.097 | -ed | 0.132 | - $a$ | 0.100 |
| -en | 0.086 | -eth | 0.109 | wa- | 0.095 |
| -na | 0.036 | -iah | 0.099 | ali- | 0.065 |
| -ade | 0.035 | -ly | 0.090 | nita- | 0.059 |
| - $a$ | 0.034 | -ings | 0.068 | aka- | 0.049 |
| -ar | 0.033 | -ing | 0.062 | $n i$ - | 0.046 |
| -er | 0.033 | -ity | 0.059 | ku- | 0.044 |
| -as | 0.032 | -edst | 0.058 | ata- | 0.042 |
| -s | 0.031 | -ites | 0.046 | ha- | 0.032 |
| -de | 0.031 | -s' | 0.036 | $a$ - | 0.031 |
|  |  | $\ldots$ |  | $\ldots$ |  |

Table 20. Comparative figures for prefix vs. suffix detection for three sample languages.
of space, the reader is referred to the said paper for a discussion of the inner workings and alternative algorithms.

As mentioned, the output from the affix extraction is a probability distribution over affixes. What we need is a probability distribution over words, in which any word ending in some salient suffix should have nonzero probability. One quite reasonable way to achieve this is to assign geometrically decreasing probabilities for longer and longer words. Thinking in this way, we let all observed (in $W_{l}$ ) word lengths get the probability mass proportional to the number of observed words with such lengths, and unseen word lengths get geometrically decreasing probability. Thus, to get a well-defined probability distribution over words based on the affix probability distribution, we multiply together the wordlength mass for $w$ with the highest (not necessarily longest!) matching, if any, affix probability, for a given word $w$. The details aren't interesting, but use $A_{l}(w)$ to denote the just described affix-based probability distribution.

Putting the affix detection together with the frequency dictionary to make an emission probability involves a related kind of estimatate. How much probability mass should be assigned to seen vs. unseen words? There are probably many similar alternatives, but here we have simply guessed that unseen words are like hapax words, and assigned the probability mass proportions to be like the proportion of hapax words: $\alpha_{l}=\frac{\left|\left\{w \in W_{l} \mid f_{T_{l}}(w)=1\right\}\right|}{\left|W_{l}\right|}$.

We are now ready to define emission probability:

$$
P_{l}(w)= \begin{cases}\left(1-\alpha_{l}\right) \cdot F D_{l}(w) & \text { if } w \in W_{l} \\ \alpha_{l} \cdot A_{l}(w) & \text { if } w \notin W_{l}\end{cases}
$$

It can happen that there is more mass given to an unseen word than to a (rare) seen word, even within one particular language. In fact, proportions vary quite wildly between languages, as can be seen in Table 21 with figures computed on the translations of the same bible text.

| Language | $\|T\|$ | $\|W\|$ | $\alpha$ | $\operatorname{argmax}_{w}(F D(w))$ |  |
| :--- | ---: | ---: | ---: | :--- | :--- |
| Greenlandic | 382188 | 107918 | 0.706 | taava (then) | 0.00857 |
| Swedish | 758773 | 26825 | 0.407 | och (and) | 0.05566 |
| Haitian creole | 904915 | 7796 | 0.335 | yo (PL/they) | 0.05531 |

Table 21. Some indications as to the widely differing identification cues for three languages; the polysynthetic Greenlandic versus the almost isolating Haitian creole.

## Language Holdback Bias

If we have $L_{1}, \ldots, L_{n}$ languages, the previous subsection shows how to construct the corresponding $P_{1}, \ldots, P_{n}$ probability distributions over words. Next, we shall define a family of probability measures over sequences of words. There will be one probability distribution for each language tuple of the same length as the sequence to be measured:

$$
P_{l_{1} l_{2} \ldots l_{m}}\left(w_{1} w_{2} \ldots w_{m}\right)=\prod_{i} P_{l_{i}}\left(w_{i}\right)
$$

Given a sequence of words we could then naively decide which language(s) it most probably belonged to by listing each tuple of the appropriate length and computing which tuple has the highest probability of having generated the sequence of words. However, for several reasons, such an approach is not advisable. First, with $n$ languages there are $n^{m}$ language tuples so it would not be tractable to enumerate them all. Second, the probability measures so defined, the output will be the concatenation of the most probable language for each word individually. This is probably not what we want since many words that are legal in several languages differ in frequency. Consider a sequence of a million words indisputably belonging to language $L_{1}$, and, interspersed inside, a word that is legal in both $L_{1}$ and $L_{2}$ but slightly more common in $L_{2}$. The naive language identifier would yield $L_{2}$ disregarding the suggestive surrounding million words of $L_{1}$. While it is technically not impossible that it is a concatenation of the two languages, a human would never see it as that. Third, it is not clear how to see if an input sequence is non-trivially legal in more than one way (i.e., there are several satisfactory language tuples). Either we insert some kind of threshold which would be hard to know how to set, or we have to say that pretty much all tuples are satisfactory identification of the sequence only with some degree variation.

For the first problem, it is easy to see that not all tuples need to be enumerated to get the maximally probable one (if we want only this one, rather than the probabilities for all). As defined, the emission probabilities depend only on a particular word, not anything else in the sequence, so maximas can be computed locally in the sequence and glued together as in any standard application of dynamic programming. For the second and third problem, we shall propose a refinement of the strategy that obviates the need for any thresholds.

We propose that a machine language identifier like ours should have a bias towards minimizing the number of times we change languages in an identification sequence. To be more precise, the prior probability that a sequence should switch language $c$ times should decrease exponentially in $c$. Also, other things being equal, the longer the sequence the stronger the bias should be, i.e., it should be less likely that a million word sequence should switch language once somewhere within it, than that a two-word sequence should switch language (once) within it. This is the way to say that having seen a million words of language $L_{1}$ counts for more than having seen just one word of $L_{1}$. We do not see any basis for this to be a sequential property, e.g., that language switches are significantly more (or less) likely after or before certain words, wherefore a (H)MM-modeling technique offers no advantage.

Formally, let $C\left(l_{1} l_{2} \ldots l_{m}\right)=\left|\left\{i \mid l_{i} \neq l_{i+1}\right\}\right|$ denote the number of times a change in language occurs in a language sequence. Clearly, we have $0 \leq c \leq m-$ 1. Let $\langle l\rangle=l_{1} l_{2} \ldots l_{m}$ be an arbitrary language tuple under consideration and $c=C(\langle l\rangle)$ its number of switches. Now, for any language identifier parametrized on $c$ and $m$, we wish the bias, regardless of the particular languages at hand, to ensure that:

$$
\begin{aligned}
& \frac{P(c, m)}{P(c+k, m)} \geq 2^{k} \quad \text { for all } k \geq 0, m \\
& P(c, m)>P(c, m+k) \quad \text { for all } k \geq 1, c
\end{aligned}
$$

A simple fulfilment of these is the following Language Holdback Bias function $B(c, m)$ :

$$
B(c, m)=\frac{1}{m^{c}} \cdot \frac{1}{\sum_{0 \leq i \leq m-1} \frac{1}{m^{i}}}
$$

There of course alternative bias functions that also fulfill the desiderata, but this is the simplest one. Now, with the bias function defined we are ready to present our full definition of the output of the now rather sophisticated language identifier.

$$
I D\left(w_{1} \ldots w_{m}\right)=\begin{aligned}
& \text { the set of all tuples }\langle l\rangle=l_{1} \ldots l_{m} \\
& \text { such that for all }\left\langle l^{\prime}\right\rangle \\
& B(C(\langle l\rangle), m) \cdot P_{\langle l\rangle}\left(w_{1} \ldots w_{m}\right) \geq \\
& B\left(C\left(\left\langle l^{\prime}\right\rangle\right), m\right) \cdot P_{\left\langle l^{\prime}\right\rangle}\left(w_{1} \ldots w_{m}\right)
\end{aligned}
$$

The formula conveys the following: look for tuples with as few cuts (i.e., minimal $c$ ) as possible, that are such that they have higher probability, the bias respected, than any other tuple with more cuts. This is the key feature which eliminates the need for a threshold. Thus, for example, a word sequence will be said to be of language $L_{l}$ iff it has higher probability than any division of the sequence into two parts of different languages (or three parts etc). There may be several such languages, but hardly all, so the yield will be a strong prediction.

The following more procedural reformulation of the identification function may be easier to understand. It should also make it clear that language identification is still polynomial in the sequence length, since there are still no dependencies between the word-probabilities.

1. Find minimal $c$ such that there exists a tuple $\langle l\rangle$ with $C(\langle l\rangle)=c$ and:

$$
\begin{aligned}
& B(c, m) \cdot P_{\langle l\rangle}\left(w_{1} \ldots w_{m}\right) \geq \\
& B\left(C\left(\left\langle l^{\prime}\right\rangle\right), m\right) \cdot P_{\left\langle l^{\prime}\right\rangle}\left(w_{1} \ldots w_{m}\right) \\
& \text { for all }\left\langle l^{\prime}\right\rangle \text { with } C(\langle l\rangle)>c
\end{aligned}
$$

2. Output all tuples $\langle l\rangle$ with $C(\langle l\rangle)=c$ and:

$$
\begin{aligned}
& B(c, m) \cdot P_{\langle l\rangle}\left(w_{1} \ldots w_{m}\right) \geq \\
& B\left(C\left(\left\langle l^{\prime}\right\rangle\right), m\right) \cdot P_{\left\langle l^{\prime}\right\rangle}\left(w_{1} \ldots w_{m}\right) \\
& \text { for all }\left\langle l^{\prime}\right\rangle \text { with } C(\langle l\rangle)>c
\end{aligned}
$$

### 5.5 Examples

## Example 1: The kings hon walikusoma

Consider the sequence the kings hon walikusoma which consists of the, which is of course the English definite article; kings is the well-known English lexical item which does occur in the training corpus - it also happens to end in $-s$ which is a very common Swedish inflectional ending (but there is no lexical item 'king' or 'kings' in Swedish); hon is a Swedish personal pronoun, abundantly occurring in the Swedish training corpus; and walikusoma is a well formed Swahili word whose individual morphemes all individually occur abundantly in the Swahili training corpus - but the semantically odd well-formed word 'walikusoma' does not occur in the training corpus (it would mean 'they read you').

The individual word-probabilities as well as a selection of the more interesting tuple-probabilities for the sequence as a whole, are shown in Table 22, As can be seen, the $P_{\text {eng,eng,swe,swa }}$ value beats all tuples with zero or one switches. It also happens to beat all tuples with three switches and it is the only such tuple. Therefore, in this case, the output will be exactly English, English, Swedish, Swahili.

## Example 2: The kings are there

The complicated interaction seen in the previous example does not disturb the "normal" easy class of classifications. Table 23 shows the word-probabilities for the almost trivial sentence the kings are there. There is a certain zero-switch tuple which is way ahead of the others. As it also beats all one-switch tuples (and no other zero-switch tuple does), it will be the output of the identifier.

## Example 3: De la

There are instances where there are several "winning" tuples, though informal tests show that this is not achieved very often. The sequence de la is very

|  | 'the' | 'kings' | 'hon' | 'walikusoma' |
| :--- | ---: | ---: | ---: | ---: |
| English | 0.051522 | 0.000286 | 0.000003 | 0.000004 |
| Swedish | 0.000002 | 0.000040 | 0.000916 | 0.000043 |
| Swahili | 0.000218 | 0.000000 | 0.000000 | 0.000317 |

All one-language tuples

| $P_{\text {eng }, \text { eng }, \text { eng }, \text { eng }}$ | $1.350 \mathrm{e}-016$ |
| :--- | :--- |
| $P_{\text {swe }, \text { swe }, \text { swe }, \text { swe }}$ | $2.468 \mathrm{e}-018$ |
| $P_{\text {swa }, \text { swa }, \text { swa,swa }}$ | $1.878 \mathrm{e}-025$ |

Some top one-switch tuples
$P_{\text {eng,swe,swe,swe }} \quad 2.034 \mathrm{e}-014$
$P_{\text {eng,eng,swe,swe }} \quad 1.465 \mathrm{e}-013$
$P_{\text {eng,eng,eng,swa }} \quad 3.008 \mathrm{e}-015$
The top two-switch tuple
$P_{\text {eng,eng,swe,swa }} \quad 2.701 \mathrm{e}-013$
Table 22. Example 1: $P_{l}(w)$ for a set of languages and some interesting words, followed by a selection of the more interesting tuple-probabilities.

|  | 'the' | 'kings' | 'are' | 'there' |
| :--- | ---: | ---: | ---: | ---: |
| English | 0.051522 | 0.000286 | 0.002812 | 0.002065 |
| Swedish | 0.000002 | 0.000040 | 0.000006 | 0.000035 |
| Swahili | 0.000218 | 0.000000 | 0.000004 | 0.000006 |
| $P_{\text {eng,eng,eng,eng }}$ | $8.5467629403443202 \mathrm{e}-011$ |  |  |  |
| $P_{\text {swe,swe,swe,swe }}$ | $1.2961894211016589 \mathrm{e}-020$ |  |  |  |
| $P_{\text {swa,swa,swa,swa }}$ | $2.5363460513704776 \mathrm{e}-023$ |  |  |  |
| ... |  |  |  |  |

Table 23. Example 2: $P_{l}(w)$ for a set of languages and some words that are very easy to classify, followed by examples to indicate that the dominance of a certain zero-switch tuple over some others.

|  | 'de' | 'la' |  |  |
| :--- | ---: | ---: | :--- | ---: |
| French | 0.029172 | 0.016325 | $P_{\text {fre,fre }}$ | 0.0003174886 |
| English | 0.000000 | 0.000000 | $P_{\text {spa } \text { spa }}$ | 0.0003227756 |
| Swedish | 0.008400 | 0.000001 | $P_{\text {spa,fre }}$ | 0.0001844997 |
| Swahili | 0.000000 | 0.001517 | $\ldots$ | $\ldots$ |
| Spanish | 0.033905 | 0.014280 |  |  |

Table 24. Example 3: $P_{l}(w)$ for a set of languages and two words, followed by a selection of the more interesting tuple-probabilities.
common to both Spanish and French. In English it is not common at all. In Swedish de is a personal pronoun so it enjoys a certain frequency, whereas $l a$ is not a word in (bible) Swedish. Similarly, $l a$ is a negator in Swahili and is therefore fairly frequent. Table 24 shows the relevant probabilities. The output will be only the tuples spa, spa and fre, fre, because tuples such as swe, swa and spa, fre lose out because of the bias, favouring few switches.

### 5.6 Evaluation and Discussion

Three extensive tests were performed using a parallel corpus of the bible in 32 languages, which contains languages from the isolating Maori to the record holding polysynthetic Greenlandic (Dryer 2005). In order to get a sufficiently cross-language comparable evaluation, size and randomness were equalized between languages the following way. A random verse from each chapter was selected (there are 1209 chapters in the bible). This was done once for the whole language set. Of course, these verses were removed from the training data. A random word from each selected verse was selected. This word-selection was done separately for each language. For each language, we thus get a set of randomly selected words $E_{l}$. Though 1209 word-selections were made for each language, many selections happened to select the same word. Thus the size of the $E_{l}$-sets varied from 350 (for Maori) to 974 (for Greenlandic). The descrepancy is not disturbing. Words are not entities of the same kind across languages, but our classifier operates on the granularity of words, and the desiderata is an evaluation of 'accuracy per (randomly selected) word'. An alternative, e.g., selecting 1000 unique words of each language would have made interpretation of the result difficult, because for Maori, it is likely that most of the 1000 words would have been seen words, occurring in other verses, whereas the opposite is the case for Greenlandic.

If $E$ is a set of tuples (possibly one-word tuples), drawn for language $l$, we define the accuracy $R_{E}(l)$ of a language identifier $I D$ :

$$
R_{E}(l)=\frac{\mid\{\langle x\rangle \mid I D(\langle x\rangle)=l \text { and }\langle x\rangle \in E\} \mid}{|E|}
$$

One-word classification: The $R_{E_{l}}$ was calculated for each of the 32 languages. Since the input sequence is of length 1 , there will never be any
cuts, so the language identifier was set to output the language with highest probability of having emitted the input word. The $E_{l}$-sets as defined above may contain words that are "impossible" predict where they were taken from, on the basis of the word alone. For example, let's say a word $w$ is legal in two languages but much more common in $l_{1}$ than $l_{2}$. If it happened to be drawn from $L_{l_{2}}$, it is hard to see how this can be predicted. However, we computed figures on the possible influence of this issue, and it turned out to be minor. Therefore, the results in Table 25 stand, but could be adjusted upwards by very small percentages.

Verse classification: To check how accurate the identifier was on longer segments, we chose to test on segments of roughly the length of a verse. Verses, in fact, happen to be around 100 characters long on average. From the 1209 verses selected (as above), those 100 verses thereof whose number of characters were closest to the average verse length of that language, were selected for testing. Denoting these 100 -verse sets by $V_{l}$, the verseclassification accuracy $R_{V_{l}}$ was calculated. This score, as well as data on average verse length, can be seen in Table 25.

4-tuple multilingual classification: A set of 1000 mixed language 4-tuples were built from $E_{1}, \ldots, E_{32}$ as follows.

1. Pick a random language $l$ and pick two random words from that $E_{l}$.
2. Precede it with a random word from a random language $E_{l^{\prime}}$.
3. Add a random word from a random language $E_{l^{\prime \prime}}$ at the end.

The results of this test was $193 \mathbf{( 1 9 . 3 \% )}$ fully correctly identified 4-tuples and $204(\mathbf{2 0 . 4 \%})$ with exactly one word misclassified.

Some figures are low, not surprisingly for languages with a lot of morphology, but overall we hold the results are very reasonable given the exceedingly difficult test problems of one-word and multi-language classification. It is very easy to make mistakes on single words when there are so many languages in the pool the accuracies are much higher if the number of competing languages is halved.

Unfortunately, we cannot contrast the verse-test with figures from competing state-of-the-art systems, as none of the systems known to us give enough details (on thresholds and such) to reconstruct a fair version of the classifier.

A matter requiring further commentary is the use of a bias function to do the job a scalar threshold value does in related work. (Human language identifiers, having the ability to assess syntactic and semantic coherence, need not use either.) Conceptually, the bias function employed is nothing other than a complex system of thresholds, in terms of growth behaviour (exponential, linear etc.) rather than scalar values. Arguably, this is an elegance improvement, although it comes with the cost of being harder to understand, compute and analyse. Also, in the experiments reported above, the bias function approach experimentally outperforms a simple systems of scalar threshold values. For example, through supervised training we have tried tuning one single threshold

| Language | 1-word | Verse | $\bar{V}$ |
| :--- | ---: | ---: | ---: |
| Haitian Creole | 0.839 | 1.00 | 101.79 |
| Zarma | 0.781 | 1.00 | 99.45 |
| Kekchi | 0.720 | 1.00 | 148.78 |
| English | 0.678 | 1.00 | 104.19 |
| Maori | 0.665 | 1.00 | 107.73 |
| Hindi | 0.607 | 1.00 | 119.50 |
| Hausa | 0.605 | 1.00 | 94.10 |
| Afrikaans | 0.594 | 1.00 | 103.34 |
| Danish | 0.580 | 1.00 | 89.30 |
| Cebuano | 0.573 | 1.00 | 129.48 |
| Icelandic | 0.550 | 1.00 | 95.58 |
| Swedish | 0.547 | 1.00 | 107.20 |
| Adamawa Fulfulde | 0.539 | 1.00 | 96.57 |
| German | 0.533 | 1.00 | 103.52 |
| Albanian | 0.523 | 1.00 | 114.80 |
| Spanish | 0.511 | 1.00 | 95.83 |
| French | 0.507 | 1.00 | 101.83 |
| Swahili | 0.494 | 1.00 | 105.03 |
| Slovene | 0.488 | 1.00 | 100.12 |
| Polish | 0.487 | 1.00 | 144.52 |
| Portuguese | 0.481 | 1.00 | 98.41 |
| Esperanto | 0.473 | 1.00 | 97.80 |
| Italian | 0.473 | 1.00 | 116.80 |
| Catalan | 0.450 | 1.00 | 109.70 |
| Dutch | 0.415 | 1.00 | 109.36 |
| Lithuanian | 0.396 | 1.00 | 104.99 |
| Hungarian | 0.386 | 1.00 | 102.10 |
| Latin | 0.366 | 0.99 | 112.54 |
| Turkish | 0.348 | 0.95 | 93.43 |
| Finnish | 0.345 | 0.99 | 107.88 |
| Malayalam | 0.276 | 0.88 | 128.65 |
| Greenlandic | 0.222 | 0.87 | 126.99 |
|  |  |  |  |

Table 25. Accuracies for the one-word and verse tests as well as average verse length in characters $(\bar{V})$.
value for all experiments, one threshold value individually for each language, different threshold values for different classification tasks (i.e., one for multilanguage classification and one for single language classification) and so on, resulting in generally lower accuracy on the same test set (obviously, there is little room for presenting and discussing figures from these tests here). Nevertheless, it remains possible that some other, yet undiscovered, system of scalar thresholds is superior to the bias function.

### 5.7 Conclusions

We have described a new model with considerable elegance for language identification on small, possibly mixed languages segments. We have also added significantly to the set of published evaluations of a language identification system with a balanced cross-language test. For larger input texts the new model has excellent accuracy, but it is bigger and slower in practice than the existing state-of-the-art systems.

# 6 Application 2: Poor Man's Stemming: Unsupervised Recognition of Same-stem Words 


#### Abstract

We present a new fully unsupervised human-intervention-free algorithm for stemming for an open class of languages. Since it does not rely on existing large annotated data collections or other linguistic resources than raw text it is especially attractive for low-density languages. The stemming problem is formulated as a decision whether two given words are variants of the same stem and requires that, if so, there is a concatenative relation between the two. The underlying theory makes no assumptions on whether the language uses a lot of morphology or little, whether it is prefixing or suffixing, or whether affixes are long or short. It does however make the assumption that 1 . salient affixes have to be frequent, 2. words essentially are variable length sequences of random characters, and furthermore 3 . that a heuristic on what constitutes a systematic affix alteration is valid. Tested on four typologically distant languages, the stemmer shows promising results in an evaluation against a human made gold standard.


### 6.1 Introduction

The problem at hand can be described as follows:
Input: An unlabeled corpus of an arbitrary natural language and two arbitrary words $w_{1}, w_{2}$ from that language

Output: A YES/NO answer as to whether $w_{1}$ and $w_{2}$ are morphological variants of one and the same stem (according to traditional linguistic analysis).

Restrictions: We consider only concatenative morphology and assume that the corpus comes already segmented on the word level.

The relevance of the problem is that of stemming as applied in Information Retrieval (IR). The issues of stemming in IR has been discussed at length elsewhere and need not be repeated here. It suffices to say that, though not uncontroversial, stemming continues to be a feature of modern IR systems for languages like English (e.g., Google ${ }^{7}$ ), and is likely to be of crucial importance for languages which make more use of morphology (cf. Pirkola 2001).

The reasons for attacking the problem in an unsupervised manner include advantages in elegance, economy of time and money (no annotated resources required), and the fact that the same technology may be used on new languages. The latter two reasons are especially important in the context of resource-scarce languages.

Our proposed unsupervised same-stem decision algorithm proceeds in two phases. In the first phase, a ranked list of salient affixes are extracted from an

[^6]unlabeled text corpus of a language. In the second phase, an input word pair is aligned to shortlist affixes that could potentially be added to a common stem to alternate between the two. Crucially, this shortlist of affix alternations is analyzed to check whether they form a systematic alternation in the language as a whole (i.e., not just in the pair at hand). This analysis depends strongly on the ranked affix list from the first phase.

### 6.2 Same-Stem Decision Desiderata and Heuristics

We use the technique described in Section 3 to extract a list of salient affixes for a given language from raw text data for that language. However, having a list of salient affixes is not sufficient to parse a given word into stem and affix(es). For example, sing happens to end in the most salient suffix yet it is not composed of $s$ and ing because crucially, there is no ${ }^{*} s,{ }^{*}$ sed etc. Thus to parse a given word we have to look at additional evidence beyond the word itself, such as the existence of other inflections of potentially the same stem as the given word, or further, look at inflections of other stems which potentially share an affix with the given word. We use the technique described in Section 4 to grow a paradigm for a given affix, given only raw text data as additional input.

The problem at hand, namely, to decide if two given words $w_{1}, w_{2}$ share a common stem (in the linguistic sense) is easier than parsing one word since we have evidence from two words and since we just have to answer yes/no and not also have to give the actual stem. Essentially, there are four interesting kinds of situations the same-stem-decider must face:

1. $w_{1}$ and $w_{2}$ do share the same stem and have a salient affix each, e.g., played vs. playing.
2. $w_{1}$ and $w_{2}$ do share the same stem but one of them has the "zero" affix, e.g., play vs. playing.
3. $w_{1}$ and $w_{2}$ do not share the same stem (linguistically) but do share some initial segment, e.g., playing vs. plough.
4. $w_{1}$ and $w_{2}$ do not share the same stem (linguistically) and do not share any initial segment, e.g., playing vs. song.

Number 4 is trivial to decide in the negative. Number 1 is also easy to affirm using a list of salient affixes, whereas the special case of number 2 requires some care. The real difficulty lies in predicting a negative answer for case number 3 (while, of course, at the same time predicting a positive for cases 1 and 2). We will go for an extended discussion of this matter below.

Consider two words $w_{1}=x s_{1}$ and $w_{2}=x s_{2}$ that share some non-empty initial segment $x$. Except for chance resemblances, which by definition are rare, we would like to say that $w_{1}$ and $w_{2}$ belong to the same stem iff:

1. $s_{1}$ and $s_{2}$ are well-segmented salient suffixes in the language, e.g., $-w$ and -lt for saw and salt are not; and
2. $s_{1}$ and $s_{2}$ must systematically contrast in the language, that is, there must be a large set of stems which can take both $s_{1}$ and $s_{2}$. For example, the word pair sting and station align to -ing and -ation which are both salient suffixes but they do not systematically contrast.

So far, corresponding to the desiderata 1 and 2 , we have the $Z_{W}$-score that ranks well-segmented salient suffixes and the $V I(P)$-score that ranks how well a set of suffixes contrast. We can put them together as:

$$
\begin{equation*}
A(P)=V I(P) \sum_{s \in P} Z_{W}(s) \tag{7}
\end{equation*}
$$

As a convention we set $Z_{W}\left({ }^{\prime \prime}\right)=0$.
The $A(P)$-score gives a score rather than a YES/NO-decision, which is the actual task. We could say that, at this point, the user has to supply a threshold value. However, instead, we devise another heuristic that obviates the need for a threshold at all. The resulting system thus supplies a YES/NO answer to the same-stem decising problem without any human interaction.

Recall the writing convention $w_{1}=x s_{1}$ and $w_{2}=x s_{2}$. Instead of having a threshold we may conjecture that:
$w_{1}, w_{2}$ have the same stem iff $s_{1} \in G^{*}\left(s_{2}\right)$ and $s_{2} \in G^{*}\left(s_{1}\right)$
For example, this predicts that sting and station are not the same stem because neither $G^{*}(i n g)=\left\{{ }^{\prime \prime}, e, e d, e r, e s, i n g, s\right\}$ contains 'ation' nor does $G^{*}($ ation $)=$ \{ate, ated, ating, ation, ations $\}$ contain 'ing'. From our experience this test is quite powerful. However, there are of course cases where it predicts wrongly, due to the greedy nature of the $G^{*}$-calculation, e.g., $G^{*}(i n g)$ does not contain 'ers'. Moreover, if one of the affixes is the empty affix, we need a special fix (see below).

### 6.3 Same-stem Decision Algorithm

We can now put all pieces together to define the full algorithm as shown in Table 26

If one of $s_{1}, s_{2}$ is the empty string then step 3 and 4 should be restated as follows (using $s$ to denote the non-empty one of the two). The maximization value in step 3 should be modified to: $\frac{Z_{W}(s)}{1+p l a c e\left({ }^{\prime \prime}, H_{s}\right)}$. Step 4 should be modified to: answer YES/NO acccordingly as ${ }^{\prime \prime} \in G^{*}(s)$.

The bad news is that the computation of the $G^{*}$ :s tends to be slow due to the summing and sorting of typically very long ( 50000 -ish items) lists. On my standard PC with a Python implementation it typically takes 30 seconds to decide whether two words share the same stem.

### 6.4 Evaluation

Several authors, e.g., Goldsmith et al. (2001) and Melucci and Orio (2003), have evaluated their stemming algorithms on Information Retrieval performance.

Input: A text corpus $C$ and two words $w_{1}, w_{2}$
Step 1. Calculate $Z_{W}$ as in Table 8
Step 2. Form the set of candidate alignment pairs as:

$$
C\left(w_{1}, w_{2}\right)=\left\{(s 1, s 2) \mid x s_{1}=w_{1} \text { and } x s_{2}=w_{2}\right\}
$$

Step 3. If $C\left(w_{1}, w_{2}\right)$ is empty then answer NO, otherwise pick the best candidate pair as:

$$
\operatorname{argmax}_{(s 1, s 2) \in C\left(w_{1}, w_{2}\right)} A\left(\left\{s_{1}, s_{2}\right\}\right)
$$

Step 4. For the winning pair, answer YES/NO acccordingly as $s_{1} \in G^{*}\left(s_{2}\right)$ and $s_{2} \in G^{*}\left(s_{1}\right)$

Table 26. Summary of same-stem decision algorithm. If one of $s_{1}, s_{2}$ is the empty string then steps 3 and 4 should be modified as follows (using $s$ to denote the non-empty one of the two). The maximization value in step 3 changes to: $\frac{Z_{W}(s)}{1+\text { place }\left({ }^{\prime \prime}, H_{s}\right)}$. Step 4 changes to: answer YES/NO acccordingly as ${ }^{\prime \prime} \in G^{*}(s)$.

While IR is the undoubtedly the major application area, we feel that evaluating on retrieval performance does not answer all relevant questions of stemming performance. For instance, a stemmer may make conflations and miss conflations that simply did not affect the test queries. In fact, one may get different best stemmers depending on the test collection. There is also difference as to whether the whole document collection, an abstract of each document or just the query is stemmed.

We find it more instructive to test stemming separately against a stemming gold standard and assess the relevance of stemming for IR by testing the stemming gold standard on IR performance. If stemming turns out to be relevant for IR, then researchers should continue to develop stemming algorithms towards the gold standard. In the other case, one wonders whether IR-improving term conflation methods should rightly be called stemmers.

In order to assess the cross-linguistic applicability of our stemming algorithm we have chosen languages spanning the spectrum of morphological typology from isolating to highly suffixing - Maori, English, Swedish and Kuku Yalanji (Dryer 2005). As training data we used only the set of words from a bible translation to emphasize the applicability to resource-scarce languages. Table 27) contains information on the bible versions used.

For the four languages we devised a stemming gold standard, consulting descriptive materials for Maori (Bauer et al. 1993, Williams 1971) and Kuku Yalanji (Patz 2002, Hershberger and Hershberger 1982), languages not generally known to the author. So as not to let the test set be dominated by too many simple test cases, the selection of test set cases was done as follows:

1. Select a random word $w_{1}$ from $W$ for the corresponding language

| Language | Language Type | Corpus | Scope |
| :--- | :--- | :--- | ---: |
| Maori | Isolating | British \& Foreign Bible Society 1996 | NT \& OT |
| English | Mildly Suffixing | King James 1977 | NT \& OT |
| Swedish | Suffixing | Svenska Bibelsällskapet 1917 | NT \& OT |
| Kuku Yalanji | Strongly Suffixing | Summer Institute of Linguistics 1985 | NT \& OT Parts |

Table 27. Summary of Bible corpora used in evaluation.

|  | same-stem |  | diff.-stem |  |
| :--- | ---: | ---: | ---: | ---: |
| Language | Correct | Total | Correct | Total |
| Maori | 10 | 13 | 100 | 100 |
| English | 97 | 100 | 100 | 100 |
| Swedish | 96 | 100 | 100 | 100 |
| Kuku Yalanji | 94 | 100 | 100 | 100 |

Table 28. Evaluation results of same-stem decisions given 100 test pairs for each language (see text).
2. Select a random number $i$ in $0 \leq i \leq\left|w_{1}\right|-1$
3. Select a random word $w_{2}$ from the subset of words from $W \backslash\left\{w_{1}\right\}$ sharing $i$ initial characters with $w_{1}$
4. Mark the pair $w_{1}, w_{2}$ to be of the same stem according to traditional linguistic analysis

This was repeated until 200 pairs of words for each language had been selected, 100 same-stem and 100 not same-stem. Except for Maori where we could only really find 13 same-stem cases this way, all involving active-passive alternating verbs (described in detail in Sanders 1990).

The evaluation results are shown in Table 28.
The errors fall into just one major type, in which the algorithm is too cautious to conflate; it is when two words do share the stem but where one of the suffixes is rather uncommon (including the case where it is actually composite) and therefore it is not in the grow-set of the other suffix; for example Swedish skap-ade-s (passive past) and skap-are-n-s (agent-noun definite genitive). We also expected false positives in the form of random resemblances involing short words and short affixes; e.g., as versus $a$ but no such cases seem to have occurred in the test set in any of the languages.

We have done attempted a comparison with other existing stemmers, mainly because they tend not be aimed at an open set of languages and those which are, are really not fully supervised and we fear we might not do justice to them in setting parametres (see the subsection below on related work). The widely known Porter stemmer (Porter 1980) for English scores exactly the same result for English as our stemmer, which suggests than an unsupervised approach may come very close to explicity human-informed stemmers. Many other stemmers, however, are superior to ours in the sense that they can stem a single word
correctly whereas ours requires a pair of words to make a decision. This is especially relevant when large bodies of data needs to be stem-indexed as it would take quadratic time (in the number of words) in our setting.

### 6.5 Related Work

A full survey of stemming algorithms for specific languages or languages like English has more or less fully been done elsewhere (the technology becoming relatively mature cf. Erjavec and Džeroski| 2004, Frakes and Fox 2003, Goldsmith et al. 2001, Melucci and Orio 2003, Rogati et al. 2003, Hull 1996, Galambos 2004, Flenner 1994 and references therein). We will focus instead on unsupervised approaches for a wider class of languages.

Melucci and Orio (2003) present a very elegant unsupervised stemming model. While training does not require any manually annotated data, some architectural choices depending on the language still has to be supplied by a human. If this can be overcome in an easy way, it would be very interesting to test their Baum-Welch training approach versus the explicit heuristics in this paper, especially on a wider scope of languages than given in their paper. The unsupervised stemmer outlined in Goldsmith et al. (2001) actually requires a lot of parametres to be tweaked humanly and mainly targets languages with one-slot morphology.

Other systems for unsupervised learning of morphology which do not explicitly do stemming could easily be transformed into stemmer (Jacquemin 1997, Yarowsky and Wicentowski 2000, Ćavar et al. 2004a, Brent et al. 1995, Déiean 1998a, Snover et al. 2002, Argamon et al. 2004, Goldsmith 2001, Gaussier 1999, Sharma et al. 2002, Oliver 2004). All of these systems, however, require some parameter tweaking as it is and perhaps one more if transformed to stemmers, so there is still work outstanding before they can be compared on equal grounds to the stemmer described here. Given that they use essentially the same kind of evidence, it is likely that some of them, especially Creutz and Lagus (2007), will reach just as competitive results on the same task.

### 6.6 Conclusion

We have presented a fully unsupervised human-intervention-free algorithm for stemming for an open class of languages showing very promising accuracy results. Since it does not rely on existing large data collections or other linguistic resources than raw text it is especially attractive for low-density languages. Although polynomial in time, it appears rather slow in practice and may not be suitable for stemming huge text collections. Future directions include investigating whether there is a speedier shortcut and better, more systematic, approach to layered morphology, i.e., languages which allow affixes to be stacked.

## Acknowledgements

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# 7 Application 3: Poor Man's Word-Segmentation: Unsupervised Morphological Analysis for Indonesian 


#### Abstract

We present a partially new fully unsupervised algorithm for morphological segmentation of a arbitrary natural language with only one-slot concatenative morphology. The behaviour of the algorithm is examined in detail for Indonesian as it is a good approximation of such a language. The underlying theory makes no assumptions on whether the language is prefixing or suffixing, or whether affixes are long or short. It does however make the assumption that 1 . salient affixes have to be frequent, 2 . words essentially are variable length sequences of random characters, and furthermore 3. that a heuristic on what constitutes a systematic affix alteration is valid. The only input required is raw unannotated text and there are no thresholds or parameters that need human tuning. Since there no reliance on existing large data collections or other linguistic resources than raw text, the approach is especially attractive for low-density languages. We will discuss the pressing question whether unsupervised approaches are advantageous over the alternative approach with human-built rules and lexica, especially as it pertains to languages like Indonesian, which do not have much morphology in the first place.


### 7.1 Introduction

Indonesian is a language with very little morphology, but nevertheless, there is some. Thus, the first step in the computational treatment of Indonesian is (a tool for) morphological parsing. A traditional approach, be it for Indonesian or another language, is to build a lexicon and morphological rules by hand. We may call this the manual approach. In the present paper, we explore another approach, namely to induce a morphological parser from raw (unannotated) text data and, in fact, without any human intervention at all. This will be called the unsupervised approach. We will discuss the advantages and disadvantages of both alternatives extensively, with Indonesian as the case at hand.

### 7.2 Problem Statement

The problem at hand can be described as follows:
Input: An unlabeled text corpus of a natural language where
(a) The corpus comes already segmented on the word level.
(b) The language only has one-slot concatenative morphology.

Output: The same text corpus annotated with morphological divisions

Any language with an orthography that shows word-divisions, e.g., with spaces, passes the (a)-restriction right away. So Indonesian, in its contemporary orthography is immediately applicable, while, e.g., Thai is not. The (b)-restriction mandates that the language in question only has concatenative morphology, and furthermore, that affixes cannot be stacked after another, i.e., that there is only maximally one 'slot' for suffixes and maximally one 'slot' for prefixes. In other words, agglutinative languages are not the target of the present problem. Indonesian passes this restriction, or nearly so, as verbal prefixes (like $d i$-) cannot be stacked, and the only inflectional suffixes are the personal endings (like -nya). On the other hand, multiple affixes do occur somewhat less commonly where the inner suffix is derivational, e.g., -an-mu or -kan-lah. Similarly, English would be a good one-slot language except for combinations of derivational and inflectional affixes, such as -ation-s and latinate prefix stacking such as dis-en-.

Considering languages which have concatenative morphology at all, Indonesian is as close to a one-slot language as one may hope to find (Dryer 2005). For this reason, Indonesian provides an excellent case for study of unsupervised versus manual approaches to morphological parsing. (The reason for having the one-slot restriction at all, is, that the unsupervised approaches can be considerably less complex.)

### 7.3 Manual versus Unsupervised Methods

In the manual approach to morphological parsing, typically, a human implements the following:
(a) A set of morphological rules for parsing and generation
(b) A lexicon of stems

There are many different frameworks for the implementation of rules and lexicon, e.g., XFST (Beesley and Karttunen 2003) or FM (Forsberg 2007) to name a few. However, the choice of framework has little bearing on the issues in this paper, wherefore we disregard this matter further.

The advantages of the manual approach is that one gets a transparent highaccuracy analyser that segments and labels morphologically complex words according to traditional linguistic analysis.

The disadvantages of the manual approach is the human labour required, both for writing the morphological rules and for building the lexicon. On the other hand, in some cases, a finished lexicon-resource is accessible or purchasable as a module, e.g., via the publisher of a dictionary, and then this major part of the human labour is covered already. Another option to reduce the human labour in lexicon-building is to "extract" a lexicon from raw-text. Given morphological paradigms and search constraints, an algorithm extracts a list of stems that are evidenced to belong to a given paradigm in the raw text. A human only needs to skim such a list of extracted lexical items to weed out false positives (see Forsberg et al. 2006, Lindén 2008, Adler et al. 2008, Carlos et al. 2009 and
references therein). Furthermore, any lexicon-based approach to morphological analysis will fail on out-of-lexicon words which inevitably occur in open-domain text (such as newspaper text). As we shall see, there is considerable overlap between out-of-lexicon guessing, lexicon extraction and unsupervised methods.

The unsupervised approach has the advantage that it eliminates the human labour and there is a certain elegance in that the same techniques can be used for different languages.

Naturally, the disadvantage of the unsupervised approaches is that they do not reach full accuracy of morphological analysis. Also, in addition to clear errors, one may expect a certain amount of morpheme segmentations which are slightly at odds with traditional linguistic analysis but not necessarily erroneous. Furthermore, the segmented morphemes are not labeled (or a separate less-than-perfect module is required to learn appropriate labels - see, e.g., Schone and Jurafsky (2001b)) and for many, but not all, applications such labels are in demand.

Various other factors, such as module size or analysis speed, no longer play significant roles, and thus do not contrast between the two alternative approaches. The key issue is how much behind in accuracy unsupervised approaches actually fare - a matter that has so far been rather unclear (see also Section (7.4). One of the main goals of the present paper is to clarify the situation.

A recent survey of published work on morphological analysis for so-called low-density languages shows that the vast majority are of the manual kind (Hammarström 2009b). While the contrast between manual and unsupervised approaches are mostly relevant for low-density languages, the division is not so simple. Perhaps as a result of the human labour required, most manually constructed morphological analysers are not freely available.

### 7.4 Previous Work on Unsupervised Morphological Analysis

A full but concise survey up to late 2007 can be found in Hammarström (2007b). Some relevant work have appeared since, notably Tepper and Xia (2008), Monson (2009), Johnson (2008). A wide variety of heuristics and models have been employed, which are not of particular importance for this paper, though the interested reader is advised to consult the surveys of (Roark and Sproat 2007, Goldsmith pear).

The relevant issue is the fact that nearly all approaches published so far exceptions include Golcher (2006) and Hammarström (2006b) - have a little supervision in the form of thresholds or parameters that have to been set and tuned by a human. This, along with the fact that many approaches target a different (related, but not identical) morphological segmentation problem makes most of this work not directly applicable to the problem considered in the present paper. For these reasons, we will focus on a particular line of work on unsupervised morphological segmentation, which is free from any kind of parameters or thresholds. The (very important) comparison between different unsupervised
or little supervised systems is better handled in the annual MorphoChallenge controlled competition 8 .

### 7.5 Poor Man's Word-Segmentation

In this section we will describe a fully unsupervised algorithm for word-segmentation as applied to Indonesian. The work is an extension of Hammarström (2006b) included in Section 6. The following is an outline of the steps and components in the model and its application.

Model: A model is compiled from raw text data
Affix Extraction: Extracts a list of affixes ranked according to salience, i.e., how likely they are to be 'real' suffixes in the language in question

Affix Alternation: Given an affix, finds the set of suffixes that systematically appears on the same stems as the given affix
Affix Purging: Given a ranked list of salient affixes (as in the extraction component above), weed out the 'unnecessary' ones, namely those which are covered by a more salient affix

Application: The model is applied to a seen or unseen word and analyses it
True/Random-Ending Heuristic: A word that ends in a salient affix that survived purging is either truly composed of a stem and this affix, or it just happens to end in (or begin with) a character sequence that is identical to a salient affix. The true/random-ending heuristic makes this decision, using affix alternation as a component.

All the above components rely on a number of heuristics which are tailored to the Indonesian language type. The heuristics will be discussed in their due place.

We will illustrate the methods on suffixes, but it is obvious that the same procedures can be used to target prefixes but looking at the word from the opposite direction.

As our input raw text corpus we have used the Indonesian bible (American Bible Society 2003), solely because of electronic availability, reproduceability and comparability with other languages. The Indonesian bible amounts to 657112 word tokens and 15251 word types (all words lowercased).

## Affix Extraction

We use the technique described in Section 3 to extract a list of salient affixes for a given language from raw text data for that language. For Indonesian we get the top 30 plus bottom 3 suffixes as shown in Table 29. The results of this first step do not immediately appear useful, but will be after some postprocessing.

[^7]| -anmu | 87195.4 | $-m u$ | 6350.9 |
| ---: | ---: | ---: | ---: |
| -nya | 73694.0 | -kannya | 5981.8 |
| -anku | 51923.8 | $-a n$ | 5931.3 |
| -lah | 39535.9 | -arlah | 5702.8 |
| -kanlah | 27933.2 | -atlah | 5148.6 |
| -hnya | 20915.8 | -anlah | 4522.9 |
| -inya | 19677.7 | -nglah | 4121.3 |
| -atnya | 18361.2 | -anglah | 3990.4 |
| -kan | 18318.4 | -akanlah | 3882.9 |
| -tnya | 14237.1 | -hlah | 3658.6 |
| -iel | 10000.7 | $-a h$ | 3596.1 |
| -snya | 9635.2 | $-n k u$ | 3359.6 |
| -rlah | 9351.8 | $-y a$ | 3203.6 |
| -annya | 7802.0 | $\ldots$. | 0.0 |
| -ilah | 7534.3 | -aadil | 0.0 |
| -anya | 7005.4 | -aadai | 0.0 |
| -nmu | 6531.7 | -aaan | 0.0 |

Table 29. Top 30 and bottom 3 extracted suffixes for an Indonesian bible corpus.

For example, when a shorter string has higher score than its extension, e.g., -nya versus -tnya, the longer one should obviously be discarded. It is also worth noting that in cases where Indonesian does show stacked affixes, we get somewhat confused outcomes; sometimes the composition is seen as one simplex segment as in -anmu and sometimes the last layer has a higher score than the compostion as in -lah versus -kanlah.

## Affix Alternation

We use the technique described in Section 4 to grow paradigms given only raw text data as input. To give the reader a feeling for the outcome for Indonesian specifically, Table 30 shows two examples of quotient functions (sorted on highest value) and Table 31 gives two examples of $V_{P}$-lists. The latter contrasts the very common paradigm $\left\{-n y a,-m u,-^{\prime \prime},-k u\right\}$ with the nonsense paradigm $\{n y a, s, a, y a\}$ consisting only of individually frequent suffixes. The ranks of the members of $P_{1}$ to the left are $[0,1,2,3]$, and for $P_{2}$ to the right the ranks are [24, 32, 50, 79]. Two growth-examples are shown in Table 32 one which attains a perfect 1.0 score and one in which the original member is not a well-segmented to begin with (the pattern such cases exhibits will be exploited for purging).

## Affix Purging

Now, if we return to the ranked list of suffixes in $Z_{W}$ as of Table 29. As mentioned, one purging heuristic is to discard longer affixes which have a tail whose score is higher. This may be achieved by keeping only those suffixes

| $y$ | $H_{n y a}(y)$ | $y$ | $H_{m u}(y)$ | y | $V_{P_{1}}(y)$ | y | $V_{P_{2}}(y)$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| nya | 1.000 | $m u$ | 1.000 | " | 2.789 | " | 1.025 |
| " | 0.913 | " | 0.943 | nya | 1.652 | $m u$ | 0.273 |
| mu | 0.261 | nya | 0.749 | mu | 1.004 | $k u$ | 0.166 |
| ku | 0.153 | ku | 0.393 | ku | 0.572 | snya | 0.098 |
| kan | 0.071 | kan | 0.063 | $l a h$ | 0.243 | $i$ | 0.092 |
| $l a h$ | 0.057 | $l a h$ | 0.059 | kan | 0.231 | kan | 0.089 |
| an | 0.043 | an | 0.056 | an | 0.197 | $l a h$ | 0.076 |
| $i$ | 0.039 | kanlah | 0.045 | $i$ | 0.157 | an | 0.069 |
| kanlah | 0.034 | $i$ | 0.040 | kanlah | 0.137 | $n$ | 0.064 |
| kah | 0.016 | kah | 0.022 | annya | 0.075 | anya | 0.058 |
| ilah | 0.015 | annya | 0.022 | ilah | 0.068 | slah | 0.057 |
| annya | 0.014 | ilah | 0.019 | kah | 0.065 | skan | 0.053 |
| kannya | 0.011 | anmu | 0.015 | $n$ | 0.049 | $k$ | 0.053 |
| $t$ | 0.008 | $n$ | 0.014 | anmu | 0.047 | $n g$ | 0.052 |
| $k$ | 0.008 | $m$ | 0.014 | $m$ | 0.043 | san | 0.048 |
| anmu | 0.008 | $k$ | 0.012 | $t$ | 0.037 | $t$ | 0.045 |
| $n$ | 0.007 | $n g$ | 0.011 | $k$ | 0.036 | kanlah | 0.044 |
| $m$ | 0.007 | mulah | 0.011 | anku | 0.033 | $m$ | 0.043 |
| $h$ | 0.007 | $t$ | 0.009 | $n g$ | 0.032 | si | 0.042 |
| $s$ | 0.005 | anku | 0.009 | $h$ | 0.031 | $r$ | 0.042 |
| $n g$ | 0.005 | wan | 0.008 | mulah | 0.031 | $h$ | 0.042 |
| $l$ | 0.005 | ya | 0.007 | ya | 0.031 | $l$ | 0.030 |
| inya | 0.004 | $t a$ | 0.007 | ta | 0.029 | $a m u$ | 0.030 |
| ya | 0.004 | $s$ | 0.007 | $s$ | 0.027 | nya | 0.027 |
| $\ldots$ | $\ldots$ | $\ldots$ | $\ldots$ | $\cdots$ | . $\cdot$ | ... | $\cdots$ |

Table 30. Sample quotient functions/lists for $n y a$ and $m u$.

Table 31. Example ranks for $P_{1}=$ $\left\{n y a, m u,^{\prime \prime}, k u\right\}$ and $P_{2}=\{n y a, s, a, y a\}$.

| $P$ | $V I(P)$ |  |
| :---: | :---: | :---: |
| ('nya',) | 0.000 |  |
| (", 'nya') | 0.333 |  |
| (", 'mu', 'nya') | 0.750 |  |
| (", 'ku', 'mu', 'nya') | 1.000 |  |
| $P$ |  | $V I(P)$ |
| ('s',) |  | 0.0 |
| ('s', 'snya') |  | 0.077 |
| ('s', 'smu', 'snya') |  | 0.273 |
| ('s', 'sku', 'smu', 'snya') |  | 0.667 |
| ('s', 'san', 'sku', 'smu', 'snya') |  | 0.833 |
| ('s', 'san', 'skan', 'sku', 'smu' | 'snya') | 0.882 |

Table 32. Example iterations of $G^{*}$ ('nya') and $G^{*}($ 's').

| $s$ | $-n y a$ | $-s$ |
| :--- | :---: | :---: |
| $G^{*}(s)$ | $\left\{^{\prime \prime}, k u, m u, n y a\right\}$ | $\{s$, san, skan, sku,smu,snya $\}$ |
| $\bar{s} P$ | $\left\{^{\prime \prime}, k u, m u, n y a\right\}$ | $\{s\}$ |
| $s P$ | $\}$ | $\{$ an, kan $, k u, m u, n y a\}$ |
| $\sum_{x \in \bar{s} P} Z_{W}(x)$ | 80790.7 | 405.5 |
| $\sum_{x \in s P} Z_{W}(x)$ | 0.0 | 105040.5 |

Table 33. The purging calculation for example suffixes -nya (remains) and $-s$ (purged out).
which are best parse for at least one word.

$$
U_{W}^{\prime}=\left\{s \mid s=\operatorname{argmax}_{s^{\prime} \triangleleft w} Z_{W}\left(s^{\prime}\right) \text { for some } w \in W\right\}
$$

This purging heuristic is not sufficient, as a certain amount spurious suffixes - albeit with low $Z_{W}$-score - remain, e.g., $-s$. At this point, one could introduce a threshold value to weed out the rest of the spurious suffixes. However, it turns out that there is another heuristic that does the same job, without human intervention.

The behaviour of the $G^{*}$ ('s')-set shown in Table 32 is typical for spurious suffixes. Indeed, if $s$ is a spurious suffix, $G(s)$ is likely to consist of $s$-prefixed to members of a 'true' paradigm. We may therefore posit the following criterion for true-suffixness of a suffix $s$. Split $G^{*}(s)$ into $s P=\left\{x\left|s x \in G^{*}(s),|x|>0\right\}\right.$, i.e., the members which consist of $s$ followed by some non-empty string versus the rest $\bar{s} P=\left\{x\left|x \in G^{*}(s), x \neq s y,|y|>0\right\}\right.$. Note that $s$ itself belongs to $\bar{s} P$ rather than $s P$ and that $s P$ contains the "tail"-strings, stripped of their initial $s$. If the sum of $Z_{W}$-values for $\bar{s} P$ is strictly larger than the the sum of $Z_{W}$-values for $s P$, then the $s$ is a true suffix, otherwise not. Table 33 shows two examples.

The final purged set of suffixes may accordingly be defined as:

$$
U_{W}^{\prime \prime}=\left\{s \in U_{W}^{\prime} \mid \sum_{x \in \bar{s} P} Z_{W}(x)>\sum_{x \in s P} Z_{W}(x)\right\}
$$

The $U_{W}^{\prime \prime}$ for Indonesian boils down to the follwing suffixes:
\{anmu, nya, anku, lah, kan, nmu, mu, nku, i, ezer, zabad, inadab,
ihud, nadab, arif, obab, ezib, ilene, laf, ilo, ore, e\}
The existence of some remaining spurious affixes, such as -ilene makes little difference, as these affixes are very infrequent and do not significantly diminish segmentation accuracy. A real error, however, is where Indonesian deviates from being a one-slot language. The lack of $-a n$, which is purged out because $-m u$ and $-k u$ are frequently attached to it.

## True/Random-Ending Heuristic

A word that ends in a salient affix that survived purging is either truly composed of a stem and this affix, or it just happens to end in (or begin with) a character
sequence that is identical to a salient affix. The true/random-ending heuristic makes this decision, using affix alternation as a component. Consider the word 'gadisnya' where the -nya is a true occurrence of the suffix -nya, and the word 'hanya' which just happens to end in the -nya character sequence. How can we (heuristically) distinguish the two cases when there is no stem lexicon to tell us that there is a stem gadis- but no stem ha-?

The intution is the following. If we count all the words in $W$ which begin with $h a-$, they are rather many ( 247 to be exact). It is not too surprising that one of them would just by chance continue as -nya, and, crucially, none of the other 246 continuations are -", $-m u$ or $-k u$, i.e., the $G^{*}(n y a)$ affixes which systematically alternate with -nya. On the other hand, if we look that the words in $W$ which begin with gadis-, there are only two more than 'gadisnya', namely 'gadis' and 'gadismu', i.e., with -" and -mu! To turn this into a formal criterion, given a word $w=x s$ such that $s \in U_{W}^{\prime \prime}$, let $C_{W}(x)=\{y \mid x y \in W\}$ be the set of "continuations" of $x$. Extend the notion of final frequency to a set of suffixes $P$ as $f_{W}(P)=\mid\{w \in W \mid w=y z$ for some $z \in P\} \mid$ and let $\alpha_{W}(P)=f_{W}(P) /|W|$. The heart of the matter is how much is inside $C_{W}(x) \cap G^{*}(s)$ versus how much is outside $C_{W}(x) \backslash G^{*}(s)$. Given $w=x s$, if $s$ is just a random continuation of an initial segment $x$, then many items in $C_{W}(x) \cap G^{*}(s)$ will be hard to explain, and if $s$ is truly a well-segmented then too many random continuations in $C_{W}(x) \backslash G^{*}(s)$ will overshadow this fact. In other words, the $w=x s$ should be segmented iff the following ratio $\geq 1$ :

$$
\frac{\left(1-\alpha_{W}\left(G^{*}(s)\right)\right)^{\left|C_{W}(x) \backslash G^{*}(s)\right|}}{\alpha_{W}\left(G^{*}(s)\right)^{\left|C_{W}(x) \cap G^{*}(s)\right|}}
$$

Or equivalently, iff the following subtraction $\geq 0$ :

$$
\begin{aligned}
& \left|C_{W}(x) \backslash G^{*}(s)\right| \cdot \log \left(1-\alpha_{W}\left(G^{*}(s)\right)\right)- \\
& \left(\left|C_{W}(x) \cap G^{*}(s)\right|\right) \cdot \log \alpha_{W}\left(G^{*}(s)\right)
\end{aligned}
$$

To better illustrate the calculation, an example with actual numbers is shown in Table 34.

In summary, the following is a procedure for segmenting (or not) a word $w$ (given a training wordset $W$ ):

1. Calculate $U_{W}^{\prime \prime}$
2. Consider any $s \triangleleft w$ such that $s \in U_{W}^{\prime \prime}$. If there is no such $s$, then output $w$ (no segmentation)
3. Otherwise, break $w=x s$ and apply the true/random-ending heuristic and output $x$ (segmentation appropriate) or $w$ (no segmentation) accordingly.

### 7.6 Evaluation

Evaluation was made on a small hand-made test set of 100 word types. 100 word types were selected from $W$ at random and manually segmented both

| $w$ | 'gadisnya' | 'hanya' |
| :--- | :--- | :--- |
| $x$ | gadis- | ha- |
| $s$ | $-n y a$ | $-n y a$ |
| $G^{*}(s)$ | $\left\{{ }^{\prime \prime}, k u, m u, n y a\right\}$ | $\left\{{ }^{\prime \prime}, k u, m u, n y a\right\}$ |
| $\alpha_{W} G^{*}(s)$ | 0.205 | 0.205 |
| $C_{W}(x)$ | $\left\{{ }^{\prime \prime}, n y a, m u\right\}$ | $\{n y a$, sratmu, ncurkanlah, rta,$\ldots\}$ |
| $C_{W}(x) \cap G^{*}(s)$ | $\left\{{ }^{\prime \prime}, n y a, m u\right\}$ | $\{n y a\}$ |
| $C_{W}(x) \backslash G^{*}(s)$ | $\}$ | $\{$ sratmu, ncurkanlah, rta,$\ldots\}$ |
| $\left\|C_{W}(x) \backslash G^{*}(s)\right\| \cdot \log \left(1-\alpha_{W}\left(G^{*}(s)\right)\right)$ | 0.0 | -56.9 |
| $\left(\left\|C_{W}(x) \cap G^{*}(s)\right\|\right) \cdot \log \alpha_{W}\left(G^{*}(s)\right)$ | -4.8 | -1.61 |

Table 34. The True/Random-Ending Heuristic as applied to the words 'gadisnya' (segmentation appropriate) and 'hanya' (no segmentation).
prefix-wise and suffix-wise. For example, 'direncanakannya' was segmented 'di-rencana-kan-nya' and 'mengerutkan' segmented to 'meng-erut-kan' (in all cases where the first character of the root changes as a prefix is added, we arbitrarily chose to define the correct segmentation border so that the result of the mutation belongs to the prefix part). A total of 64 segmentations were found on the 100 words. The unsupervised algorithm was applied to the 100 words, once suffixwise and once prefix-wise. 58 of segmentations were appropriately found, none spurious and 6 missed (i.e., full precision but $58 / 64=90.6 \%$ recall). All 6 of the missed segmentations were words with stacked affixes such as -kan-lah, or with final -an.

We know of no purely unsupervised stemming approach to Malay/Indonesian. On the other hand, a relatively large number of descriptions of work on manual, supervised and semi-supervised Malay/Indonesian stemmers/analyzers have appeared in the literature (Pisceldo et al. 2008, Adriani et al. 2007, Abdullah et al. 2009, Tai et al. 2000, Ahmad et al. 1996, Ranaivo 2001, Ranaivo-Malançon 2004, Indradjaja and Bressan 2003). Unfortunately, none of these stemmer/analyzers appears to be available for online processing or as a downloadable program, and, though well-described, require a fair amount of manual labour to reproduce. Therefore we are unable to present accuracy figures for comparison.

### 7.7 Discussion

The outlined algorithm is admittedly a complex path of rather untransparent heuristics whose properties we are, at this stage, not able to prove in a mathematically rigourous manner. Nevertheless, all of them have a clear intuition and therefore some of its virtues and errors are easily explainable. Also, as promised, there are no human thresholds or parameters whatsoever.

The accuracy is promising, but we do expect false positives to turn up in larger test sets, such as oversegmentations of $-i$ and segmentation with one of the very rare spurious suffixes that survived purging. Undersegmentation, as a result of the one-slot straitjacket, is the main error. Future work, naturally, will
focus on extending the heuristics to the multi-slot case. Our feeling is that this is possible, with the same level of accuracy, at the cost of an even more complex web of heuristics.

The present experiment aims to show that, at least for a certain type of languages, unsupervised approaches are competitive accuracywise, and likely to be favoured in a labour/accuracy stand-off. On the other hand, Indonesian morphology is so simple that rule-writing would so take little time, that a hybrid system of hand-written rules and lexicon-less heuristics borrowed from the present approach, would be a serious competitor as well.

### 7.8 Conclusion

We have presented a partially novel unsupervised algorithm for morphological segmentation of a arbitrary natural language with only one-slot concatenative morphology. The algorithm achieves high accuracy on Indonesian, a language with little, but mostly one-slot, morphology. An extension of the algorithm to deal systematically with multi-slot morphology is a priority for future work. The presented experiment with Indonesian clarifies the position of unsupervised methods for morphological analysis for low-density languages as an alternative to traditional manual implementation of rules and lexicon.

# 8 Application 4: Bootstrapping Language Description: The case of Mpiemo (Bantu A, Central African Republic) 


#### Abstract

Linguists have long been producing grammatical decriptions of yet undescribed languages. This is a time-consuming process, which has already adapted to improved technology for recording and storage. We present here a novel application of NLP techniques to bootstrap analysis of collected data and speed-up manual selection work. To be more precise, we argue that unsupervised induction of morphology and part-of-speech analysis from raw text data is mature enough to produce useful results. Experiments with Latent Semantic Analysis were less fruitful. We exemplify this on Mpiemo, a so-far essentially undescribed Bantu language of the Central African Republic, for which raw text data was available.


### 8.1 Introduction

Descriptive linguistics, i.e., producing a grammatical description of a language (often previously unstudied or little-studied), is essential for the understanding of the language diversity in the world, for linguistic theory, for the historical study of populations and, last but not least, for the speakers themselves (van der Voort 2007). It is even more a priority given the current state of language endangerment (Brenzinger 2007).

Describing a language typically consists of producing a grammar, a dictionary and a collection of texts. In this paper, we suggest that this process can benefit from technology in the sense that it can speed up the human tasks of analysis and organisation. In particular, we show that techniques from computational linguistics are now mature enough that morphological analysis, part-ofspeech analysis and potentially lexical semantic analysis can be bootstrapped from raw text. As an example language, we use Mpiemo (Bantu A, Central African Republic), for which some raw text data was available.

We focus here on motivation and proof-of-concept, leaving the linguistic details to a specialist northwest Bantu audience, and the technical details to a computational linguistics audience.

### 8.2 Motivation and Related Work

In language documentation and language description, one is bang-up-to-date with technology for recording, storage, annotation, modularization and presentation Gippert et al. 2006 . But technology can be further used to bootstrap analysis and speed-up manual work. In particular, we suggest that some analysis and organizing can be automatically extracted from raw text data.

[^8]Typically, a researcher works on grammar, texts and dictionary incrementally. A text is gathered first, which is then analysed and vacuumed for dictionary entries. Usually, texts can be gathered by a wider range of people, including people not schooled in linguistic theory, and there are many cases, old and new, where large text collections exist but there is no written down grammar/dictionary for the same language 10 In other words, large text collections already exist for various undescribed languages, and for many others, text collections can be gathered relatively cheaply. This motivates our approach of bootstrapping from text.

There are also other, perfectly legitimate, ways to adapt grammar writing to enable technological exploitation. Nordhoff (2007a,b) describes the grammar authoring system GALOES where the researcher writes the data in a format which allows harvesting, i.e., a computational tool can automatically select and collect data from grammars written in this way. Considerable flexibility in presentation, i.e., away from the strictly linear format of book grammars, also come with this grammar authoring system. Similarly, Beermann Hellan (2007) describes TypeCraft which is a support tool for glossing and annotation which helps researchers with consistency and sharing. This enables more systematic searching and harvesting as well. These approaches are complimentary to the one suggested in this paper because the analysis itself is still fully the researchers burden, and use of the tools require linguistic training as well as computer familiarity.

Similar, unsupervised, techniques as we describe in this paper exist for further applications such as Information Retrieval, Spell-Checking etc. which are on the want list for low-density languages (Saxena and Borin 2006), but this is not the focus of the present paper. Unfortunately, we are not aware of any Speech Technology tools equally suitable for facilitating work on language description.

### 8.3 Mpiemo Profile and Data

Mpiemo is spoken predominantly in the southwest of the Central African Republic (CAR) and in neighbouring Cameroon and Congo (= République du Congo, or Congo-Brazzaville). There are approximately 24000 speakers in the Central African Republic, about 5000 in Cameroon and an unknown, but presumably small, number of people in Congo (Gordon 2005).

In the Central African Republic, almost all speakers are bilingual in Sango (the lingua franca of CAR), and knowledge of (varieties of) Gbaya, French, Lingala is also common. Mpiemo is losing ground but is still being transmitted to children. At present it is not an endangered language. Traditionally Mpiemo is not written but an orthography has been developed recently by missionaries (Thornell 2004a).

[^9]Mpiemo is placed in the Bantu A. 80 (or 'Maka-Njem') group, but there is no detailed understanding of its proper classification (Maho 2003).

The is no published grammatical description of Mpiemo but a text collection is scheduled to appear shortly (Thornell 2008). There are also some papers on special topics (Thornell and Nagano-Madsen 2004, Thornell 2003, 2004b) as well as some unpublished papers by SIL members in Cameroon. While the full morphosyntax of Mpiemo has yet to be described, some typological features are apparent. Like (almost) all Bantu languages, Mpiemo has a noun class system with alternating singular/plural prefixes. However, unlike Southern and Eastern Bantu, Mpiemo and other northwest Bantu languages tend not to have elaborate verb morphology. The language has SVO basic constituent order and has tones, but the tonal distinctions appear to have a low functional load.

At our disposal we had raw text data amounting to approximately 60000 running words collected (1999-2008) by Christina Thornell in the Nola district of the Central African Republic. The texts are narrative descriptions of daily activities and local flora/fauna. We made use of all text data available. An example snippet is shown in Table 35 .

Bandi he ri ke gwobi i ri be de go: Hi no meligi, hi ke be sombi Mpanja, hi joว̀ pèà go, ha ne Kamil hó ri ké. Hí jò̀ pèà gó, Kamil no mعlándi. Hí kè joò téri sómbi, a nó mélígí, à wá tí sómbi ya. Mè rì yé nyè mèkògì. À lán mélígí má tí sombi yà gó. Hi kwàn, hí sàà, hí ké bé mpàlà.
La pêche se passe comme ça: Nous prenons les filets, nous allons à la rivière Pandja, nous arrivons là-bas, Camille et moi, nous partons. En arrivant là-bas, Camille prend la pirogue. A peine arrivons-nous au beau milieu de la rivière, il prend les filets, les met à la rivière. Je lui passe des pierres. Il tend les filets dans la rivière.

Table 35. Sample snippet of Mpiemo text.

### 8.4 Bootstrapping Experiments

## Morphological Induction

As mentioned above, Mpiemo appears to have very little morphology. However, it is quite clear that there is a typical Bantu noun class system with alternating singular/plural prefixes, i.e., all nouns have two forms, one with a prefix to yielding singular meaning and one prefix yielding plural meaning. The Bantu descriptive tradition calls each prefix a 'class' and each class has a number. The goal is that classes which are cognate across Bantu languages should have the same class number in different languages (Maho 2003). Our task is thus to unravel the Mpiemo specifics and relate them to the Bantu descriptive tradition.

Hammarström (2007b) describes techniques for inducing concatenative morphology automatically, i.e., with no human intervention, from raw text data. In other words, if we input raw text data only, salient suffixes and prefixes can
be extracted, and stems which take the same suffixes/prefixes systematically, can be listed. How this is done is explained elsewhere (Hammarström 2007b) including a full survey of work done on morphology induction.

The algorithm of Hammarström (2006a) was run on the approxiamtely 60 000 running words of Mpiemo text. The goal was to find the known prefixes correctly segmented and not to find any spurious prefixes or suffixes. As expected, the algorithm finds no salient suffixes for Mpiemo 11 As for prefixes, the algorithm found the segmentations listed in Table 36. All of the segmentations turn out to be consistent with human analysis. (There is no point in a formal evaluation since the human analysis is not definitive, rather, the idea is to suggest segmentations that the researcher checks.)

| Segmentation | Comment |
| :--- | :--- |
| $a-$ | class prefix for 5 |
| $b-$ | class concord for 2 |
| $b i-$ | class prefix for 8 |
| $b o-$ | class prefix for 2 |
| $b \grave{-}$ | tonal allomorph for $b i-?$ |
| $b \varepsilon-$ | class prefix for $2 \mathrm{a} ?$ |
| $b \varepsilon \bar{\varepsilon}-$ | allomorph for $b \varepsilon-$ |
| $m-$ | concord for 6 |
| $m \varepsilon-$ | class prefix for 6 |
| $m \dot{\varepsilon}-$ | tonal allomorph for $m \varepsilon-$ |
| $y-$ | concord for 9 and others |
| $y i-$ | concord for 9 |

Table 36. Outcome of affix extraction for Mpiemo.
Hammarström (2006b) is an unsupervised method to find stems which tend to appear with the same set of affixes, or, as one might call it, paradigm induction (presented in Section 4). Together with prefix extraction, we get a ranked list of <stem, prefix-set> pairs. The top pairs are shown in Table 37, The precision is excellent - fully conformant to human analysis - but recall is low. The paradigm of most stems cannot be inferred since they occur too sparsely, or, in other words, the corpus size is too small.

| Prefix-Set | Stem | Translation |
| :--- | :--- | :--- |
| $b i-$ sani "thing" <br> $\varnothing-$   <br> mo- <br> $b o-$ ri "person" <br> $\ldots$  $r$ |  |  |

Table 37. Top pairs in paradigm induction.

[^10]The value of these lists is that it speeds up the human analysis. Looking at the ranked lists, it is easy for a researcher to compare with other Bantu languages of the same region. The best described closely related language is Kol in Cameroon (Henson 2007). With stems neatly categorized for prefixes, it is straightforward to compare and to see that, e.g., bi-must be class 8. Similarly, all of the above prefixes can be readily identified as inherited Bantu classes or subclasses (Maho 2003). There appears to be some tonal allomorphy associated with the noun class prefixes. The morphology induction algorithm has no access to semantics, so it can not suggest which prefixes are allomorphic to each other, but the listings are handy for forming testable hypotheses.

In any case, whether human or machine analysed morphology, all stems and paradigms need to be double checked with speakers.

## Part-of-speech Induction

Even a cursory inspection of the text data shows that Mpiemo distinguishes nominal and verbal classes distributionally. In addition, there are a number of particles whose position is unclear. Our task is therefore to get some headway in the understanding of these particles.

We have surveyed part-of-speech induction techniques. In general, there is very little work that is both truly unsupervised and aimed at a wide range of languanges. Biemann (2006) describes a mostly unsupervised part-of-speech tagger. The algorithm determines the number of different part-of-speech tags automatically, but there are a number of parameters that need to be tweaked.

The results are complicated by a number of parameter variations which are set ad hoc according to our existent but imperfect knowledge of Mpiemo. The exact settings and iterations are of little interest in this case - the point is whether the unsupervised computational analysis, allowing for a reasonable number of iterations, was of any help for the researcher. The results are that nominal and verbal classes emerge, but there is more than one nominal class and more than one verbal class. Impressionistically, also many infrequent words seem to end up in the right company. This is important, because most words of a running text are infrequent, and a good first guess at their part-of-speech can save a lot of time in dictionary making. 'go' which may be a focal particle, is given a class of its own. Pronouns and what appears to be a pre-verbal particle for future marking always end up in the same class.

The results are good enough for some provisional assignments, but the distributional nature of particles need further study.

## Semantic Grouping

Latent Semantic Indexing (Sahlgren 2006) is a popular technique that can be used to infer semantic distances between words from raw text data. The intuition is that words that appear in the same "context" tend to be similar in meaning, once frequency discrepancies are discounted for. (Frequent words appear in all contexts, but they are not semantically similar to "everything".)

Sometimes a one-word windows is used as the context, sometimes the sentence, but most commonly the document is used as a context (the raw text data used comes already divided into documents in these cases). When latent semantic analysis is successfully applied to major European languages, the raw data sources are typically huge, with (at least) millions of word tokens.

The goal of experimenting with latent semantic analysis on Mpiemo was to find semantically related words, such as animates, and because many of the texts were about plants, perhaps a category of plant names. In order for LSA techniques to operate on the minuscule size of the corpus, we had little choice but to use the sentence as context (anything bigger would have made the data set tiny, and anything smaller would reduce the semantic analysis towards part-of-speech analysis, i.e., syntactically legal contexts). We then tried simply to cluster on the LSA similarity measure. The result was that 'question words' was the cluster deemed most semantically related, presumably because of the question marks in sentences containing them. Little more of value came out of the attempt, presumably because the text corpus was simply too small.

### 8.5 Discussion

Bootstrapping from text data for grammar/dictionary writing is parallel to Machine Translation in that it will not replace humans in the foreseeable future. Its purpose is instead to save time for the same humans. Even small time saves are valuable. We have indicated that bootstrapping is worthwhile if the text collection is of moderate size. There are also some positive side-effects of the attempts that were unforeseen:

- Transcription consistency checking (almost like spell-checking) came out naturally from the morphological listings.
- The automatically annotated texts, which would otherwise just have gathered dust after analysis, could easily be ported to other formats, for example TEI/XML to be used in a pedagogical tool which teaches grammar to linguistics students (Borin and Saxena 2004).

NLP bootstrapping techniques can be seen as a generalization of a corpus concordancer. A concordancer highlights and selects raw data and presents it in a manner suitable for a human analysis. As we argue, the same can be done at least for morphological analysis and part-of-speech analysis.

The usefulness hinges on the existence of a large body of raw text data. For some languages, division of labour allows such data to be gathered relatively cheaply. For many other languages, text collections already exist and can be made use of.

### 8.6 Conclusion

We have shown that language technology can be used to save time in language description. For the particular language Mpiemo, the morphology is quite sim-
ple, and morphology induction works very well for it. The usefulness of part-of-speech induction is harder to assess, and we were not successful in exploiting techniques for latent semantic analysis. Some positive side effects that may arise from the applying NLP technology to languages which traditionally were not treated computationally, are consistency checking and usage of tagged corpora for teaching purposes.

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# Chapter II A Survey of Computational Morphological Resources for Low-Density Languages 

Hammarström, H. (2009). A Survey of Computational Morphological Resources for Low-Density Languages Submitted.

# A Survey of Computational Morphological Resources for Low-Density Languages 

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#### Abstract

The present paper is a survey of published work on computational morphological resources for so-called low-density languages. To avoid confusion, we introduce the term low-affluence language for a language whose speakers have low economic power. We assert empirically the appreciable observation that computational morphological resources emerge for languages with higher affluence, and we can now also account for the manner in which this happens and for the exceptions to the rule. The survey collects a wide array of work on computational morphology for low-density languages and as such outlines cross-linguistic trends in computational morphology.


## 1 Introduction

The present paper looks at computational morphological resources for so-called low-density languages. A survey of this kind is relevant for understanding how language resources come about [for low-density languages], which in turn is relevant for the broader questions of language survival [of low-density languages]. It is also relevant for the design and application of unsupervised NLP tools, which potentially offer their highest added value for low-density languages. These issues have been discussed in more detail in several works (Yli-Jvrä|2005, Streiter et al. 2006, Berment 2004, David and Maxwell 2008, Sornlertlamvanich 2008, Singh 2008) but there is so far no empirically grounded understanding of how language resources for low-density languages emerge. For this reason, in this paper we focus on a comprehensive survey, with the aim of a better understanding of the past and future dynamics of language resources.

The term low-density languages is increasingly employed to denote a set of languages distinct from the most powerful and affluent languages. To some,
to have a low density of language resources is the defining property of being a low-density language. In this view, a language which receives a fair amount of resources automatically ceases to be a low-density language. To others, low density languages are a class which are underprivileged vis-a-vis the big players, and an absolute increase in density - as long as it fails to disrupt the skewing - does not change the status of a language. To avoid confusion, we introduce a new term "low-affluence language'11, which singles out the set of languages of interest but is oblivious as to whether there exist resources for a given language. It is then an empirical question which low-affluence language have resources of various kinds. Accordingly, the present paper surveys which languages have (a published description of) a computational morphological analyser of some sort.

We also aim to gather together work which is otherwise scattered in very disparate fora to facilitate comparison - presumably important lessons from one language can be taught to another language in a similar situation.

We focus on resources for morphological analysis since it is one of the bottom layers of analysis of written language data (cf. Beesley 2004, Berment 2004:1826 and Oflazer 2009). The layer below, namely raw text data, has already been addressed in several other initiatives (Baldwin et al. 2006, Xia and Lewis 2009, Lewis 2003, Xia and Lewis 2008, Scannell 2007, Mallikariun 2003). It is clear that the languages for which raw text data appears on the web ${ }^{2}$ is much larger than those for which there is a published description of a morphological analyser.

## 2 Low-Affluence Languages

For this survey to be practical we need a clear definition of what a low-density language is, rather than a sliding scale or a prototypical set of properties.

We suggest that the set of languages of interest may be characterized in terms of the economic power of its speakers. Hence, in analogy with Gross National Product (GNP), we define the Gross Language Product (GLP), of a language as the total market value of all final goods and services produced by the speakers of the language within a calendar year. Since there is no detailed data available to compute this statistic accurately for a large number of languages, we use the following formula to estimate GLP:

$$
G L P(L)=\sum_{C} S_{C}(L) \cdot G N P \text {-per-capita }(C)
$$

Where $S_{C}(L)$ denotes the number of L1 speakers of language $L$ in country $C$. For example, our data claims that Finnish has 4700000 speakers in Finland $(G N P$-per-capita $=46769), 200000$ in Sweden $(G N P$-per-capita $=50415)$ and

[^11]$34100(G N P$-per-capita $=14800)$ in Russia. So GLP (Finnish $)=4700000 \cdot$ $46769+200000 \cdot 50415+34100 \cdot 14800=230401980000$. Since most languages are spoken only in a few countries, $S_{C}(L)=0$ for most countries $C$, thus contributing nothing to the sum.

We employ the convenient fiction that the GNP-per-capita for a country is indicative also of each subpopulation of speakers of that country. We strongly suspect, however, that for most minority languages of a country, the $G N P$-per-capita of the speakers of the minority languages is lower than the average of the country as a whole. Furthermore, we only have systematic data on L1 speaker numbers but, obviously, the economic power of L2 speakers is relevant as well. However, the cases where L2-economies appear to be the most significant ${ }^{3}$ are among high-affluent languages anyway, so although their economic power is underestimated by the above formula, they are still too far from being low in affluence. Data for GNP per capita from Central Intelligence Agency of the United States (2007) and speaker numbers from Lewis (2009) are accessible. The GNP-figures used are not PPP-adjusted since the prices for NLP related services appear to have little to do with local prices for basic commodities. Table $1 / 2$ shows the top 140 affluent languages according to the GLP-metric just explained.

For the purposes of this paper, we will put the threshold of low-density at 100 billion dollars of GLP. This threshold was chosen based on nothing more than its large number of zeroes and the fact that a convenient number of non-low-affluence languages emerge. With this setting, there are currently 44 non-low-affluence languages, and all the rest, beginning with Ukrainian at rank \#45, are low-affluence languages 4 Of the 44 high-affluence languages, 25 are predominantly European, 16 are Asian and 3 (English, Spanish, Portuguese) are European in origin but have more speakers in the Americas.

The top 44 high-affluence languages all have fair amounts of NLP infrastructure (including the less obvious Catalan, Farsi, Romanian, Hungarian and Bengali) except for an important class of languages with the following properties:

- They are not popularly written
- In the country where they are spoken, there is a standardized close relative which is the preferred language for written communication

The high-affluence languages which fall into this class are Bavarian-MainfränkischSwiss German (under German), Min Nan-Wu-Yue-Hakka-Kinyu (under Mandarin Chinese), Galician (under Spanish), Lombard-Piemontese-Napoletano-Calabrese-Sicilian-Venetian (under Italian), Javanese (under Indonesian), Vlaams (under Dutch) and Najdi Arabic (under Modern Standard Arabic).

[^12]| \# | Language | iso-639-3 | GLP |  |  | Total | Pop. | GNP-per-capita |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | English | eng | 14570 | 1196 | 604622 | 326959 | 888 | 44562.4 |
| 2 | Japanese | jpn | 4162 | 6420 | 000000 | 121000 | 000 | 34402.0 |
| 3 | Spanish | spa | 41177 | 7238 | 821500 | 327380 | 860 | 12577.7 |
| 4 | German, Standard | deu | 3408 | 8031 | 154660 | 84959 | 210 | 40122.8 |
| 5 | Arabic, Standard | arb | 28077 | 780 | 000000 | 206000 | 000 | 13630.0 |
| 6 | French | fra | 2775 | 416 | 019700 | 67661 | 960 | 41018.8 |
| 7 | Chinese, Mandarin | cmn | 2146 | 3872 | 252580 | 845033 | 030 | 2540.0 |
| 8 | Italian | ita | 20611 | 1189 | 900800 | 56638 | 620 | 36390.6 |
| 9 | Russian | rus | 1809 | 9379 | 945460 | 125102 | 940 | 14467.5 |
| 10 | Portuguese | por | 1345 | 0898 | 888980 | 174307 | 980 | 7716.7 |
| 11 | Dutch | nld | 966 | 8831 | 126740 | 21309 | 290 | 45373.7 |
| 12 | Korean | kor | 885 | 3678 | 820000 | 64739 | 000 | 13675.9 |
| 13 | Bavarian | bar | 570 | 2874 | 492000 | 13259 | 000 | 43011.3 |
| 14 | Turkish | tur | 445 | 3439 | 958400 | 47777 | 700 | 9321.1 |
| 15 | Swedish | swe | 412 | 6262 | 274000 | 8206 | 000 | 50283.4 |
| 16 | Polish | pol | 412 | 3587 | 750120 | 36998 | 360 | 11145.3 |
| 17 | Catalan-Valencian-Balear | cat | 404 | 2980 | 076000 | 11351 | 000 | 35617.8 |
| 18 | Norwegian | nor | 392 | 5208 | 800000 | 4640 | 000 | 84595.0 |
| 19 | Chinese, Min Nan | nan | 382 | 848 | 478700 | 46915 | 100 | 8160.4 |
| 20 | German, Swiss | gsw | 337 | 4111 | 118000 | 6469 | 000 | 52158.1 |
| 21 | Lombard | lmo | 336 | 656 | 463000 | 9133 | 000 | 36861.5 |
| 22 | Greek | ell | 334 | 0908 | 819150 | 11526 | 360 | 28984.9 |
| 23 | Danish | dan | 312 | 1612 | 238200 | 5478 | 830 | 56975.8 |
| 24 | Vlaams | vls | 267 | 9494 | 458000 | 6132 | 000 | 43696.9 |
| 25 | Napoletano-Calabrese | nap | 255 | 2170 | 050000 | 7050 | 000 | 36201.0 |
| 26 | Finnish | fin | 230 | 4019 | 980000 | 4934 | 100 | 46695.8 |
| 27 | Mainfränkisch | vmf | 197 | 946 | 650000 | 4910 | 000 | 40315.0 |
| 28 | Chinese, Wu | wuu | 189 | 9184 | 445380 | 77201 | 820 | 2460.0 |
| 29 | Hindi | hin | 177 | 285 | 437200 | 180469 | 200 | 982.3 |
| 30 | Sicilian | scn | 174 | 8508 | 830000 | 4830 | 000 | 36201.0 |
| 31 | Czech | ces | 158 | 6907 | 740000 | 9290 | 000 | 17081.8 |
| 32 | Javanese | jav | 157 | 8223 | 354630 | 84600 | 970 | 1865.4 |
| 33 | Romanian | ron | 157 | 0939 | 940480 | 23118 | 480 | 6795.1 |
| 34 | Hungarian | hun | 156 | 1321 | 196260 | 12253 | 140 | 12742.2 |
| 35 | Chinese, Yue | yue | 148 | $4025$ | 526750 | 54471 | 530 | 2724.4 |
| 36 | Bengali | ben | 121 | 6329 | 915000 | 180624 | 200 | 673.4 |
| 37 | Chinese, Hakka | hak | 116 | 4569 | 948110 | 29976 | 560 | 3884.9 |
| 38 | Galician | glg | 113 | 0906 | 635000 | 3185 | 000 | 35507.2 |
| 39 | Piemontese | pms | 112 | 5851 | 110000 | 3110 | 000 | 36201.0 |
| 40 | Hebrew | heb | 112 | 3308 | 850000 | 4850 | 000 | 23161.0 |
| 41 | Arabic, Najdi Spoken | ars | 112 | 1171 | 150000 | 9450 | 000 | 11864.2 |
| 42 | Chinese, Jinyu | cjy | 110 | 6550 | 000000 | 45000 | 000 | 2459.0 |
| 43 | Farsi, Western | pes | 109 | 3059 | 988000 | 22455 | 000 | 4867.7 |
| 44 | Venetian | vec | 106 | 5936 | 680000 | 6230 | 000 | 17109.7 |
| 45 | Ukrainian | ukr | 96 | 1739 | 972800 | 31260 | 800 | 3076.5 |
| 46 | Chinese, Xiang | hsn | 88 | 5240 | 000000 | 36000 | 000 | 2459.0 |
| 47 | Arabic, Egyptian Spoken | arz | 835 | 5800 | 000000 | 52500 | 000 | 1592.0 |
| 48 | Malay | zlm | 82 | 3787 | 737000 | 10181 | 000 | 8091.4 |
| 49 | Occitan | oci | 81 | 9245 | 544560 | 2048 | 310 | 39996.1 |
| 50 | Arabic, Hijazi Spoken | acw | 817 | 7858 | 879400 | 6023 | 900 | 13576.8 |
| 51 | Saxon, Upper | sxu | 80 | 6300 | 000000 | 2000 | 000 | 40315.0 |
| 52 | Arabic, Algerian Spoken | arq | 80 | 4780 | 000000 | 20400 | 000 | 3945.0 |
| 53 | Tatar | tat | 79 | 1819 | 967200 | 5350 | 800 | 14798.1 |
| 54 | Tamil | tam | 79 | 0910 | 044720 | 66787 | 482 | 1184.2 |
| 55 | Thai | tha | 76 | 275 | 200000 | 20200 | 000 | 3776.0 |
| 56 | Arabic, Gulf Spoken | afb | 75 | 1086 | 676000 | 2339 | 000 | 32111.4 |
| 57 | Emiliano-Romagnolo | eml | 73 | 1296 | 640100 | 2020 | 100 | 36201.0 |
| 58 | Ligurian | lij | 697 | 7109 | 940000 | 1925 | 100 | 36211.5 |
| 59 | Telugu | tel | 67 | 7208 | 800000 | 69600 | 000 | 973.0 |
| 60 | Arabic, South Levantine Spoken | ajp | 67 | 3916 | 610000 |  | 000 | 11213.2 |
| 61 | Slovak | slk |  | 261 | 405800 | 4894 | 800 | 13741.4 |
| 62 | Marathi | mar | 66 | 1640 | 000000 | 68000 | 000 | 973.0 |
| 63 | Sunda | sun | 627 | 730 | 000000 | 34000 | 000 | 1845.0 |
| 64 | Zulu | zul | 587 | 7076 | 636000 | 10344 | 500 | 5675.2 |
| 65 | Limburgish | lim | 58 | 6611 | 100000 | 1300 | 000 | 45123.9 |
| 66 | Azerbaijani, South | azb | 56 | 6778 | 840000 | 12360 | 000 | 4585.5 |
| 67 | Thai, Northeastern | tts | 56 | 640 | 000000 | 15000 | 000 | 3776.0 |
| 68 | Urdu | urd | 56 | 428 | 350000 | 59126 | 000 | 954.3 |
| 69 | Vietnamese | vie | 54 | 2811 | 199800 | 66200 | 200 | 819.9 |
| 70 | Panjabi, Western | pnb | 53 | 3078 | 830000 | 62510 | 000 | 852.7 |
| 71 | Croatian | hrv | 51 | 4182 | 268570 | 4666 | 300 | 11019.0 |
| 72 | Chinese, Gan | gan | 50 | 655 | 400000 | 20600 | 000 | 2459.0 |
| 73 | Chinese Sign Language | csl | 49 | 278 | 360000 | 20040 | 000 | 2459.0 |
| 74 | Walloon | wln | 48 | 8857 | 760000 | 1120 | 000 | 43648.0 |
| 75 | Bulgarian | bul | 475 | 5785 | 541000 | 8781 | 750 | 5417.8 |

Table 1. 140 top-affluence languages, ranked by GLP [Page 1(2)].

| \# | Language | iso-639-3 |  |  | GLP | Tota | al P | Pop. | GNP-per-capita |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 76 | Kurdish, Northern | kmr | 47420 | 2050 | 000 | 84 | 493 | 000 | 5583.4 |
| 77 | Xhosa | xho | 45530 | 52400 | 000 | 78 | 808 | 000 | 5831.2 |
| 78 | Gujarati | guj | 44508 | 4926 | 600 | 459 | 959 | 800 | 968.4 |
| 79 | Slovene | slv | 44161 | 0461 | 190 | 18 | 851 | 190 | 23855.4 |
| 80 | Tswana | tsn | 42204 | 8735 | 500 | 45 | 521 | 700 | 9333.8 |
| 81 | Indonesian | ind | 42066 | 00000 | 000 | 228 | 800 | 000 | 1845.0 |
| 82 | Arabic, North Levantine Spoken | apc | 41684 | 3000 | 000 | 127 | 700 | 000 | 3282.2 |
| 83 | Arabic, Moroccan Spoken | ary | 40814 | 8000 | 000 | 188 | 800 | 000 | 2171.0 |
| 84 | Kazakh | kaz | 39924 | 3568 | 800 | 75 | 535 | 600 | 5298.0 |
| 85 | Arabic, Libyan Spoken | ayl | 38312 | 69200 | 000 | 4 | 321 | 000 | 8866.6 |
| 86 | Filipino | fil | 38250 | 00000 | 000 | 250 | 000 | 000 | 1530.0 |
| 87 | Bhojpuri | bho | 37933 | 9460 | 000 | 385 | 546 | 000 | 984.1 |
| 88 | Awadhi | awa | 36868 | 91300 | 000 | 382 | 261 | 000 | 963.6 |
| 89 | Pidgin, Nigerian | pcm | 34920 | 0000 | 000 | 300 | 000 | 000 | 1164.0 |
| 90 | Malayalam | mal | 34798 | 4700 | 000 | 354 | 410 | 000 | 982.7 |
| 91 | Kannada | kan | 34346 | 9000 | 000 | 353 | 300 | 000 | 973.0 |
| 92 | Guadeloupean Creole French | gcf | 34089 | 60000 | 000 |  | 848 | 000 | 40200.0 |
| 93 | Arabic, Mesopotamian Spoken | acm | 34054 | 4000 | 000 | 145 | 500 | 000 | 2348.5 |
| 94 | Azerbaijani, North | azj | 33962 | 6630 | 000 |  | 243 | 000 | 4689.0 |
| 95 | Okinawan, Central | ryu | 33851 | 5680 | 000 |  | 984 | 000 | 34402.0 |
| 96 | Belarusan | bel | 33339 | 5200 | 000 | 69 | 940 | 000 | 4803.9 |
| 97 | Swabian | swg | 33017 | 9850 | 000 |  | 819 | 000 | 40315.0 |
| 98 | Tagalog | tgl | 32895 | 0000 | 000 |  | 500 | 000 | 1530.0 |
| 99 | Maithili | mai | 31971 | 1000 | 000 | 347 | 700 | 000 | 921.3 |
| 100 | Lithuanian | lit | 31748 | 9600 | 000 | 29 | 960 | 000 | 10726.0 |
| 101 | Oriya | ori | 30844 | 1000 | 000 |  |  | 000 | 973.0 |
| 102 | Arabic, Tunisian Spoken | aeb | 30645 | 0000 | 000 | 90 | 000 | 000 | 3405.0 |
| 103 | Arabic, Sa'idi Spoken | aec | 30248 | 0000 | 000 | 190 | 000 | 000 | 1592.0 |
| 104 | Luxembourgeois | ltz | 29030 | 8431 | 150 |  | 320 | 010 | 90718.5 |
| 105 | Friulian | fur | 28743 | 5940 | 000 |  | 794 | 000 | 36201.0 |
| 106 | Afrikaans | afr | 28506 | 5273 | 300 | 49 | 903 | 900 | 5813.0 |
| 107 | Hawai'i Creole English | hwc | 27575 | 4000 | 000 |  | 600 | 000 | 45959.0 |
| 108 | Gronings | gos | 27462 | 2880 | 000 |  | 592 | 000 | 46389.0 |
| 109 | Turkmen | tuk | 27251 | 4771 | 160 | 59 | 930 | 920 | 4594.8 |
| 110 | Panjabi, Eastern | pan | 26712 | 7965 | 500 | 271 | 119 | 500 | 985.0 |
| 111 | Sotho, Southern | sot | 26107 | 1300 | 000 | 60 | 010 | 000 | 4343.9 |
| 112 | Chinese, Min Bei | mnp | 25469 | 4080 | 000 | 103 | 304 | 000 | 2471.7 |
| 113 | Madura | mad | 25123 | 8843 | 300 | 136 | 600 | 900 | 1847.2 |
| 114 | Chinese, Min Dong | cdo | 25099 | 4422 | 220 | 91 | 134 | 060 | 2747.8 |
| 115 | Serbian | srp | 25004 | 8411 | 100 | 63 | 379 | 460 | 3919.5 |
| 116 | Chuvash | chv | 24272 | 0000 | 000 |  | 640 | 000 | 14800.0 |
| 117 | Cebuano | ceb | 24174 | 0000 | 000 | 158 |  | 000 | 1530.0 |
| 118 | Hausa | hau | 23948 | 6965 | 500 |  |  | 000 | 963.1 |
| 119 | Sotho, Northern | nso | 23897 | 8700 | 000 | 40 | 090 | 000 | 5843.0 |
| 120 | Basque | eus | 23697 | 3200 | 000 |  | 656 | 200 | 36112.9 |
| 121 | Welsh | cym | 23340 | 3080 | 000 |  | 533 | 000 | 43790.4 |
| 122 | Uyghur | uig | 22699 | 7155 | 500 | 87 | 704 | 500 | 2607.8 |
| 123 | Thai, Northern | nod | 22661 | 8092 | 200 | 60 | 009 | 400 | 3771.0 |
| 124 | Réunion Creole French | rcf | 22311 | 0000 | 000 |  | 555 | 000 | 40200.0 |
| 125 | Yoruba | yor | 22304 | 6400 | 000 | 193 | 365 | 000 | 1151.8 |
| 126 | Sinhala | sin | 22257 | 1129 | 950 | 155 | 500 | 850 | 1435.8 |
| 127 | Frisian, Western | fry | 21663 | 6630 |  |  | 467 | 000 | 46389.0 |
| 128 | Igbo | ibo | 20952 | 0000 | 000 | 180 | 000 | 000 | 1164.0 |
| 129 | Gaelic, Irish | gle | 20697 | 3100 | 000 |  | 355 | 000 | 58302.2 |
| 130 | Bashkort | bak | 20424 | 000 | 000 |  | 380 | 000 | 14800.0 |
| 131 | Hunsrik | hrx | 20328 | 000 | 000 | 30 | 000 | 000 | 6776.0 |
| 132 | Breton | bre | 20100 | 000 | 000 |  | 500 | 000 | 40200.0 |
| 133 | Umbundu | umb | 20012 | 000 | 000 | 40 | 000 | 000 | 5003.0 |
| 134 | Chechen | che | 19691 | 9350 | 000 |  | 333 | 000 | 14772.6 |
| 135 | Malay, Kedah | meo | 19523 | 4000 | 000 | 26 | 600 | 000 | 7509.0 |
| 136 | Sindhi | snd | 18440 | 6300 | 000 | 213 | 310 | 000 | 865.3 |
| 137 | Sardinian, Logudorese | src | 18100 | 5000 | 000 |  | 500 | 000 | 36201.0 |
| 138 | Kabardian | kbd | 17807 | 7750 | 000 |  | 629 | 000 | 10931.7 |
| 139 | Arabic, Sudanese Spoken | apd | 17580 | 0000 | 000 | 150 | 000 | 000 | 1172.0 |
| 140 | Chhattisgarhi | hne | 17027 | 5000 | 000 | 175 | 500 | 000 | 973.0 |
| 141 | Thai, Southern | sou | 16992 | 000 | 000 | 45 | 500 | 000 | 3776.0 |
| 142 | Latvian | lav | 16816 | 2200 | 000 | 13 | 390 | 000 | 12098.0 |
| 143 | Assamese | asm | 16253 | 4290 | 000 | 167 | 709 | 000 | 972.7 |
| 144 | Arabic, North Mesopotamian Spoken | ayp | 16120 | 1000 | 000 |  | 100 | 000 | 2642.6 |

Table 2. 144 top-density languages, ranked by GLP [Page 2(2)].

## 3 Survey Methodology

The methodology used for gathering the items in the survey was general knowledge, browsing of the meta-literature, the corpora-list and googling suitably for each of the 100 most affluent low-affluence languages. No restriction as to the meta-language was applied (the author is able read nearly all languages under consideration) but, nevertheless, mostly descriptions written in English turned up.

For languages which have very little morphology we listed some other NLP work at a comparable stage, that is, the next processing level after raw text data. Similarly, work on languages where the orthography forces morphological segmentation, is listed along the same principle.

In some cases, the work found does not cover all of morphology of the language in question. In such cases, the language is "rounded-off" and counted as one having morphological resources. Stemmers are counted along the same principle.

We have adhered to the criterion that the work has to have been published, available as a thesis or available on the web with a fair amount of information. Conference presentations, manuscripts and other items of partial or unavailable reports are not counted 5

For short, we use the term CMR for computational morphological resources with a published description of the kind explained.

## 4 Survey Results

The results of the survey are shown in Tables [3] arranged alphabetically and by continent. Table 7 shows a summary of the number of languages found in the survey. The survey lists 80 low-affluence languages for with CMR. We suspect, however, that there is more work on which nothing has been published so far.

## 5 Discussion

The survey allows us to shed light on the questions posed in the introduction about the emergence of CMR for low-affluence languages.

### 5.1 Which languages obtain CMR?

The survey outcome confirms the intuition that high GLP is strongly correlated with obtaining CMR - on all continents, the average GLP of the languages with CMR is higher than the average GLP of the continent as a whole.

[^13]| Language | iso-639-3 | GLP | \# | Publication(s) |
| :---: | :---: | :---: | :---: | :---: |
| Afrikaans | afr | 28506527300 | 106 | de Stadler and Coetzer 1990 |
| Amharic | amh | 5154640000 | 255 | Gambäck et al. 2009, Ephrem |
|  |  |  |  | 2006, Alemayehu and Willett |
|  |  |  |  | Alemu Argaw and Asker 2007, Bavou |
|  |  |  |  | 2000, Bati 2002, Fissaha Adafre 2005 |
| Bamanankan | bam | 1523003100 | 442 | Fleisch and Seidel 2006 |
| Dholuo | luo | 3447920000 | 306 | Pauw et al. 2007 |
| Gikuyu | kik | 5700920000 | 242 | De Pauw and Wagacha 2007 |
| Ekegusii | guz | 1683403300 | 417 | Elwell 2008 |
| На | haq | 406890000 | 790 | Hariula 2005 |
| Malagasy, Plateau | plt | 2827954700 | 339 | Dalrymple et al. 2006 |
| Ndebele | nbl | 3739520000 | 288 | Bosch et al. 2008a |
| Oshiwambo | kua | 2989782000 | 325 | Hurskainen and Halme 2001 |
| Rwanda | kin | 2496844000 | 349 | Muhirwe and Trosterud 2008, Muhirwe 2007 |
| Somali | som | 4050678000 | 277 | Abdillahi et al. 2006 |
| Sotho, Northern | nso | 23897870000 | 119 | Faaß et al. 2009, Prinsloo and Heid 2006. Prinsloo 1994 |
| Sotho, Southern | sot | 26107130000 | 111 | Johnson 2008, de Schryver and Pauw |
|  |  |  |  | 2007 |
| Swahili | swh | 424619270 | 777 | Hurskainen 1992, Pauw et al. 2006, |
|  |  |  |  | Pauw and de Schryver 2008 |
| Swati | SSW | 8473423400 | 196 | Bosch et al. 2008a |
| Tamajaq, Tawal- | ttq | 252591640 | 1001 | Enguehard and Modi 2009 |
| lammat |  |  |  |  |
| Tswana | tsn | 42204873500 | 80 | Groenewald 2009, Pretorius et al. 2009 |
| Xhosa | xho | 45530524000 | 77 | Bosch et al. 2008b, 2003, |
|  |  |  |  | Pretorius and Bosch 2009, Bosch et al. |
|  |  |  |  | 2008a |
| Yoruba | yor | 22304640000 | 125 | Finkel and Odejobi 2009 |
| Zulu | zul | 58707636000 | 64 | Bosch et al. 2008b, |
|  |  |  |  | Pretorius and Bosch 2003 |

Table 3. Low-affluence languages with CMR 1(4): Africa.

| Language | iso-639-3 | GLP | $\#$ | Publication(s) |
| :--- | ---: | ---: | ---: | :--- | :--- |
| American Sign Language | ase | 91596287 | 1636 | Shield and Baldridge 2008 |
| Aymara, Central | ayr | 4465996300 | 269 | Beeslev 2003 |
| Cayuga | cay | 2633490 | 4829 | Graham 2007 |
| Chuj, Ixtatán | cnm | 136579200 | 1357 | Medina Urrea and Díaz 2003 |
| Cree, Plains | crk | 1482847900 | 447 | Wolfart and Pardo 1979 |
| Inuktitut, Greenlandic | kal | 3296912000 | 311 | Trosterud 2008b |
| Inupiatun, North Alaskan | esi | 1720048230 | 416 | Trosterud 2008d |
| K'iche', West Central | qut | 661750000 | 633 | Kudlek 1975 |
| Mapudungun | arn | 2658600000 | 343 | Monson et al. 2008 |
| Tarahumara, Central | tar | 452045000 | 756 | Medina-Urrea 2006 |

Table 4. Low-affluence languages with CMR 2(4): Americas.

The extinct Ancient Greek, Latin, Syriac and Sanskrit serve as cultural heritage languages. If we count the people in these respective cultural sphere and estimate their purchasing powers, these languages too achieve considerable GLP.

Most remaining language with low (or even very low) GLP which nevertheless have CMR, i.e., Akkadian (extinct), Cayuga, American Sign Language, Chuj, Tarahumara, K'iche', Ha, A-Pucikwar and the small Uralic languages all appear to owe their CMR to a dedicated individual or group who "happen" to be interested in the language, for a variety of reasons independent of GLP. Such endeavors tend to be more distant from concrete usage with the speech community. For example, we find work here which was produced in past decades when the practical role of computational processing of language must have been rather opaque. Also, we find proof-of-concept descriptions of other aspects than morphology for this class of languages, e.g., Bender (2008). Except for continental biases, the selection of these languages versus the plethora of other languages of similar low GLP appears to be random. The continent bias is that the Americas are overrepresented, while, if anything, the Pacific region is underrepresented.

Swahili and Tamajaq also have low GLP, but Swahili has a high number of L2 speakers. Tamajaq, on the other hand, is a true example of a low-GLP language with CMR which is not due to an external dedicated individual.

As even with high-affluence languages, languages which are second to a dominant nation-state variety tend lag behind in attaining CMR, despite competitive GLP.

Among the remaining languages that have competitive GLP but lack CMR, the only real eye-raisers are the Nigerian languages Hausa and Igbo (but see Adegbola 2009).

### 5.2 Who creates CMR?

As noted above, a small number of CMR are the result of the entrepreneurship of a dedicated individual.

| Language | iso-639-3 | GLP | \# | Publication(s) |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Akkadian | akk | 0 | 6863 | Berthélemy | 1998, |
|  |  |  |  | Kataja and Koskenniemi 1988 |  |
| Assamese | asm | 16253429000 | 143 | Sharma et al. 2002 |  |
| A-Pucikwar | apq | 9730 | 6807 | Choudhary 2006 |  |
| Burmese | mya | 9296300000 | 185 | Htav and Murthy | 2008, |
|  |  |  |  | Maung and Mikami 2008 |  |
| Gujarati | guj | 44508492600 | 78 | Patel and Gali 2008 |  |
| Indonesian | ind | 42066000000 | 81 | Hammarström 2009, Adriani et al. |  |
|  |  |  |  | 2007, Pisceldo et al. | 2008, |
|  |  |  |  | Indradiaia and Bressan 2003 |  |
| Kannada | kan | 34346900000 | 91 | Vikram and Urs | 2007, |
|  |  |  |  | Sharada and Lakshmi 2006 |  |
| Lao | lao | 1864455000 | 402 | Berment 2004 |  |
| Malay | zlm | 82378737000 | 48 | Sankupellay and Valliappan | 2009 |
|  |  |  |  |  |  |
|  |  |  |  | Ahmad et al. 1996, Tai et al. | 2000, |
|  |  |  |  | Ranaivo-Malancon 2004 |  |
| Malayalam | mal | 34798470000 | 90 | Idicula and David 2007 |  |
| Meitei | mni | 1341941000 | 468 | Singh and Bandyopadhyay 2008, 2006, |  |
|  |  |  |  | Choudhury et al. 2004 |  |
| Marathi | mar | 66164000000 | 62 | Devlekar et al. 2006 |  |
| Mongolian, Halh | khk | 3121958000 | 321 | Khaltar and Fuiii 2008 |  |
| Oriya | ori | 30844100000 | 101 | Mohanty et al. 2005, Shabadi 2003 |  |
| Pashto, Northern | pbu | 12475810000 | 162 | Khan and Zuhra 2007 |  |
| Sanskrit | san | 2870350 | 4757 | Huet 2005, Bharati et al. | 2006, |
|  |  |  |  | Jha et al. 2006 |  |
| Sinhala | sin | 22257112950 | 126 | Herath et al. 1989 |  |
| Syriac | syc | 0 | 6863 | Kiraz 1998, 2001, 2000 |  |
| Tagalog | tgl | 32895000000 | 98 | Nelson 2004 |  |
| Tamil | tam | 79091044720 | 54 | Anandan et al. | 2002, |
|  |  |  |  | Viswanathan et al. 2003 |  |
| Telugu | tel | 67720800000 | 59 | Karthik Kumar et al. | 2006, |
|  |  |  |  | Rama Sree et al. 2008 |  |
| Thai | tha | 76275200000 | 55 | Tongchim et al. 2008 |  |
| Turkmen | tuk | 27251477160 | 109 | Tantuğ et al. 2006 |  |
| Uyghur | uig | 22699715500 | 122 | Ablimit et al. 2008 |  |
| Urdu | urd | 56428350000 | 68 | Humavoun et al. 2007, Hardie Bögel et al. 2008, Hussain 2008, | 2003 , |
|  |  |  |  |  | 2004, |
|  |  |  |  | Akram et al. 2009 |  |
| Vietnamese | vie | 54281199800 | 69 | Nguyen et al. 2008 |  |

Table 5. Low-affluence languages with CMR 3(4): Asia.

| Language | iso-639-3 | GLP | \# | Publication(s) |
| :---: | :---: | :---: | :---: | :---: |
| Basque | eus | 23697320000 | 120 | Alegria et al. 1996 |
| Bulgarian | bul | 47578541000 | 75 | Slavcheva 2003, Simov et al. 2004, <br> Nakov\| 2003, Angelov\| 2008 |
| Czech | ces | 158690740000 | 31 | Chrupała 2008, Schmid and Laws 2008 |
| Erzya | myv | 9088541500 | 187 | Prószéky and Novák 2005 |
| Estonian | est | 15691577000 | 146 | Uibo 2002, Kaalep and Vaino 2001, <br> Müürisep et al. 2003 |
| Faroese | fao | 2749328000 | 341 | Trosterud 2008a |
| Gaelic, Irish | gle | 20697310000 | 129 | $\begin{aligned} & \text { Uí Dhonnchadha et al. 2003, Sulger } \\ & 2008 \end{aligned}$ |
| Greek, Ancient | grc | 0 | 6863 | Lee 2008 |
| Khanty | kca | 201280000 | 1130 | Prószéky and Novák 2005 |
| Komi-Zyrian | kpv | 3211600000 | 317 | Prószéky and Novák 2005 |
| Icelandic | isl | 15235200000 | 148 | Loftsson 2008a, b |
| Latin | lat | 0 | 6863 | Forsberg 2007 |
| Latvian | lav | 16816220000 | 142 | Paikens 2008 |
| Lithuanian | lit | 31748960000 | 100 | Rimkutė et al. 2007 |
| Mansi | mns | 40700000 | 2336 | Prószéky and Novák 2005 |
| Nenets | yrk | 463240000 | 747 | Prószéky and Novák 2005 |
| Nganasan | nio | 7400000 | 3923 | Prószéky and Novák 2005 |
| Saami, North | sme | 1550092300 | 436 | Trosterud 2008d |
| Serbian | srp | 25004841100 | 115 | $\begin{aligned} & \text { Krstev et al. 2004, Kešelj and Šipka } \\ & 2008 \end{aligned}$ |
| Slovene | slv | 44161046190 | 79 | Eriavec and Džeroski 2004, Chrupała 2008, Haiic 2000 |
| Udmurt | udm | 6867200000 | 214 | Prószéky and Novák 2005 |
| Ukrainian | ukr | 96173972800 | 45 | Katrenko 2004, Kovalenko 2002 |
| Welsh | cym | 23340308000 | 121 | Chrupała 2008 |

Table 6. Low-affluence languages with CMR 4(4): Europe.

| Continent | $\#$ <br> with CMR | languages <br> languages <br> CMR | for <br> with | \# Languages | Average GLP |
| :--- | :--- | :--- | :--- | ---: | ---: |
|  |  | 13830066200.5 | 2169 | 499712661.1 |  |
| Africa | 21 | 1496900840.7 | 1187 | 272294046.4 |  |
| Americas | 10 | 32734534912.4 | 2320 | 1295239804.7 |  |
| Asia | 26 | 24682518995.0 | 258 | 6229757797.5 |  |
| Europe | 23 | - | 1380 | 31167413.1 |  |
| Oceania | 0 | 20834739866.5 | 7314 | 828867197.7 |  |

Table 7. Numbers of low-affluence languages with CMR per continent, along with continent totals.

Not one of the surveyed publications shows any sign of private sector involvement (though this does not preclude that the work described is made use of in the private sector after the publication). If private companies are interested in CMR for low-affluence languages, they do not publish about this.

The bulk of CMR work comes about through academic support in the respective nation state. Some or all authors of the published articles are either employed at universities in the corresponding nation state and/or acknowledge more specific funding initiatives to develop CMR.

Perhaps surprisingly, there is no Australian Aboriginal language represented in spite of their presence in a high-technological country where there is government support and revitalization efforts (Larkin 2005).

### 5.3 How are CMR created?

On one end of the spectrum, CMR consist of human-written rules in some formal framework. At the other end, unsupervised methods are used to induce CMR probabilistically from raw text data. A mid-way approach arranges the human to provide annotation of a certain amount of text, from which CMR is abstracted using supervised methods.

Another dimension of interest is that of transfer, i.e., if language A has CMR and language B is similar to A, then CMR for B are built from those of A. Transfer can occur with manually intensive methods, e.g., the source-code for morphological rules is taken over and is subjected to small adjustments, as well as in unsupervised methods, e.g., the same unsupervised method is applied to a new language with similar morphological typology.

Though we cannot go into detail, there is one clear division as to CMR for low-affluence languages, namely that the majority of CMR are human-written morphological rule systems, often in a finite-state framework. In later years, more supervised and unsupervised work has began to surface, probably boosted by increased availability of raw text data.

Relative to the number of opportunities, there is surprisingly little evidence of transfer, though this is visible among the Southern and Eastern Bantu languages, and presumably among the small Uralic languages. It appears to be lacking in such obvious pairs as Faroese-Icelandic, Malay-Indonesian, DutchAfrikaans and Lao-Thai. In fact, even for one and the same language, in the cases where we have different lines of work, they tend to be parallel rather than serial. There is insufficient information for a systematic analysis, but one may speculate that the lack of transfer has to do with access limitations to sourcecode and annotated corpora.

Put bluntly, one strategic lesson that emerges is that, sooner or later, GLPcompetitive languages will muster the institutional support for manual labourintensive CMR, and thus that unsupervised solutions have an edge on languages with lower GLP.

## 6 Conclusion

Analogous to the Gross National Product (GNP) of a country, one may define the Gross Language Product (GLP) of a language as the sum economic power of its speakers. Low-affluence languages are languages whose speakers muster a low GLP. Through an empirical survey of published work on Computational morphological resources (CMR), we can confirm the intuition that Computational morphological resources surface for languages with high GLP, except those high-GLP languages which are dominated by a related language in their respective nation-state. The rather obvious generalization that languages which are not even popularly written rarely attain CMR is also borne out. Also, a few "lucky" languages have CMR owing to the entrepreneurship of a dedicated individual. The manner in which GLP-competitive languages obtain their CMR is via state support through funded university positions and/or specific language technology development funding. Non-state-channelled driving forces, such as private sector, are not heard of in the survey. So far, most CMR for low-affluence languages has been manually built rule systems but the field is open also for supervised and unsupervised statistical approaches.

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## Chapter III Morphological Lexicon Extraction from Raw Text Data

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# Morphological Lexicon Extraction from Raw Text Data 

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#### Abstract

We introduce a tool extract developed for automatic extraction of lemma-paradigm pairs from raw text data. The tool combines regular expressions containing variables with propositional logic to form search patterns which identify lemmas tagged with their paradigm class. Furthermore, we describe the underlying algorithm of the tool and suggest a method for developing a morphological lexicon.

The tool was primarily developed for morphologies defined in the tool Functional Morphology (Forsberg and Ranta 2004), but it is usable for all similar systems that implement a word-and-paradigm description of a morphology.

We demonstrate the usefulness of the tool with a case study on the Canadian Hansards Corpus of French. The result is evaluated in terms of precision of the extracted lemmas and statistics on coverage and rule productiveness. Competitive extraction figures show that human-written rules in a tailored tool is a relatively time-efficient approach to the task at hand.


## 1 Introduction

A wide-coverage morphological lexicon is a key part of any information retrieval system, machine translation engine and of a variety of other Natural Language Processing applications. The demand is high not only for low-density languages, since existing lexica for major languages are often not publicly available. Moreover, even if they were, running text - especially newspaper and technical texts - will always contain out-of-lexicon words.

Manual development of a full-scale lexicon is a time-consuming task, so it is natural to investigate how the lexicon development can be automated. The situation is usually such that access to large collections of raw language data is
cheap, so cheap that it is tempting to look at ways to exploit the raw data to obtain the sought after high-quality morphological lexicon. Clearly, attempts to fully automatize the process (e.g (Creutz and Lagus 2005, Sharma et al. 2002) - most other systems for unsupervised learning of morphology cannot be used directly to build a lexicon) do not reach the kind of quality we are generally interested in. However, instead of using humans for supervised learning of lexicon extraction in some form, we believe there is a more advantageous placement of the human role. With a suitable tool, humans can use their knowledge to guide a computerized extraction from raw text, with comparatively little time spent. To be more specific, we intend to show that a profitable role for the human is to write intelligent extraction rules, given that there is a sufficiently flexible environment.

The extract tool has been developed with this in mind. The idea behind extract is simple: start with a large-sized corpus and a description of the word forms in the paradigms with the varying parts, which we refer to as technical stems, represented with variables. In the tool's syntax, we could describe the first declension noun of Swedish with the following definition.

```
paradigm decl1 =
    x+"a"
    { x+"a" & x+"as" & x+"an" & x+"ans" &
        x+"or" & x+"ors" & x+"orna & x+"ornas" } ;
```

Given that all forms in the curly brackets, called the constraint, are found for some prefix x , the tool outputs the head $\mathrm{x}+$ "a" tagged with the name of the paradigm. E.g., if these forms exist in the text data: ärta, ärtas, ärtan, ärtans, ärtor, ärtors, ärtorna and ärtornas, the tool will output decl1 ärta. Given that we have the lemma and the paradigm class, it is a relatively simple task to generate all word forms.

The paradigm definition has a major drawback: very few lemmas appear in all word forms. It could in fact be relaxed to increase recall without sacrificing precision: to identify a Swedish word as a noun of the first declension it is often enough to find one instance of the four singular forms and one of the four plural forms. The tool offers a solution by supporting propositional logic in the constraint, further described in section 2.1. Various issues of the extraction process are discussed in section 3 .

Another problem with the given definition is the lack of control over what the variable x might be. Section 2.2 describes how the tool improves this situation by allowing variables to be associated with regular expressions.

The stems of first declension nouns in Swedish are the same for all word forms, but this is not the case for many paradigms, e.g. German nouns with umlaut. Section 2.3 presents the tool's use of multiple variables as a solution to this problem.

$$
\begin{array}{rlll}
\langle\text { Def }\rangle::= & \text { paradigm } & \begin{array}{l}
\langle\text { Name }\rangle\langle\text { VarDef }\rangle= \\
\\
\\
\end{array} \quad \begin{array}{l}
\text { Head }\rangle\{\langle\text { Logic }\rangle\}
\end{array} \\
\mid & \text { regexp } & \langle\text { Name }\rangle=\langle\text { Reg }\rangle
\end{array}
$$

Figure 1. Regexp and paradigm definitions

```
LLogic\rangle ::= \langleLogic \rangle&\langleLogic > ~ <Logic \rangle
    | <logic\rangle|\langleLogic \rangle}\langle<\mathrm{ Pattern }
```

Figure 2. Propositional logic grammar

## 2 Paradigm File Format

A paradigm file consists of two kinds of definitions: regexp and paradigm, in figure 1

A regexp definition associates a name (Name) with a regular expression (Reg). A paradigm definition consists of a name (Name), a set of variableregular expression associations (VarDef), a set of output constituents (Head) and constraint (Logic).

The basic unit in Head and Logic is a pattern that describes a word form. A pattern consists of a sequence of variables and string literals glued together with the ' + ' operator. An example of a pattern given previously was x+"a".

Both definitions will be discussed in detail in the following sections.

### 2.1 Propositional Logic

Propositional logic appears in the constraint to enable a more fine-grained description of what word forms the tool should look for. The basic unit is a pattern, corresponding to a word form, which is combined with the operators \& (and), । (or), and ~ (not).

The syntax for propositional logic is given in figure 2, where Pattern refers to one word form.

The addition of new operators allow the paradigm in section 1 to be rewritten with disjunction to reflect that it is sufficient to find one singular and one plural word form.

```
paradigm decl1 =
    x+"a"
    { (x+"a" | x+"as" | x+"an" | x+"ans") &
        (x+"or" | x+"ors" |x+"orna | x+"ornas") } ;
```


### 2.2 Regular Expressions

It was mentioned in section 1 that control over the variable part of a paradigm description was desired. The solution provided by the tool is to enable the user

| $\langle R e g\rangle$ | ::= | $\begin{aligned} & \langle\operatorname{Reg}\rangle\|\langle\operatorname{Reg}\rangle\| \\ & \langle\operatorname{Reg}\rangle-\langle\operatorname{Reg}\rangle \\ & \langle\operatorname{Reg}\rangle\langle\operatorname{Reg}\rangle \\ & \langle\operatorname{Reg}\rangle * \\ & \langle\operatorname{Reg}\rangle+ \\ & \langle\operatorname{Reg}\rangle ? \\ & \mathrm{eps} \\ & \langle\text { Char }\rangle \end{aligned}$ | digit <br> letter <br> upper <br> lower <br> char <br> $\langle$ String $\rangle$ <br> ( $\langle\operatorname{Reg}\rangle$ ) |
| :---: | :---: | :---: | :---: |

Figure 3. Regular expression
to associate every variable with a regular expression. The association dictates which (sub-)strings a variable can match. An unannotated variable can match any string, i.e. its regular expression is Kleene star over any symbol.

As a simple example, consider German, where nouns always start with an uppercase letter. This can be expressed as follows.

```
regexp UpperWord = upper letter*;
paradigm n [x:UpperWord] = ... ;
```

The syntax of the tool's regular expressions is given in figure 3, with the normal connectives: union, concatenation, set minus, Kleene star, Kleene plus and optionality. eps refers to the empty string, digit to $0-9$, letter to an alphabetic character, lower and upper to a lowercase respectively an uppercase letter. char refers to any character. A regular expression can also contain a double-quoted string, which is interpreted as the concatenation of the characters in the string.

### 2.3 Multiple Variables

Not all paradigm definitions are as neat as the initial example - phenomena like umlaut require an increased control over the variable part. The solution the tool provides is to allow multiple variables, i.e. a pattern may contain more than one variable. This is best explained with an example, where two German noun paradigms are described, both with umlaut. The change of the stem vowel is captured by introducing two variables and by letting the stem vowel be a constant string.

```
regexp Consonant = ... ;
regexp Pre = upper letter*;
regexp Aft = Consonant+ ;
paradigm n2 [F:Pre, ll:Aft] =
    F+"a"+ll
        { F+"a"+ll & F+"ä"+ll+"e" } ;
```

```
paradigm n3 [W:Pre, rt:Aft] =
    W+"o"+rt
        { W+"o"+rt & W+"ö"+rt+"er" } ;
```

The use of variables may reduce the time-performance of the tool, since every possible variable binding is considered. The use of multiple variables should be moderate, and the variables should be restricted as much as possible by their regular expression association to reduce the search space.

A variable does not need to occur in every pattern, but the tool only performs an initial match with patterns containing all variables. The reason for this is efficiency - the tool only considers one word at the time, and if the word matches one of the patterns, it searches for all other patterns with the variables instantiated by the initial match. For obvious reasons, an initial match is never performed under a negation, since this would imply that the tool searches for something it does not want to find.

It is allowed to have repeated variables, i.e. non-linear patterns, which is equivalent to back reference in the programming language Perl. An example where a sequence of bits is reduplicated is given. This language is known to be non-context-free (Hopcroft and Ullman 2001).

```
regexp ABs = (0|1)*;
paradigm reduplication [x:ABs] =
    x+x { x+x } ;
```


### 2.4 Multiple Arguments

The head of a paradigm definition may have multiple arguments to support more abstract paradigms. An example is Swedish nouns, where many nouns can be correctly classified by just detecting the word forms in nominative singular and nominative plural. An example is given below, where the first and second declension is handled with the same paradigm function, where the head consists of two output forms. The constraints are omitted.

```
paradigm regNoun = paradigm regNoun =
flick+"a" flick+"or" pojk+"e" pojk+"ar"
{...} ;
{...} ;
```


### 2.5 The Algorithm

The underlying algorithm of the tool is presented in pseudo-code notation.

```
let L be the empty lexicon.
let P be the set of extraction paradigms.
let W be all word types in the corpus.
for each w : W
    for each p : P
        for each constraint C with which w matches p
```

```
if W satisfies C with the result H,
    add H to L
```

The algorithm is initialized by reading the word types of the corpus into an array $W$. A word $w$ matches a paradigm $p$, if it can match any of the patterns in the paradigm's constraint that contains all variables occurring in the constraint. The result of a successful match is an instantiated constraint $C$, i.e. a logical formula with words as atomic propositions. The corpus $W$ satisfies a constraint $C$ if the formula is true, where the truth of an atomic proposition $a$ means that the word $a$ occurs in $W$.

### 2.6 The Performance of the Tool

The extraction tool is implemented in Haskell. It is available as an open-source free software. A typical example of using the tool, the experiment reported in Section 4 extracted a lexicon of 19,295 lemmas from a corpus of 66,853 word types, by using 43 paradigms. The execution time was 22 min 36 s on a laptop running Mandrake Linux 9.2 with a 1.4 GHz Pentium M. The memory consumption was 46 MB .

## 3 The Art of Extraction

The constraint of a paradigm describes a sub-paradigm, a subset of the word forms, considered to be evidence enough to be able to judge that the lemmas in the head are in that paradigm class. The identification of appropriate subparadigms requires good insights into the target language and intuitions about the distributions of the word forms. However, these insights and intuitions may be acquired while using the tool by trial and error.

Lexicon extraction is a balance between precision, i.e. the percentage of the extracted lemmas that are correctly classified, and recall, i.e. the percentage of the lemmas in the text data that are extracted. Precision, however, is by far the most important, since poor recall can be compensated with more text data, but poor precision requires more human labor.

How about extracting the paradigm descriptions from a set of paradigms automatically? We use the term minimum-size sub-paradigm to describe the minimum-sized set of word forms needed to uniquely identify a paradigm $P$. More formally, a minimum-sized sub-paradigm is a minimum-size set of word forms $P^{\prime} \subseteq P$ such that for any other paradigm $Q, P^{\prime} \nsubseteq Q$. It turns out that the problem of finding the minimum-size sub-paradigm for a paradigm $P$ is NP-complete (proof in section 3.1), and thus has a theoretical worst-case complexity exponential in $|P|$. Therefore there is all the more reason to let a human choose which forms to require and also weigh in which forms are likely to be common/uncommon in actual usage.

Also, some natural languages have overshadowed paradigms, i.e. paradigms where the form of one paradigm is a subset of another paradigm. For example, in Latin some noun paradigms are overshadowed by adjective paradigms.

The distinction of Latin nouns and adjectives can be done through the use of negation where a second declension noun paradigm is defined by also stating that the feminine endings, which would indicate that it is an adjective, should not be present. If the set of word forms are equal then there is no way to distinguish the words morphologically.

```
paradigm decl2servus =
    serv++"us"
    { serv+"us" & serv+"i" &
        ~(serv+"a" | serv+"ae")};
```

Negation is similar with negation as failure in Prolog, with the same problems associated with it. The main problem is that negation rests on the absence, not the presence, of information, which in turn means that the extraction process with negation is non-monotonic: the use of a larger corpus may lead to an extracted lexicon which is smaller. A worst-case scenario is a misspelt or foreign word that, by negation, removes large parts of the correctly classified lemmas in the extracted lexicon.

In most cases, a better alternative to negation is a more careful use of regular expressions, and in the case of Latin nouns, a rudimentary POS tagger that resolves the POS ambiguity may outperform negation.

### 3.1 Sub-Paradigm Problem is NP Complete

The minimum-size sub-paradigm problem (MSS) is equivalent to the well-known set-cover problem (Garey and Johnson 1979). We repeat the problem definitions for clarity:

SET-COVER: Input: a collection of sets $C=C_{1}, \ldots, C_{n}$ all being subsets of some universe $U=\{1, \ldots, k\}$ with $\bigcup C=U$. Goal: Find a minimum-size subcollection $C^{\prime} \subseteq C$ such that $\bigcup C^{\prime}=U$.

MSS: Input: A paradigm (set) $P$ and a collection of sets $P_{1}, \ldots, P_{m}$ with $P \nsubseteq P_{j}$ for any $j$. Goal: Find a minimum-size $P^{\prime} \subseteq P$ such that $P^{\prime} \nsubseteq P_{j}$ for any $j$.

The following polynomial transformations translate between the two problems:

- To solve SET-COVER with MSS: Let $P=U$ and $P_{j}=\left\{i \mid j \notin C_{i}\right\}$ for $j \in P$. An output $P^{\prime}$ gives a minimum-size cover $C^{\prime}=\left\{C_{i} \mid i \in P^{\prime}\right\}$.
- To solve MSS with SET-COVER: Let $C_{i}=\left\{j \mid i \notin P_{j}\right\}$ for all $i \in P$. An output $C^{\prime}$ gives a minium-size sub-paradigm $P^{\prime}=\left\{i \mid C_{i} \in C^{\prime}\right\}$.

It is instructive to model the problem(s) in terms of a matrix. Rows represent elements and columns stand for sets of these elements. We put a plus at $(x, y)$ if element $x$ in contained in the set at $y$ and a minus otherwise. Now we can think of set-cover as a selection of as few columns as possible such that there

|  | $P_{1}$ | $P_{2}$ |
| :---: | :---: | :---: |
| 1 | + | - |
| 2 | - | + |
| 3 | - | - |


|  | 1 | 2 | 3 |
| :---: | :---: | :---: | :---: |
| $P_{1}$ | - | + | + |
| $P_{2}$ | + | - | + |

Figure 4. Example correspondence between MSS and SET-COVER.
is a plus in every row in at least one of the selected columns. Likewise, the sub-paradigm problem as selection of as few rows as possible such that there is a minus in every column in at least one of the selected rows.

To see what is going on, consider the following example: Let $P=\{1,2,3\}$, $P_{1}=\{1\}$ and $P_{2}=\{2\}$. Clearly, $P^{\prime}=\{3\}$ is the minimal solution. The corresponding matrix is given to the left in figure 4. Intuitively, selecting e.g 1 for our $P^{\prime}$ means that we can assure $P^{\prime} \not \subset P_{2}$. Selecting e.g 3 for our $P^{\prime}$ means that we can assure both $P^{\prime} \not \subset P_{2}$ and $P^{\prime} \not \subset P_{2}$. Since selecting 3 covers every column with a minus, we are finished.

The transformations simply rotate the matrix and exchange the minus and plus:es. Thus, the corresponding set-cover instance is shown to the right in figure 4. and easily gives $C^{\prime}=\{3\}$ as the minimal collection (from $C=\{1,2,3\}$ ).

### 3.2 Manual Verification

Almost all corpora have misspellings which may lead to false conclusions. Added to that are word forms that incidentally coincide. One possible solution to handle misspellings is to only consider words that occur at some frequency. However, that would remove a lot of unusual but correctly spelled words (to an extent which is unacceptable).

Misspellings, foreign words and coincidences are the main reason why manual verification of the extracted lexicon cannot be circumvented even with "perfect" paradigm definitions. However, browse-filtering a high-precision extracted lexicon requires much less time than building the same lexicon by hand. Also, nothing in principle prohibits statistical techniques to be applied in collaboration here. For instance, one can sort the extracted lemmas heuristically according to how many forms and with what frequencies they occur (cf. section 5). In general, this is productive for poly-occurring lemmas but helps little for the (typically many) hapax lemmas.

## 4 Experiments

We will evaluate our proposed extraction technique with a study of real-world extraction on the Hansards corpus of Canadian French (Germann 2003). All words were manually annotated to enable a thorough evaluation. However, the intended practical usage of the extraction tool is to simply eye-browse the output list for erroneous extractions.

| Tokens | 15000000 |
| :--- | ---: |
| Types | 66853 |
| Non-junk types | 49477 |
| Lemmas | 27681 |

Figure 5. Statistics on the corpus of Canadian French Hansards used in the experiment

The corpus consisted of approximately 15 million running tokens of 66853 types. From these 66853 types we manually removed all junk - foreign words, proper names, misspellings, numeric expressions, abbreviations as well as pronouns, prepositions, interjections and non-derived adverbs - so that a 49477 true lexical items remained. 27681 lemmas account for the 49477 forms, where verb-lemmas tended to occur in more forms than noun- and adjective-lemmas. Of course, not all these lemmas occurred in such forms that their morphological class could be recognized by their endings alone. Many lemmas occur in only one form - usually not enough to infer its morphological class - unless, as is often the case, they contain a derivational morpheme which, together with its inflectional ending, does suffice. For example, a single occurrence of a word ending in $-e$ is hardly conclusive, whereas one ending in -tude is almost certainly a feminine noun with a plural in $-s$. Nouns without derivational ending cannot be reliably distinguished from adjectives even when they occur in all their forms, i.e both the singular and plural. The table in figure 5 summarizes these data.

We now turn to the question of precision and coverage of rule-extraction of the targeted 27681 lemmas. We quickly devised a set of 43 rules to extract French nouns (18 rules), verbs ( 7 rules) and adjectives (18 rules). The verbrules aimed at -ir and -er verbs by requiring salient forms for these paradigms, whereas the noun- and adjective rules make heavy use of regularities in derivational morphology to overcome the problems of overlapping forms. Two typical example groups are given below:

```
regexp NOTi = char* (char-"i") ;
paradigm Ver [regard:NOTi]
    = regard+"er"
        {regard+"e" &
            (regard+"é" | regard+"ée" |
            regard+"ez" | regard+"ont" |
            regard+"ons" | regard+"a" )} ;
    paradigm Aif
    = sport+"if"
        {sport+"if" | sport+"ifs" |
            sport+"ive" | sport+"ives"} ;
```

The results of the extraction are shown in figure 6. If possible, one would like to know where one's false positives come from - sloppy rules or noisy data?

|  | Extr. All | Extr. Non-Junk |
| :--- | ---: | ---: |
| False Positives | 2031 | 664 |
| Correctly Indentified | 17264 | 17264 |
|  | 19295 | 17928 |
| Precision | $89.5 \%$ | $96.3 \%$ |

Figure 6. Extraction results on raw text vs. text with junk removed first.

At least one would like to know roughly what to expect. Since we have already annotated this corpus we can give some indicative quantitative data. To assess the impact of misspellings and foreign words - the two main sources for spurious extractions - we show the results of the same extraction performed on the corpus with all junk removed beforehand. As expected, false positives increase when junk is added. To be more precise, we get a lot of spurious verbs from English words and proper names in -er (e.g farmer, worchester) as well as many nouns, whose identification requires only one form, from misspellings (e.g qestion). Non-junk-related cases of confusion worth mentioning are nouns in -ment the same ending as adverbs - and verbs which have spelling changes (mangermangeait, appeler-appelle etc).

The rule productiveness, i.e a rule on average catches $17264 / 43 \approx 401$, must be considered very high. As for coverage, we can see that our rules catch the lions share of the available lemmas, 17264 out of 27681 (again, not all of which occur in enough forms to predict their morphological class), in the corpus. This is relevant because even if we can always find more raw text cheaply, we want our rules to make maximal use of whatever is available and more raw data is of little help unless we can actually extract a lot of them with reasonable effort. It is also relevant because a precision figure without a recall figure means nothing. It would be easy to tailor 43 rules to perfect precision, perhaps catching one lemma per rule, so what we show is that precision and rule productiveness can be simuntaneously high. In general it is of course up to the user how much of the raw-data lemmas to sacrifice for precision and rule-writing effort, which are usually more important objectives.

## 5 Related Work

The most important work dealing with the very same problem addressed here, i.e extracting a morphological lexicon given a morphological description, is the study of the acquisition of French verbs and adjectives in (Clément et al. 2004). Likewise, they start from an existing inflection engine and exploit the fact that a new lemma can be inferred with high probability if it occurs in raw text in predictable morphological form(s). Their algorithm ranks hypothetical lemmas based on the frequency of occurrence of its (hypothetical) forms as well as part-of-speech information signalled from surrounding closed-class words. They do not make use of human-written rules but reserve an unclear, yet crucial, role
for the human to hand-validate parts of output and then let the algorithm reiterate. Given the many differences, the results cannot be compared directly to ours but rather illustrate a complementary technique.

Tested on Russian and Croat, (Oliver and Tadić 2004, Oliver 2004:Ch. 3) describe a lexicon extraction strategy very similar to ours. In contrast to humanmade rules, they have rules extracted from an existing (part of) a morphological lexicon and use the number of inflected forms found to heuristically choose between multiple lemma-generating rules (additionally also querying the Internet for existence of forms). The resulting rules appear not at all as sharp as handmade rules with built-in human knowledge of the paradigms involved and their respective frequency (the latter being crucial for recall). Also, in comparison, our search engine is much more powerful and allows for greater flexibility and user convenience.

For the low-density language Assamese, (Sharma et al. 2002) report an experiment to induce both morphology and a morphological lexicon at the same time. Their method is based on segmentation and alignment using string counts only - involving no human annotation or intervention inside the algorithm. It is difficult to assess the strength of their acquired lexicon as it is intertwined with induction of the morphology itself. We feel that inducing morphology and extracting a morphological lexicon should be performed and evaluated separately.

There is a body of work on inducing verb subcategorization information from raw or tagged text (see Kermanidis et al. (2004), Faure and Nédelled (1998), Gamallo et al. (2003) and references therein). However, the parallel between subcategorization frame and morphological class is only lax. The latter is a simple mapping from word forms to a paradigm membership, whereas in verb subcategorization one also has the onus discerning which parts of a sentence are relevant to a certain verb. Moreover, it is far from clear that verb subcategorization comes in well-defined paradigms - instead the goal may be to reduce the amount of parse trees in a parser that uses the extracted subcategorization constraints.

## 6 Conclusions and Further Work

We have shown that building a morphological lexicon requires relatively little human work. Given a morphological description, typically an inflection engine and a description of the closed word classes, such as pronouns and prepositions, and access to raw text data, a human with knowledge of the language can use a simple but versatile tool that exploits word forms alone. It remains to be seen to what extent syntactic information, e.g part-of-speech information, can further enhance the performance. A more open question is whether the suggested approach can be generalized to collect linguistic information of other kinds than morphology, such as e.g verb subcategorization frames.

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# Chapter IV ${ }^{\text {Automatic Annotation of }}$ Bibliographical References with Target Language 

Hammarström, H. (2008). Automatic annotation of bibliographical references with target language. In Proceedings of MMIES-2: Wokshop on Multi-source, Multilingual Information Extraction and Summarization, pages 57-64. ACL.

# Automatic Annotation of Bibliographical References with Target Language 

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#### Abstract

In a large-scale project to list bibliographical references to all of the ca 7000 languages of the world, the need arises to automatically annotate the bibliographical entries with ISO-639-3 language identifiers. The task can be seen as a special case of a more general Information Extraction problem: to classify short text snippets in various languages into a large number of classes. We will explore supervised and unsupervised approaches motivated by distributional characterists of the specific domain and availability of data sets. In all cases, we make use of a database with language names and identifiers. The suggested methods are rigorously evaluated on a fresh representative data set.


## 1 Introduction

There are about 7000 languages in the world (Hammarström 2008) and there is a quite accurate database of which they are (Gordon 2005). Language description, i.e., producing a phonological description, grammatical description, wordlist, dictionary, text collection or the like, of these 7000 languages has been on-going on a larger scale since about 200 years. This process is fully de-centralized, and at present there is no database over which languages of the world have been described, which have not, and which have partial descriptions already produced (Hammarström 2007b). We are conducting a large-scale project of listing all published descriptive work on the languages of the world, especially lesser-known languages. In this project, the following problem naturally arises:

Given: A database of the world's languages (consisting minimally of <uniqueid, language-name>-pairs)

Input: A bibliographical reference to a work with descriptive language data of (at least one of) the language(s) in the database

Desired output: The identification of which language(s) is described in the bibliographical reference

We would like to achieve this with as little human labour as possible. In particular, this means that thresholds that are to be set by humans are to be avoided. However, we will allow (and do make use of - see below) supervision in the form of databases of language references annotated with target language as long as they are freely available.

As an example, say that we are given a bibliographical reference to a descriptive work as follows:

Dammann, Ernst 1957 Studien zum Kwangali: Grammatik, Texte, Glossar, Hamburg: Cram, de Gruyter \& Co. [Abhandlungen aus dem Gebiet der Auslandskunde / Reihe B, Völkerkunde, Kulturgeschichte und Sprachen 35]

This reference happens to describe a Namibian-Angolan language called Kwangali [kwn]. The task is to automatically infer this, for an arbitrary bibliographical entry in an arbitrary language, using the database of the world's languages and/or databases of annotated entries, but without humanly tuned thresholds. (We will assume that the bibliographical entry comes segmented into fields, at least as to the title, though this does not matter much.)

Unfortunately, the problem is not simply that of a clean database lookup. As shall be seen, the distributional characteristics of the world language database and input data give rise to a special case of a more general Information Extraction (IE) problem. To be more precise, an abstract IE problem may be defined as follows:

- There is a set of natural language objects $O$
- There is a fixed set of categories $C$
- Each object in $O$ belong to zero or more categories, i.e., there is a function $C: O \rightarrow \operatorname{Powerset}(C)$
- The task is to find classification function $f$ that mimics $C$.

The special case we are considering here is such that:

- Each object in $O$ contains a small amount of text, on the order of 100 words
- The language of objects in $O$ varies across objects, i.e., not all objects are written in the same language
- $|C|$ is large, i.e., there are many classes (about 7000 in our case)
- $|C(o)|$ is small for most objects $o \in O$, i.e., most objects belong to very few categories (typically exactly one category)
- Most objects $o \in O$ contain a few tokens that near-uniquely identifies $C(o)$, i.e., there are some words that are very informative as to category, while the majority of tokens are very little informative. (This characteristic excludes the logical possibility that each token is fairly informative, and that the tokens together, on an equal footing, serve to pinpoint category.)

We will explore and compare ways to exploit these skewed distributional properties for more informed database lookups, applied and evaluated on the outlined reference-annotation problem.

## 2 Data and Specifics

The exact nature of the data at hand is felt to be quite important for design choices in our proposed algorithm, and is assumed to be unfamiliar to most readers, wherefore we go through it in some detail here.

### 2.1 World Language Database

The Ethnologue (Gordon 2005) is a database that aims to catalogue all the known living languages of the world 11 As far as language inventory goes, the database is near perfect and language/dialect divisions are generally accurate, though this issue is thornier (Hammarström 2005).

Each language is given a unique three-letter identifier, a canonical name and a set of variant and/or dialect names ${ }^{2}$ The three-letter codes are draft ISO-639-3 standard. This database is freely downloadable 3 . For example, the entry for Kwangali [kwn] contains the following information:

Canonical name: Kwangali<br>ISO 639-3: kwn<br>Alternative names 4 : \{Kwangali, Shisambyu, Cuangar, Sambio, Kwan-<br>gari, Kwangare, Sambyu, Sikwangali, Sambiu, Kwangali, Rukwangali\}.

The database contains 7299 languages (thus 7299 unique id:s) and a total of 42768 name tokens. Below are some important characteristics of these collections:
${ }^{1}$ It also contains some sign languages and some extinct attested languages, but it does not aim or claim to be complete for extinct and signed languages.
${ }^{2}$ Further information is also given, such as number of speakers and existence of a bible translation is also given, but is of no concern for the present purposes.
${ }^{3}$ From http://www.sil.org/iso639-3/download. asp accessed 20 Oct 2007.
4 The database actually makes a difference between dialect names and other variant names. In this case Sikwangali, Rukwangali, Kwangari, Kwangare are altername names denoting Kwangali, while Sambyu is the name of a specific dialect and Shisambyu, Sambiu, Sambio are variants of Sambyu. We will not make use of the distinction between a dialect name and some other alternative name.

- Neither the canonical names nor the alternative names are guaranteed to be unique (to one language). There are 39419 unique name strings (but 42 768 name tokens in the database!). Thus the average number of different languages (= unique id:s) a name denotes is 1.08 , the median is 1 and the maximum is 14 (for Miao).
- The average number of names (including the canonical name) of a language is 5.86 , the median is 4 , and the maximum is 77 (for Armenian [hye]).
- It is not yet well-understood how complete database of alternative names is. In the preparation of the test set (see Section (2.4) an attempt to estimate this was made, yielding the following results. 100 randomly chosen bibliographical entries contained 104 language names in the title. 43 of these names ( $41.3 \%$ ) existed in the database as written. 66 ( $63.5 \%$ ) existed in the database allowing for variation in spelling (cf. Section 1). A more interesting test, which could not be carried out for practical reasons, would be to look at a language and gather all publications relating to that language, and collect the names occurring in titles of these. (To collect the full range of names denoting languages used in the bodies of such publications is probably not a well-defined task.) The Ethnologue itself does not systematically contain bibliographical references, so it is not possible to deduce from where/how the database of alternative names was constructed.
- A rough indication of the ratio between spelling variants versus alternative roots among alternative names is as follows. For each of the 7299 sets of alternative names, we conflate the names which have an edit distanc $5^{5}$ of $\leq i$ for $i=0, \ldots, 4$. The mean, median and max number of names after conflating is shown below. What this means is that languages in the database have about 3 names on average and another 3 spelling variants on average.

| $i$ | Mean | Median | Max | Entry |
| :---: | :---: | :---: | :---: | :---: |
| 0 | 5.86 | 4 | 77 | 'hye' |
| 1 | 4.80 | 3 | 65 | 'hye' |
| 2 | 4.07 | 3 | 56 | 'eng' |
| 3 | 3.41 | 2 | 54 | 'eng' |
| 4 | 2.70 | 2 | 47 | 'eng' |

### 2.2 Bibliographical Data

Descriptive data on the languages of the world are found in books, $\mathrm{PhD} / \mathrm{MA}$ theses, journal articles, conference articles, articles in collections and manuscripts. If only a small number of languages is covered in one publication, the title usually carries sufficient information for an experienced human to deduce which language(s) is covered. On the other hand, if a larger number of languages is

[^14]targeted, the title usually only contains approximate information as to the covered languages, e.g., Talen en dialecten van Nederlands Nieuw-Guinea or West African Language Data Sheets. The (meta-)language [as opposed to target language] of descriptive works varies (cf. Section 2.4).

### 2.3 Free Annotated Databases

Training of a classifier ('language annotator') in a supervised framework, requires a set of annotated entries with a distribution similar to the set of entries to be annotated. We know of only two such databases which can be freely accessed ${ }^{6}$; WALS and the library catalogue of MPI/EVA in Leipzig.

WALS: The bibliography for the World Atlas of Language Structures book can now be accessed online (http://www.wals.info/). This database contains 5633 entries annotated to 2053 different languages.

MPI/EVA: The library catalogue for the library of the Max Planck Institute for Evolution Anthropology (http://biblio.eva.mpg.de/) is queryable online. In May 2006 it contained 7266 entries annotated to 2246 different languages.

Neither database is free from errors, imprecisions and inconsistencies (impressionistically $5 \%$ of the entries contain such errors). Nevertheless, for training and development, we used both databases put together. The two databases put together, duplicates removed, contain 8584 entries annotated to 2799 different languages.

### 2.4 Test Data

In a large-scale on-going project, we are trying to collect all references to descriptive work for lesser-known languages. This is done by tediously going through handbooks, overviews and bibliographical for all parts of the world alike. In this bibliography, the (meta-)language of descriptive data is be English, German, French, Spanish, Portuguese, Russian, Dutch, Italian, Chinese, Indonesian, Thai, Turkish, Persian, Arabic, Urdu, Nepali, Hindi, Georgian, Japanese, Swedish, Norwegian, Danish, Finnish and Bulgarian (in decreasing order of incidence $)^{7}$. Currently it contains 11788 entries. It is this database that needs to be annotated as to target language. The overlap with the joint WALS-MPI/EVA

[^15]database is 3984 entries 8 Thus $11788-3984=7804$ entries remain to be annotated. From these 7804 entries, 100 were randomly selected and humanly annotated to form a test set. This test set was not used in the development at all, and was kept totally fresh for the final tests.

## 3 Experiments

We conducted experiments with three different methods, plus the enhancement of spelling variation on top of each one.

Naive Lookup: Each word in the title is looked up as a possible language name in the world language database and the output is the union of all answers to the look-ups.

Term Weight Lookup: Each word is given a weight according to the number of unique-id:s it is associated with in the training data. Based on these weights, the words of the title are split into two groups; informative and non-informative words. The output is the union of the look-up:s of the informative words in the world language database.

Term Weight Lookup with Group Disambiguation: As above, except that names of genealogical (sub-)groups and country names that occur in the title are used for narrowing down the result.

Following a subsection on terminology and definitions, these will be presented in increasing order of sophistication.

### 3.1 Terminology and Definitions

- $C$ : The set of 7299 unique three-letter language id:s
- $N$ : The set of 39419 language name strings in the Ethnologue (as above)
- $C(c)$ : The set of names $\subseteq N$ associated with the code $c \in C$ in the Ethnologue database (as above)
- $L N(w)=\{i d \mid w \in C(i d), i d \in C\}$ : The set of id:s $\subseteq C$ that have $w$ as one of its names
- $C_{S}(c)=\cup_{w i n C(c)}$ Spellings $(w)$ : The set of variant spellings of the set of names $\subseteq N$ associated with the code $c \in C$ in the Ethnologye database. For reference, the Spelling $(w)$-function is defined in detail in Table 1.

[^16]- $L N_{S}(w)=\left\{i d \mid w \in C_{S}(i d), i d \in C\right\}$ : The set of id:s $\subseteq C$ that have $w$ as a possible spelling of one of its names
- WE: The set of entries in the joint WALS-MPI/EVA database (as above). Each entry $e$ has a title $e_{t}$ and a set $e_{c}$ of language id:s $\subseteq C$
- $W \operatorname{ords}\left(e_{t}\right)$ : The set of words, everything lowercased and interpunctation removed, in the title $e_{t}$
- $L W E N(w)=\left\{i d \mid e \in W E, w \in e_{t}, i d \in e_{c}\right\}$ : The set of codes associated with the entries whose titles contain the word $w$
- $T D(w)=L N(w) \cup L W E N(w)$ : The set of codes tied to the word $w$ either as a language name or as a word that occurs in a title of an code-tagged entry (in fact, an Ethnologue entry can be seen as a special kind of bibliographical entry, with a title consisting of alternative names annotated with exactly one category)
- $T D_{S}(w)=L N_{S}(w) \cup L W E N(w)$ : The set of codes tied to the word $w$ either as a (variant spelling of a) language name or as a word that occurs in a title of an code-tagged entry
- $W C(w)=|T D(w)|$ : The number of different codes associated with the word $w$
- $W I(w)=\left|\left\{e_{t} \mid w \in W \operatorname{ords}\left(e_{t}\right), e_{t} \in W E\right\}\right|:$ The number of different bibliographical entries for which the word $w$ occurs in the title
- A: The set of entries in the test set (as above). Each entry $e$ has a title $e_{t}$ and a set $e_{c}$ of language id:s $\subseteq C$
- $P A_{A}(X)=\frac{\left|\left\{e \mid X(e)==e_{c}, e \in A\right\}\right|}{|A|}$ : The perfect accuracy of a classifier function $X$ on test set $A$ is the number of entries in $A$ which are classified correctly (the sets of categories have to be fully equal)
- $S A_{A}(X)=\sum_{e \in A} \frac{\left|\left\{X(e) \cap e_{c}\right\}\right|}{\left|e_{c} \cup X(e)\right|}$ : The sum accuracy of a classifier function $X$ on a test set $A$ is the sum of the (possibly imperfect) accuracy of the entries of $A$ (individual entries match with score between 0 and 1)


### 3.2 Naive Union Lookup

As a baseline to beat, we define a naive lookup classifier. Given an entry $e$, we define naive union lookup (NUL) as:

$$
N U L(e)=\cup_{w \in W \operatorname{ords}\left(e_{t}\right)} T D(w)
$$

For example, consider the following entry $e$ :

| \# | Substition Reg. Exp. | Replacement | Comment |
| :---: | :---: | :---: | :---: |
| 1. | \’\'\^ |  |  |
| ~\" | , ' | diacritics truncated |  |
| 2. | [qk] (?= [ei]) | qu | k -sound before soft vowel to qu |
| 3. | $\mathrm{k}(?=[\mathrm{aou}] \mid \$) \mid \mathrm{q}(?=[\mathrm{ao}])$ | c | k -sound before hard vowel to c |
| 4. | oolouloe | u | oo, ou, oe to u |
| 5. | [hgo]?u(?= [aouei] \|\$ | W | hu-sound before hard vowel to w |
| 6. | ( (?: [^aouei] *[aouei] [^aouei]*)+?) |  |  |
|  | (?: an\$\|ana\$|ano\$|o\$) | \1a | an? to a |
| 7. | eca\$ | ec | eca to ec |
| 8. | tschltx\|tj | ch | tsch, tx to ch |
| 9. | dschldj | j | dsch, dj to j |
| 10. | $\mathrm{x}($ ? $=\mathrm{i}$ ) | sh | x before i to sh |
| 11. | i (? [aouei]) | y | i before a vowel to y |
| 12. | ern\$\|i?sche?\$ | , , | final sche, ern removed |
| 13. | ( $[a-z]) \backslash 1$ | $\backslash 1$ | remove doublets |
| 14. | [bdgv] | $\mathrm{b} / \mathrm{p}, \mathrm{d} / \mathrm{t}, \mathrm{g} / \mathrm{k}, \mathrm{v} / \mathrm{f}$ | devoice b, d, g, v |
| 15. | [oe] | o/u,e/i | lower vowels |

Table 1. Given a language name $w$, its normalized spelling variants are enumerate according to the following (ordered) list of substitution rules. The set of spelling variants Spelling $(w)$ should be understood as the strings $\left\{w /\right.$ action $\left._{1-i} \mid i \leq 15\right\}$, where $w /$ action $_{1-i}$ is the string with substitutions 1 thru $i$ carried out. This normalization scheme is based on extensive experience with language name searching by the present author.

| Words $\left(e_{t}\right)$ | $L N\left(W \operatorname{lords}\left(e_{t}\right)\right)$ | Words $\left(e_{t}\right)$ | $L N\left(W \operatorname{lords}\left(e_{t}\right)\right)$ |
| :--- | :--- | :--- | :--- |
| etude | $\}$ | cameroun | $\}$ |
| du | $\{d u x\}$ | du | $\{d u x\}$ |
| samba | $\{n d i, c c g, s m x\}$ | nord | $\}$ |
| leko | $\{n d i, l s e, l e c\}$ | famille | $\}$ |
| parler | $\}$ | adamawa | $\}$ |
| d'allani | $\}$ |  |  |

Table 2. The calculation of $N U L$ for an example entry

Anne Gwenaïélle Fabre 2002 Étude du Samba Leko, parler d'Allani (Cameroun du Nord, Famille Adamawa), PhD Thesis, Université de Paris III - Sorbonne Nouvelle
The steps in its $N U L$-classification is as follows are given in Table 2,
Finally, $N U L(e)=\{n d i, l s e, s m x, d u x, l e c, c c g\}$, but, simply enough, $e_{c}=$ $\{n d i\}$.

The resulting accuracies for the test set are $P A_{N U L}(A) \approx 0.15$ and $S A_{N U L}(A) \approx$ 0.21. NUL performs even worse with spelling variants enabled. Not surprisingly, NUL overclassifies a lot, i.e., it consistently guesses more languages than is the case. This is because guessing that a title word indicates a target language just because there is one language with such a name, is not a sound practice. In fact, common words like $d u$ [dux], in [irr], the [thx], to [toz], and la [wbm, lic, tdd] happen to be names of languages (!).

### 3.3 Term Weight Lookup

We learn from the Naive Union Lookup experiment that we cannot guess blindly which word(s) in the title indicate the target language. Something has to be done to individuate the informativeness of each word. Domain knowledge tells us two relevant things. Firstly, a title of a publication in language description typically contains one or few words with very precise information on the target language(s), namely the name of the language(s), and in addition a number of words which recur throughout many titles, such as 'a', 'grammar', etc. Secondly, most of the language of the world are poorly described, there are only a few, if any, publications with original descriptive data. Inspired by the $t f$-idf measure in Information Retrieval (Baeza-Yates and Ribeiro-Neto 1997), we claim that informativeness of a word $w$, given annotated training data, can be assessed as $W C(w)$, i.e., the number of distinct codes associated with $w$ in the training data or Ethnologue database. The idea is that a uniquitous word like 'the' will be associated with many codes, while a fairly unique language name will be associated with only one or a few codes. For example, consider the following entry:
W. M. Rule 1977 A Comparative Study of the Foe, Huli and Pole Languages of Papua New Guinea, University of Sydney, Australia
[Oceania Linguistic Monographs 20]

| foe | pole | huli | papua | guinea | comparative | new | study | languages | and | a | the | of |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 1 | 2 | 3 | 57 | 106 | 110 | 145 | 176 | 418 | 1001 | 1101 | 1169 | 1482 |
| 1.0 | 2.0 | 1.5 | 19.0 | 1.86 | 1.04 | 1.32 | 1.21 | 2.38 | 2.39 | 1.10 | 1.06 | 1.27 |

Table 3. The values of $W C(w)$ for $w$ taken from an example entry (mid row). The bottom row shows the relative increase of the sequence of values in the mid-row, i.e., each value divided by the previous value (with the first set to 1.0).

Table 3 shows the title words and their associated number of codes associated (sorted in ascending order).

So far so good, we now have an informativeness value for each word, but at which point (above which value?) do the scores mean that word is a nearunique language name rather than a relatively ubiquitous non-informative word? Luckily, we are assuming that there are only those two kinds of words, and that at least one near-unique language will appear. This means that if we cluster the values into two clusters, the two categories are likely to emerge nicely. The simplest kind of clustering of scalar values into two clusters is to sort the values and put the border where the relative increase is the highest. Typically, in titles where there is exactly one near-unique language name, the border will almost always isolate that name. In the example above, where we actually have three near-unique identifiers, this procedure correctly puts the border so that Foe, Pole and Huli are near-unique and the rest are non-informative.

Now, that we have a method to isolate the group of most informative words in a title $e_{t}$ (denoted $S I G_{W C}\left(e_{t}\right)$ ), we can restrict lookup only to them. $T W L$ is thus defined as follows:

$$
T W L(e)=\cup_{w \in S I G_{W C}\left(e_{t}\right)} T D(w)
$$

In the example above, $T W L\left(e_{t}\right)$ is $\{f l i, k j y, f o i, h u i\}$ which is almost correct, containing only a spurious [fli] because Huli is also an alternative name for Fali in Cameroon, nowhere near Papua New Guinea. This is a complication that we will return to in the next section.

The resulting accuracies jump up to $P A_{T W L}(A) \approx 0.57$ and $S A_{T W L}(A) \approx$ 0.73 .

Given that we "know" which words in the title are the supposed near-unique language names, we can afford, i.e., not risk too much overgeneration, to allow for spelling variants. Define $T W L_{S}$ ("with spelling variants") as:

$$
T W L_{S}(e)=\cup_{w \in S I G_{W C}\left(e_{t}\right)} T D_{S}(w)
$$

We get slight improvements in accuracy $P A_{T W L_{S}}(A) \approx 0.61$ and $S A_{T W L_{S}}(A) \approx$ 0.74 .

The $W C(w)$-counts make use of the annotated entries in the training data. An intriguing modification is to estimate $W C(w)$ without this annotation. It turns out that $W C(w)$ can be sharply estimated with $W I(w)$, i.e., the raw number of entries in the training set in which $w$ occurs in the title. This identity breaks down to the extent that a word $w$ occurs in many entries, all of them
pointing to one and the same language id. From domain knowledge, we know that this is unlikely if $w$ is a near-unique language name, because most languages do not have many descriptive works about them. The $T W L$-classifier is now unsupervised in the sense that it does not have to have annotated training entries, but it still needs raw entries which have a realistic distribution. (The test set, or the set of entries to be annotated, can of course itself serve as such a set.)

Modeling Term Weight Lookup with $W I$ in place of $W C$, call it $T W I$, yields slight accuracy drops $P A_{T W I}(A) \approx 0.55$ and $S A_{T W I}(A) \approx 0.70$, and with spelling variants $P A_{T W I_{S}}(A) \approx 0.59$ and $S A_{T W I_{S}}(A) \approx 0.71$. Since, we do in fact have access to annotated data, we will use the supervised classifier in the future, but it is important to know that the unsupervised variant is nearly as strong.

## 4 Term Weight Lookup with Group Disambiguation

Again, from our domain knowledge, we know that a large number of entries contain a "group name", i.e., the name of a country, region of genealogical (sub-)group in addition to a near-unique language name. Since group names will naturally tend to be associated with many codes, they will be sorted into the non-informative camp with the $T W L$-method, and thus ignored. This is unfortunate, because such group names can serve to disambiguate inherent small ambivalences among near-unique language names, as in the case of Huli above. Group names are not like language names. They are much fewer, they are typically longer (often multi-word), and they exhibit less spelling variation.

Fortunately, the Ethnologue database also contains information on language classification and the country (or countries) where each language is spoken. Therefore, it was a simple task to build a database of group names with genealogical groups and sub-groups as well as countries. All group names are uniqu ${ }^{9}$ as group names (but some group names of small genetic groups are the same as that of a prominent language in that group). In total, this database contained 3202 groups. This database is relatively complete for English names of (sub-)families and countries, but should be enlarged with the corresponding names in other languages.

We can add group-based disambiguation to $T W L$ as follows. The nonsignificant words of a title is searched for matching group names. The set of languages denoted by a group name is denoted $L(g)$ with $L(g)=C$ if $g$ is not a group name found in the database.

$$
\begin{aligned}
T W G(e)= & \left(\cup_{w \in S I G_{W C}\left(e_{t}\right)} L N(w)\right) \\
& \cap_{g \in\left(W \operatorname{Words}\left(e_{t}\right) \backslash S I G_{W C}\left(e_{t}\right)\right)} L(g)
\end{aligned}
$$

[^17]|  | PA | SA |
| :--- | ---: | ---: |
| $N U L$ | 0.15 | 0.21 |
| $T W L$ | 0.57 | 0.73 |
| $T W L_{S}$ | 0.61 | 0.74 |
| $T W I$ | 0.55 | 0.70 |
| $T W I_{S}$ | 0.59 | 0.71 |
| $T W G$ | 0.59 | 0.74 |
| $T W G_{S}$ | 0.64 | 0.77 |

Table 4. Summary of methods and corresponding accuracy scores.

We get slight improvements in accuracy $P A_{T W G}(A) \approx 0.59$ and $S A_{T W G}(A) \approx$ 0.74. The corresponding accuracies with spelling variation enabled are $P A_{T W G}(A) \approx$ 0.64 and $S A_{T W G}(A) \approx 0.77$.

## 5 Discussion

A summary of accuracy scores are given in Table 4
All scores conform to expected intuitions and motivations. The key step beyond naive lookup is the usage of term weighting (and the fact the we were able to do this without a threshold or the like).

In the future, it appears fruitful to look more closely at automatic extraction of groups from annotated data. Initial experiments along this line were unsucessful, because data with evidence for groups is sparse. It also seems worthwhile to take multiword language names seriously (which is more implementational than conceptual work). Given that near-unique language names and group names can be reliably identified, it is easy to generate frames for typical titles of publications with language description data, in many languages. Such frames can be combed over large amounts of raw data to speed up the collection of further relevant references, in the typical manner of contemporary Information Extraction.

## 6 Related Work

As far as we are aware, the same problem or an isomorphic problem has not previously been discussed in the literature. It seems likely that isomorphic problems exist, perhaps in Information Extraction in the bioinformatics and/or medical domains, but so far we have not found such work.

The problem of language identification, i.e., identify the language of a (written) document given a set of candidate languages and training data for them, is a very different problem - requiring very different techniques (see Hammarström (2007a) for a survey and references).

We have made important use of ideas from Information Retrieval and Data Clustering.

## 7 Conclusion

We have presented (what is believed to be) the first algorithms for the specific problem of annotating language references with their target language(s). The methods used are tailored closely to the domain and our knowledge of it, but it is likely that there are isomorphic domains with the same problem(s). We have made a proper evaluation and the accuracy achieved is definetely useful.

## Acknowledgements

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## Part Two: Languages of the World

# Chapter V $\mid$ Counting Languages in Dialect Continua Using the Criterion of Mutual Intelligibility 

Corrected version of Hammarström, H. (2008). Counting languages in dialect continua using the criterion of mutual intelligibility. Journal of Quantitative Linguistics, 15(1):34-45.

# Counting Languages in Dialect Continua Using the Criterion of Mutual Intelligibility 

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#### Abstract

This paper shows how it is possible to count languages vs. dialects if, for every pair of varieties, we are given whether they are mutually intelligible or not. The method is to divide the varieties into a minimum number of internally mutually intelligible groups where each group counts as one language. Expressed in terms of graphs (as in discrete mathematics), the method is even easier understood as: applying graph-colouring to a graph over varieties with the intelligibility interrelationships as edges. Graph colouring is already mathematically well-understood and we can easily prove properties intuitively associated with the concepts language and dialect, and remove any fears that these concepts should lead to inconsistencies. The presentation requires only a minimal acquaintance with sets, combinatorics and graphs.


## 1 Introduction

In trying to answer the question "how many languages are there in the world?", linguists have had a hard time coming up with a satisfactory answer. Even when explicitly disregarding non-linguistic criteria (such as ethno-socio-economico-politico-cultural ones), they say that defining languages by the mutual intelligibility criterion (MI) is not possible (e.g. Anderson 2005).

Firstly, mutual intelligibility is not a strict yes/no distinction but a matter of degree. Subsumed hereunder are also cases where the degree of intelligibility is not enough to enable communication immediately, but high enough to enable communication after, say, only a few days of exposure, such as among the Mekeo languages (Jones 1998:19). Also, there may exist cases where intelligibility is not symmetric, i.e., $A$ understands $B$ but not vice versa, although I have yet to
see a genuine well-documented example $\sqrt{1}$.
Secondly, even if it were simplified into being yes/no and symmetric, counting languages by the MI, would lead to contradictions in dialect-chain situations. E.g. if $A$ is MI with $B, B$ is MI with $C$ but $A$ is not MI with $C$ - a completely realistic situation - then setting $A$ and $B$ to be the same language and $B$ and $C$ as the same language is contradictory because $A$ and $C$ are not the same language by the MI criterion.

In this paper we will show that the second objection is premature. There is a perfectly consistent way to count languages using a symmetric strict yes/no mutual intelligibility criterion that preserves intuitive properties about languages and numbers of languages. Linguists seem to have so far failed to appreciate this ${ }^{2}$, as the following selection of quotations exemplify:

Such situation are referred to by linguists as 'dialect chains', and they result in sometimes arbitrary decisions being made as to how many languages are involved. (Lynch and Crowley 2001:2)

The criterion that "technically ... mutually intelligible forms of speech are known as dialects, and [that] the term language is used for mutually unintelligible forms of speech" (Lehmann 1973:33), does not apply satisfactorily to such situations as the Chaga continuum from Siha to Usseri. (Polomé 1980:3)

A common situation is a string of similar varieties, in which the speakers of variety A understand those of C, and so on, but the speakers of A do not understand the variety at the other end of the continuum, or even those part way along. Even if we can define 'understand', where is the divide between language and dialect in this situation? (Heine and Nurse 2000:2)

In some cases, the intelligibility criterion actually leads to contradictory results, namely when we have a dialect chain, i.e., a string of dialects such that the adjacent dialects are readily mutually intelligible, but dialects from the far ends of the chain are not mutually intelligible. A good illustration of this is the Dutch-German dialect complex. One could start from the far south of the German-speaking area and move to the far west of the Dutch-speaking area without encountering any sharp boundary across which mutual intelligibility is broken; but the two end points of this chain are speech varieties

[^18]so different from one another that there is no mutual intelligibility possible. If one takes a simplified dialect chain $\mathrm{A}-\mathrm{B}-\mathrm{C}$, where A and B are mutually intelligible, as are B and C , but A and C are mutually unintelligible, then one arrives at the contradictory result that A and B are dialects of the same language, B and C are dialects of the same language, but A and C are different languages. There is in fact no way of resolving this contradiction if we maintain the traditional strict difference between language and dialects, and what such examples show is that this is not an all-or-nothing distinction, but rather a continuum. In this sense, it is impossible to answer the question how many languages are spoken in the world. Comrie 1987:3)

On the latter quote, a few clarifying remarks are in order: Comrie is discussing the definition that runs "two varieties are the same language if and only if they are mutually intelligible, 3 . I am not denying that this definition leads to a contradiction - I am saying that other intuitively acceptable definitions based (solely) on the MI have been ignored. In particular, I will present a definition whereby it is still true that "if two varieties are the same language then they are mutually intelligible" but the converse "if two varieties are mutually intelligible then they are of the same language" does not have to be true. The spirit of the latter is instead rendered by a slightly more relaxed requirement that says that the number of languages should not be unnecessarily multiplied. The definition is given full formal treatment below.

## 2 Counting Languages

The task is to decide, for a finite set $X$ of speech varieties, how many languages there are using only a binary symmetric strict yes/no relation of mutual intelligibility (henceforth MI). For ease of presentation we shall model the situation as there being $n$ speakers each speaking exactly one variety. It will be seen that the method is really indifferent to the distribution of varieties over people, names or any other grouping, so there is no loss of generality. Speakers will be denoted by capital letters, e.g., $A, B, C$. Thus let $X=\{A, B, C, \ldots\}$ be a any finite set of speakers.

### 2.1 Definition

Definition 1 The number of languages in $X$ is the least $k$ such that one can partition $X$ into $k$ blocks such that all members within a block understand each other.

[^19]A partition of a set $X$ into blocks is simply a division of the members of $X$ into disjoint non-empty groups that exhaust $X$. So if say, $X=\{A, B, C\}$, we can partition it into:

1. One block: $\{A, B, C\}$
2. Two blocks: there are exactly three possibilities $\{A, B\},\{C\}$ or $\{A\},\{B, C\}$ or $\{A, C\},\{B\}$.
3. Three blocks: $\{A\},\{B\},\{C\}$.

Clearly, the number of blocks in a partition ranges between 1 and the number of members of the set (also known as the cardinality of the set).

Now let's say $X=\{A, B, C\}$ depicts the classic dialect chain situation where $A$ and $B$ are MI, $B$ and $C$ are MI, but $A$ and $C$ are not MI. The partition into one block does not satisfy the requirement of the definition, since $A$ and $C$, that are in the same block, do not understand each other. Of the three partitions into $k=2$ blocks, two of them satisfy the definition: $\{A, B\},\{C\}$ is ok because $A$ and $B$ are MI; $\{A\},\{B, C\}$ is ok because $B$ and $C$ are MI. The partition into three blocks also trivially satisfies the condition that no pair within a block should be mutually unintelligible, but $k=3$ is not minimal. Thus the number of languages in the example is 2 , and we can immediately observe a curious feature of the definition: the number of languages $k$ is unique, but there may be several satisfying partitions into $k$ blocks.

### 2.2 Properties

It should be obvious that the definition is well-behaved in the sense it yields a unique number of languages $k$ (for example, one way to arrive at the number is to just try out all partitions of the given set $X$ ). It should also be clear that a partition defines an assignment of speech varieties into languages such that $A$ and $B$ belong to the same language if and only if they belong to the same block. But what about properties of partitions that satisfy the minimal $k$ and the requirement of inside-block intelligibility? Intuitively, if blocks are to be identified with languages, one would expect the following two properties to hold:

Property 1 All those who speak the same language speak varieties which are mutually intelligible.

Property 2 There are no "superfluous" languages, i.e., for any division of varieties into languages satisfying property 1, a person speaking exactly one variety of each of the languages can communicate with everyone, whereas someone speaking less than $k$ varieties cannot communicate with everyone.

That the first property holds for the given definition is immediate from the definition. Informally, the second property holds because otherwise $k$ would not be minimal, as required. A more detailed proof, which involves a little more work, is given below in section 3.3

The definition and the properties emanating from it, is not specific to any particular type of language-variety landscape but extends to completely arbitrary constellations of language varieties and MI-interrelationships. It should actually be understood as an even more abstract counting method: given a set of objects and a symmetric, non-reflexive, non-transitive "is-different" relation over them (here: mutual unintelligibility), what is the minimal number of blocks one can partition this set into such that all members within a block are not different to each other?

For pedagogical reasons we shall now continue the presentation in terms of graphs.

## 3 Further Examples and Properties

Again, the task is to decide, for $n$ speech varieties, how many languages there are using only a binary symmetric strict yes/no relation of mutual intelligibility.

### 3.1 Definition

Let the $n$ speakers be vertices $V$ of a graph ${ }^{4} G$. Let $G$ have an edge between vertices $A, B \in V$ if and only if $A$ and $B$ do not speak mutually intelligible varieties.

Definition 2 The number of languages is the smallest $k$ such that one can colour the vertices of $G$ with $k$ colours such that no two vertices that share an edge have the same colour.

This number is usually called the chromatic number of a graph $G$ and is denoted $\chi(G)$ (Read 1968).

### 3.2 Examples

Again, an example of a graph illustrating the most basic dialect-chain situation is shown in figure 1 For $G$ in figure 1 the chromatic number is 2 . It is not possible to colour the vertices $A, B$ and $C$ with only one colour because then $A$ and $C$ would get the same colour - violating the condition that vertices which share an edge should not have the same colour. It would be possible to colour the vertices with (exactly) three colours, one each, without violating the shared-edge-different-colour condition, but 3 is not the chromatic number because it is also possible to colour $G$ with less, namely 2 , colours. There are in fact two different ways to colour $G$ with 2 colours (say red and green): 1. $\{A, B\}$ red, $\{C\}$ green; 2. $\{A\}$ red, $\{B, C\}$ green.

Another example, a four-member dialect chain, is shown in figure 2 For $G$ in figure 2 the chromatic number is also 2 . There is only one 2 -colouring: $A, B$

[^20]

Figure 1. Graph for $(A, B),(B, C)$ are MI but $(A, C)$ are not MI.
green and $C, D$ red. (Clearly, one colour is not sufficient. However, if one tries 2 colours: $A$ must have some colour, then $C$ and $D$ must have a different colour. Nothing prevents $C$ and $D$ from having the same colour, so they get the same colour. Now, only $B$ remains which cannot be coloured by the colour of $C$ and $D$, but it can have $A$ :s colour. All the choices were forced or colour-conservative so this is the only 2 -colour possibility.)


Figure 2. Graph for $(A, B),(B, C),(C, D)$ are MI but no other pairs are MI.

Lastly, a third slightly more complicated example is shown in figure 3. The chromatic number of the graph in figure 3 is 3 . There are no less than five different minimal colourings: 1. $\{A\}\{B, D\}\{C, E\} ; 2 .\{B\}\{A, D\}\{C, E\} ; 3$. $\{A, D\}\{B, E\}\{C\} ;$ 4. $\{A, C\}\{B, E\}\{D\} ; 5$. $\{A, C\}\{B, D\}\{E\}$. This is perhaps more easily seen if the graph is redrawn (not changed) as a pentagon, i.e by keeping $A$ at the top, but putting $D$ and $C$ at the next level and $B$ and $E$ at the bottom level (as shown in figure (4).

### 3.3 Properties

As may have been experienced by the reader, it is not trivial to calculate what the chromatic number is, even for a graph of quite moderate size. It should be clear to everyone though, that it is always possible to reach the answer by tediously enumerating and checking all possibilities.

There is a mathematically well-understood systematic method to calculate the chromatic number (and the number of minimal-size colourings), in terms of


Figure 3. Graph for $(A, B),(B, C),(C, D),(D, E),(E, A)$ are MI but no other pairs are MI.
breaking down any graph into more tractable pieces. The interested reader may consult the excellent introduction by Read (1968).

The bad news is that finding the chromatic number is an NP-complete problem (Garey and Johnson 1979). In layman terms, this implies that there is no known "smarter" method to find the chromatic number than to go through all the possible partitions of the vertices into blocks ("colours"). All known methods rely on the fact that it is "easy" to check whether a given colouring is ok, i.e., just to check if any edges violate the constraint, but still, in the worst case, need to step through essentially all possible partitions. This is the bottleneck because the number of possible partitions of $n$ vertices in blocks is exponentia $\sqrt[5]{5}$ in $n$. For instance, if $n=20$ there are 51724158235372 partitions to consider. Such is the problem in its full generality. But of course, for specific cases, there may be symmetries and regularities which makes the solution considerably more digestible.

As has been observed, there may be more than one minimal colouring. For any of one these minimal colourings, we can identify colours as languages. That is, let $G$ again be the graph depicting the situation at hand and let $c_{1}, c_{2}, \ldots, c_{k} \neq \emptyset$ be a minimal colouring, thus satisfying $k=\chi(G)$ (the chromatic number of $G), \bigcup c_{i}=V$ and $c_{i} \bigcap c_{j} \neq \emptyset$ for $i \neq j$. Identifying languages as colours simply means that $c_{1}, \ldots, c_{k}$ form the $k$ languages. Languages so defined have the following two crucial properties:

Property 1 All those who speak the same language speak varieties which are mutually intelligible.

Property 2 There are no "superfluous" languages, i.e., for any division of varieties into languages satisfying property 1, a person speaking exactly one variety of each of the languages can communicate with everyone, whereas someone

[^21]speaking less than $k$ varieties cannot communicate with everyone.

Proof of property 1: Assume there were a pair of non-MI varieties of the same language, i.e., assigned the same colour. Since they were not MI they would share an edge in the graph - contradicting that colouring was legal in the first place.

Proof of Property 2: Assume that one speaks $k^{\prime}<k$ varieties $Z_{1}, Z_{2}, \ldots, Z_{k^{\prime}}$. Form the $k^{\prime}$ groups one could communicate with using the respective variety: $c_{i}^{\prime}=\left\{Y \in V \mid Y\right.$ is MI with $\left.Z_{i}\right\}$ for $1 \leq i \leq k^{\prime}$. (If $c_{i}^{\prime} \bigcap c_{j}^{\prime} \neq \emptyset$ for some $i<j$ then remove the intersecting elements from (say) $c_{i}^{\prime}$ ). If one could communicate with everyone using the $Z_{i}$ varieties, then $\bigcup c_{i}^{\prime}=V$. If $c_{1}^{\prime}, c_{2}^{\prime}, \ldots, c_{k^{\prime}}^{\prime}$ satisfies property 1 , i.e., within each $c_{i}^{\prime}$ there are no edges between the members, then $c_{1}^{\prime}, c_{2}^{\prime}, \ldots, c_{k^{\prime}}^{\prime}$ would yield a legal colouring of $G$ - contradicting the minimality of $k$.

Restating, any minimal colouring of a (graph of) a language/dialect situation has the above two properties. Any count of the number languages other than "as many as the blocks of a minimal colouring" would in some way fail to satisfy one of the two properties about the languages counted. And clearly, the two stated properties must be part of the intuitive understanding of what it means to be a language.

At this point, however, we still cannot give a finished count of the number languages of the world because:

- We still do not have an answer to when mutual intelligibility holds given two languages (cf. the first point in the introduction).
- Even if we did have a good (or arbitrary) method to decide when two varieties are mutually intelligible, we do not have complete knowledge of the speech varieties of the world. The best one-piece source on this matter is the Ethnologue (Gordon 2005) but it does not provide (nor does it aim to) systematic detailed information on (any kind of) intelligibility between varieties.
- As alluded to above, even if we did have complete knowledge etc, the resulting graph for the world would have on the order of 6900 vertices, which might be intractable. Since most language varieties, unquestionably, aren't intelligible to each other, this graph would turn out quite easyhandled, but it remains to see just how complex it does get.


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Figure 4. Graph for $(A, B),(B, C),(C, D),(D, E),(E, A)$ are MI but no other pairs are MI.

## Appendix: Failing Approaches to Defining Languages Uniquely

As seen in the previous section, the method for counting languages does not always uniquely determine which the languages are, it just says how many they are and gives a number of alternatives to which they are. It is tempting to look at ways to synthesize the alternatives into a unique language/dialect definition.

For example, it is readily seen in figure 1 that in the two minimal colourings, $A$ and $C$ are never in the same colour, whereas $B$ is once in the company of $A$ and once in $C$. It is then tempting to define the languages as "the maximum-size set $L$ of vertices that are never in the same colour in any minimal colouring". The rest of the vertices can then be thought of as dialects of the varieties to which they are MI. (A dialect can then be the dialect of several (distinct) languages, and even be a dialect of a dialect). In the example of figure 1 this would beautifully synthesize the two minimal colourings to say that $A$ and $C$ are separate languages and $B$ is a dialect of $A$ as well as a dialect of $C$.

Unfortunately there are cases where this approach does not "work". In the graph of figure 2, $L$ would not be unique; either of $L=\{A, C\},\{A, D\},\{B, C\}$, $\{B, D\}$ has the maximum-size 2. (Here, of course, since there is only one minimal colouring, we can satisfactorily take $A B$ and $C D$ as the two languages and call $A$ a dialect of $A B, B$ another dialect of $A B$, and so on).

But, more seriously, in the case of figure 4 (depicting the same situation as in figure (1), there are five different maximum-size $L=\{A, C\},\{A, D\},\{B, D\}$, $\{B, E\},\{C, E\}$, so $|L| \neq k$ which invalidates the idea. The graph of figure 4 is the smallest graph where $|L| \neq k$. I don't believe there is a sensible way of uniquely defining languages in such graphs (that is, graphs which have oddsize circles but whose chromatic number is lower than the number of members of the circle). In the graph in question, we are told that there are exactly 3 languages but all the vertices are symmetric so there seems to be no way to
single out three of them or divide five nodes into three equal-size groups. If we wish to select 3 of the five to be languages and the other 2 dialects, there is no un-arbitrary way to decide which go as languages since all five vertices are structurally indistinguishable. If we wish to divide the 5 into three groups, they would not all be of equal size and, again, there is no basis for putting one or the other vertex in the bigger (or smaller) group.

This might not just be a purely theoretical problem. It is conceivable that such a "ring" could be the correct state of affairs somewhere in the world, say, if a dialect continuum settled around a mountain and the two extremes of the chain meet and influence each other (for a couple of centuries) so that they become intelligible dialects.

## Chapter VI $\mid$ Whence the Kanum base-6 numeral system?

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# Whence the Kanum base-6 numeral system? 

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#### Abstract

Base-6-36 numeral systems, a typological rarity, are found in Kanum languages of New Guinea as testified by Donohue (2008). We look at the probable relatives of the Kanum languages and show that the base-6 system must have emerged in the Tonda group specifically. Since there is no evidence of body-part terms in the base-6 forms attested, we speculate that these systems have a different origin. Specifically, we suggest that the base- 6 systems arose for counting yams. The ethnographic data for Kanum and other relevant languages are in concord with such a scenario. Whether there is a historical connection with base-6 systems of the Kolopom languages, near, but not adjacent, to the west, remains an open question. If there is a connection, it is areal rather than genetic, but sufficient evidence for a pre-historic areal connection remains to be amassed. Equally, if not more, puzzling would be the conclusion that there is no historical connection, given the rarity of base-6 in the world as a whole.


Keywords: Numerals, Numeral Systems, New Guinea, Papuan Languages, Areal Diffusion, Kolopom, Frederik-Hendrik-Eiland, Kanum, Nambu, Tonda, Yei, Trans New Guinea, Typological Rarities, Morehead and Upper Maro

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## 1 Background on Kanum and Related Languages

This commentary attempts to trace the origins of the base- 6 numeral system of Kanum, as far as available data permits 1

Conventionally, the Kanum languages are classified as belonging to the Morehead and Upper Maro family, consisting of Tonda (ca 10 languages, including Kanum, around the Bensbach [aka Torassi] and Morehead rivers), Nambu (about 6 languages, immediately east of the Tonda languages, east of the Morehead) and Yei (roughly two languages (Sohn 2006:20), immediately north of the Tonda area).

It is not yet certain whether Tonda, Nambu and Yei are genetically related, but there are interesting numeral form resemblances in Tonda-Nambu-Yei for 1 and 2 (see below), so if it is indeed a valid genetic family, these are probably cognates. As far as we can tell, no other languages in the region show suggestive form resemblances in the numeral domain.

## 2 Numerals in Kanum and other Relevant Languages

It is clear from early and late data that the Yei language(s) originally had a restricted numeral system, i.e., monomorphemic numerals for 1 and 2, above which ad hoc repetitions or inexact words would be used $2^{2}$ A selection of the published forms for 1 and 2 are shown in Table 1 .

There are some 20 attestations of numerals from varieties of the Nambu group, most of which are collected and analyzed in Lean (1986:52-59). Almost all vocabularies agree on the roots for 1 and 2 . These roots resemble the \#marked ${ }^{3}$ forms shown in Table 1 . In contrast, above 2, the vocabularies wholly diverge. Some vocabularies show a restricted system with $3=2+1$ and $4=2+2$, whereas others have a monomorphemic $3,4=2+2$ and evidence of base 5 above that. In other words, proto-Nambu must have had a restricted system whereas some modern Nambu varieties show base- 5 , or incipient base- 5 systems.

The base- 6 system of Kanum, along with the parallel simple and moderate systems, as recorded by Donohue (2008) are repoduced in Table 3. All other available data on Tonda group languages are collected in Table 2, but, as will

[^22]Table 1. Numerals in Yei and Nambu. Komadeau, Dongeab, Kwĕl are from Nevermann (1942) while Poo is cited from Sohn (2000) and Jéi [from the Upper Maro] is from Drabbe (1954). The Yei varieties are separated into two languages as suggested by (Sohn 2006:20). The Nambu resemblant forms are based on the data in Lean (1986:52-59). The three-letter codes in brackets are the iso-639-3 codes for the languages in question.

|  | Tanas-Bupul [jei] Komadeau | Doñgeab | Erambu-Poo [jei] |  |  | Nambu |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | Kwĕl | Poo | Jéi |  |
| 1 | námpŭе̄ | námpĕ | námpai | na:mpaj | nāmpèi | \# ambiro |
| 2 | jītáape | hētăpē | ìtápai | jeta:paj | jètapaé | \#tumbi |

be seen, many of the vocabularies do not include numerals beyond 6 . The first publication to unambiguously attest a full base-6 system is an anthropological work, frequently overlooked by linguists. Williams (1936:225-227) comprehensively describes the use of a base- 6 system used for counting taitu (a smaller variety of yams) with the groups he labels Keraki. The words for 1, 2, 36, 216 and 1296, all monomorphemic, can be found in the text. Now, the peculiarity is that the Keraki speak a Nambu group language and would normally use a base- 5 counting system, only borrowing the base- 6 system in question from a Tonda group for the said counting activity. Williams himself testifies that for most of the Nambu groups (including Keraki) "The numerals run up to 5, and there is no elaborate system of counting except in so far as it has been learned from the west [i.e., Tonda languages - HH]" (Williams 1936:38), that for most of the Tonda varieties "numerals run up to six" (Williams 1936:35), and finally that "The custom of counting the taitu accurately is apparently a more or less recent fashion among the Keraki, having been imported from beyond the Morehead. It is still necessary, indeed, to have the assistance of experts before the count can be attempted in a Keraki village, for the enumeration is that of the Gambadi and Semariji [= dialects of Kunja, in modern language listings - HH] languages, viz. a 1-6 system, not that of the Keraki group, which employs a 1-5 system." There can be no question that Tonda group languages are what Williams meant by "from the west" and that the final quote witnesses this statement, because Tonda group languages are the only languages to the west considered by Williams, ${ }^{4}$

We may now turn to the analysis of the above Tonda, Nambu and Yei data.
The base-6 system is clearly at home in the Tonda group as it is unattested in Yei and Nambu, apart from the one case in Nambu where it is explicitly recognized as a Tonda group borrowing. The forms for 1-2 in Tonda-Nambu-Yei show some promising resemblance, but, as the transciption is dubious for most of the data, it is hardly meaningful to elaborate on these potential correspondences. No form correspondence between any Nambu and Tonda numeral above

[^23]Table 2. Numerals in Tonda group languages. Sources and non-trivial identifications into the language division of Gordon (2005) are as follows. "Bangu" (MacGregor 1897) is a dialect of Kunja (Ayres 1983:11). "Keraki" (Williams 1936:225-227) borrowed the listed numerals from Kunja. "Mani" is not from native speakers but from Ngkâlmpu Kanum speakers who knew Mani (Nevermann 1939:58), and while the Mani village was abandoned in the 50s (Hitchcock 2004:388), it would have been a dialect of Kunja in the time of Nevermann. Tokwasa (Lyons 1914) is a dialect of Kunja (Avres 1983:141). "Peremka" (Riley and Ray 1931:849-850) is a dialect of Wára. Wandatokwe (Lyons 1914) is a dialect of Wára (Ayres 1983:139). Ngkâlmpu 1 is from Drabbe (1954:37). Ngkâlmpu 2 is from Nevermann (1939). "N'gowugar" (Nevermann 1939) is a dialect of Blafe. "Tonda" (Lean 1986:48-49) is a dialect of Blafe. Sota Kanum is from Donohue (no date). The three-letter codes in brackets are the iso-639-3 codes for the languages in question.


Table 3. The base-6 system of Kanum, along with the parallel simple and moderate systems Donohue (2008). The forms are from Yanggandur which belong to Ngkâlmpw Kanum [kcd] in the division of Gordon (2005).

|  | Kanum, Ngkâlmpw [kcd] Yanggandur |  |  |
| :---: | :---: | :---: | :---: |
|  | simple | moderate | complex |
| 1 | naempr | aempy | aempy |
| 2 | yempoka | ynaoaempy | ynaoaempy |
| 3 | ywaw | ylla | ylla |
| 4 | eser | eser | eser |
| 5 | swabra | tampwy | tamp |
| 6 | 'swy | traowao | ptae |
| 7 |  | psymery aempy | aempy ptae |
| 8 |  | psymery ynaoaempy | ynaoaempy ptae |
| 9 |  | psymery ylla | ylla ptae |
| 10 |  | psymery eser | eser ptae |
| 11 |  | psymery tampwy | tamp ptae |
| 12 |  | psymery traowao or yempoka traowao | tarwmpao |
| 13 |  |  | aempy tarwmpao |
| 14 |  |  | ynaoaempy tarwmpao |
| 15 |  |  | ylla tarwmpao |
| 16 |  |  | eser tarwmpao |
| 17 |  |  | tamp tarwmpao |
| 18 |  |  | ntamnao |
| 19 |  |  | aempy ntamnao |
| 20 |  |  | ynaoaemy ntamnao |
| 24 |  |  | wramaekr |
| 25 |  |  | aempy wramaekr |
| 30 |  |  | ptae wramaekr |
| 31 |  |  | aempy ptae wramaekr |
| 36 |  |  | (ntaop) ptae |
| 37 |  |  | aempy (ntaop) ptae |
| 50 |  |  | ynaoaempy tarwmpao (ntaop) ptae |
| 100 |  |  | eser wramaekr ptae ynaoaempy |
| 216 |  |  | tarwmpao |
| 1296 |  |  | (ntaop) ntamnao |
| 7776 |  |  | (ntaop) wramaekr |

2 has been noted. Consequently, if Tonda-Nambu-Yei are related, the simplest hypothesis is that proto-Tonda-Nambu-Yei had a restricted system, and that the Tonda base- 6 system post-dates the breakup of the hypothesized family. The alternative hypothesis, that a Tonda-Tambu-Yei proto-language had a base-6 system, is less favourable because is requires two traceless evaporations of the base-6 system, once in Tonda and once in Yei.

To pinpoint the origin of the base- 6 system within the Tonda group is not easy with the data at hand and the fact that, in Kanum as described by Donohue (2008) - the case where we do have reliable data - several systems are at play at the same time (cf. Table 3). If we posit the base- 6 system to proto-Tonda all vocabularies are reasonably well-explained, except Mani of Nevermann which then could be deemed erroneous (recall that it does not come from native speakers). The divergence in forms for 5 and 6 could be accounted for by contrasts between simple/moderate systems and the forms for 3 as divergences after the break-up of proto-Tonda. On the other hand, the possibility that the base- 6 was borrowed between Tonda varieties after the break-up of proto-Tonda cannot be ruled out; this hypothesis has the advantage of explaining Mani of Nevermann as a dialect that simply did not borrow it, and would also readily explain why the higher numerals 36,216 and 1296 turn up in identical forms.

Be the phylogeny of the base- 6 system within Tonda as it may, we must ask what provoked the appearance of this system, for it is a major typological rarity. In a survey that covers languages from every language family in the world (including isolates), and in each family covers most of the languages of the family, we find general purpose base-6-36 systems on only two places in the world; in Tonda as above, and on Kolopom Island (see below) Hammarström pear) 5

Usually, restricted numeral systems, as they develop normed expressions for higher exact quantities, take the path via hands and feet to make 5-10-20 systems. This is usually apparent in the etymologies for the forms in questions. What happened in Tonda is different - the base-6 system does not connect with fingers, hands, feets or any other body part counting. If the Tonda base-6 system does not come from counting on the body, where does it come from? As we shall see, there is an intriguing connection with the counting of yams!

The hypothesis can be formulated as follows. As a culture switches from hunting and gathering to a more tuber-cultivating subsistence mode, which requires storing and planting, there is more incentive for exact counting, thus more pressure for a speech community to develop normed expressions for higher exact quantities than 2 or 3 ( $=$ number of objects whose number one immediately recognizes, without grouping or counting). Almost always, tallying on the hands (fingers) and feet (toes) bootstraps the emergence of such normed expressions, yielding a 5-10-20 structure. If, as in the case of Tonda, the human body is not the source of these expressions, we should get some other structure than the 5-10-20 with hand-feet-man etymologies.

[^24]This hypothesis explains a number of facts. The first part, which says that tuber-agricultural languages should have non-restricted system: $\sqrt{6}$, explains why the base- 6 arose in Tonda and was borrowed into Nambu where yams are staple food (Ayres 1983, Williams 1936, Hitchcock 2004), rather than in Yei, who are essentially hunter-gatherers (van Baal 1982). This is further strengthened by the fact that both Williams (1936:225-227) and Lean (1986:48) independently (Lean was unaware of Williams) adduce that the base- 6 was intrinsically connected with counting yama $\sqrt[7]{ }$. The second part, which says that that if the system is not $5-10-20$ then the etymologies of the forms should not involve body parts 8 explains why we fail to find 'hand' etc. etymologies in the base- 6 systems in Tonda. Now, of course, there is nothing we know about yams that predicts 6 it could have been 4,7 or some other number - the point is that it is in sharp contrast with the otherwise ubiquitous 5-10-20 systems.

To make the epistemology clear, let us summarize the kind of evidence - so far absent - that would refute the above hypothesis about the emergence of the Tonda base- 6 systems.

- Etymologies of crucial Tonda forms involving body-parts (or anything disconnected from tuber cultivation).
- Evidence of tuber cultivation, either in the past or present, in nearby varieties which do not show base-6 numeral systems.
- Presence of base-6 systems, either in the past or present, in nearby varieties without a subsistence type with similar importance of tuber cultivation.
- Very many examples around the world of tuber cultivating societies with restricted numeral systems.
- Ethnographic data about counting and specific cultural objects that would render the comments by Lean and Williams without discriminatory power. For example, if counting some other objects than yam was prior to, or more common, in Tonda and surrounding varieties, this would weaken the causal interpretation of the yams connection. Likewise, if ethnographic comments connecting the actual numeral system and some specific thing counted can be found in the non-base-6 languages "everywhere" then this evidence does not "select" the Tonda languages.

There is one more point to be made as to the Tonda base- 6 numeral systems, namely the base- 6 system(s) attested in the Kolopom languages. The Kolopom

[^25]languages are Kimaama, Riantana and Ndom, occupying most of Kolopom island (formerly Frederik-Hendrik-Eiland) in southeast Indonesian Papua. Kimaama and Riantana are almost certainly genetically related, since the 1st and 2 nd person pronouns correspond in singular as well as plural, and have lexicostatistical agreement in the 20-40\% range (Drabbe 1949, Voorhoeve 1975, Menanti and Susanto 2001). Ndom is likely to be genetically related to KimaamaRiantana as well, but there is a little room for doubt. Ndom also shares the 1st person singular and plural pronoun form but lexicostatistical figures between Ndom and Kimaama/Riantana villages may drop below $10 \%$ Menanti and Susanto 2001). Table 4 reproduces all available Kolopom numeral data $\sqrt{9}$

Considering that the data by Drabbe is the most reliable, we can interpret the vocabularies as follows. Drabbe's data attests base-6 for Kimaama below 20, and this is corroborated by "Teri-Kalwasch" of Geurtjens (up to 10) and by "Täri-Kalwa" of Nevermann, though Nevermann presumably made an error at 13: Since 13 (cf. 13 and 19 of Riantana) can be either n $\tilde{\imath}$ or ñ növere (Drabbe 1949:8), Nevermann must have got the impression that the former was 13 and the latter 14 , resulting in a wordlist with a $6-13(!)$ system. This is understandable given the difficult circumstances under which he collected this data (Nevermann 1935b:56-59). At 20 (19?), Kimaama of Drabbe turns into base-20, and in "Klader", "Kimaam" of Nevermann as well as "Kaladdarsch" of Geurtjens, the systems lapse into base- 5 already at 7 . Note that both the $\# i b u d a$ and \#turwa roots adapt the meaning 5 rather than 6 in these cases! Clearly, the base- 6 system in the Kimaama area was a competition with a base- 5 system of the commonplace type - as expected ketsja nda kawé/kitjanta kuwe literally means "two hands" (Kluge 1938:148), and tjĩ means "man" (Drabbe 1949:8). Not unexpectedly, Donohue who collected Kimaama data more recently, found only a base- 5 system (p.c. July 2008). Riantana is base 6 up to 24 which seems to have been the limit of counting ("en verder schijnt men daar niet te tellen") (Drabbe 1949:8). Also, tarö is the Riantana word (both) for 'many' and 'all' (Drabbe 1949:24). Finally, Drabbe's Ndom informant gave a consistent 6-36 system up to 180 , with multiplications, a feature which is lacking in the Kimaam and Riantana data.

As for resemblances in form, it will be seen that the Kimaama and Riantana 3-6 seem to correspond, and not impossibly 1-2 as well. However, the TeriKalwa Kimaama of Geurtjens constructs $6-10$ with the \#me-morpheme that Drabbe ascribes to Riantana rather than Kimaama. Thus we are faced with borrowing, parallel systems or both - in a way we cannot hope to unravel at this point. The bottom line is that we now have a total of three base- 6 systems with independent sets of forms, Kimaama-Riantana, Ndom and Tonda.

We have found no suggestive etymologies for any of the morphemes involved (except 10 and 20 of some Kimaam varieties, as above). Kluge (1938:148) did propose a link between Kimaam durua 'upper arm 10 and turua ' 6 ', but there are good reasons for considering it a minimal pair rather than an etymological

[^26]link 11 . Firstly, Drabbe fails to mention any such connection, which one suspects he would have caught if it was real. Secondly, the three independent attestations distinguish the 'upper arm/leg'-word with $d$ from the ' 6 '-word with $t$ as durua $\sim$ turua (Nevermann), durò $\sim$ turò (Drabbe) and doerwa $\sim$ toeroea (Geurtjens) showing that we are not dealing with allophonic variation for initial $\mathrm{d} / \mathrm{t}$. Also, two likely Austronesian loans with an unvoiced initial dental stop, tùano 'owner' and tamoekoe 'tobacco', are rendered as such, i.e., with t rather than d (Drabbe 1949).

The three systems have independent morphemes but are similar in structure. The fact that this structure, base-6, is extremely rare in the world, merits an investigation of a possible historical connection between the three. It is extremely unlikely that a genetic connection is the reason for the shared base6 systems, since we cannot find likely lexical cognates bridging Tonda to any Kolopom language, and, as we have seen, the base-6 system does not go back to the most likely relatives of Tonda. Ndom is adjacent to Kimaama-Riantana (and only to Kimaama-Riantana) so a historical connection here is almost certain, in spite of the differing morphemes.

However, between Kolopom and Tonda we find intervening Komolom, YelmekMaklew, Morori and Marind languages which show no traces of base-6. The Komolom languages have base-5. The Yelmek-Maklew and Marind languages have restricted systems (Galis 1955), as did Morori originally (Nevermann 1939:69). It is relevant here to note that, as expected, the Kolopom (Serpentil 1965 ) ${ }^{12}$ and Komolom (Nevermann 1935a) are tuber-agriculturalists while Yelmek-Maklew (Walker and Mansoben 1990, Aubaile-Sallenave and Bahuchet 1994), Morori (Nevermann 1939:37) and Marind speakers rely more on sago, hunting and gathering (van Baal 1966, Wirz 1922).

Figure 1 has a map of all the languages involved in the discussion.
If there is a historical connection between the Kolopom and Tonda languages it should thus be along the following scenario. There was once a stretch of tuber-cultivators connecting the Kolopom and Tonda languages geographically; this stretch was broken by invading Marind family speakers who rather depend on sago, hunting and gathering. While this scenario has in fact been painted before, based on other similarities than base-6 (Nevermann 1939:6), it remains very speculative. Should one wish to entertain this speculation further, there are, in fact, two potentially cognate forms in key terms in the base-6 systems, namely \#turua (Kimaama-Riantana) ~ \#traowao (Tonda) for '6' and \#teroamä (Kimaama-Riantana) ~ \#tarwmpao (Tonda) for '12'.

The opposite hypothesis, that the only two veritable base-6 systems appeared in a tiny area in South West New Guinea by chance, is no stronger than accounting for phonemic click languages in Eastern Africa and Southern Africa by independent innovation!

[^27]Table 4. Published data on numerals in the Kolopom languages. Sources and non-trivial identifications into the language division of Gordon (2005) are as follows. Ndom, Riantana, and Kimaghama are from Drabbe (1949:6-8). "Kaladdarsch" and "Teri-Kalwasch" (Geurtjens 1933) are Kimaama villages (Gordon 2005). "Klader", "Kimaam" and "Täri-Kalwa" in Kluge (1938: 148), originally from manuscript vocabularies taken up by Nevermann in 1933-1934, are all all village names within the boundaries of Kimaama. The three-letter codes in brackets are the iso-639-3 codes for the languages in question.

|  | Ndom [nqm] | Riantana [ran] |  |  | Kimaama |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Ndom | Riantana | Kimaghama | Kaladdarsch | Teri-Kalwasch | Klader | Kimaam | Täri-Kalwa |
| 1 | ${ }^{\text {sas }}$ | mebob | növere | nuwwéda | dubbadnè | nüwoda | mübärä | newere |
| 2 | thef | enàva | kàvé | kawé | kabi | kawä | kawe | gawir |
| 3 | ${ }^{\text {ithin }}$ | pendö | péndji | pendsji | péndji | pändji | pintji | pendji |
| 4 | thonith | wēndö | jàndo | jándo | jándoe | jandoa | jaemdo | jamdo |
| 5 | merègh | mata | màdo | madoa | mando | madoa | mado | mado |
| 6 | mer | törwa | turò | toeroea | tulwa | turua | turo | terva |
| 7 | (mer) abo sas | mêbö be | ${ }^{\text {iburo növere }}$ | turrewahabé | dubbad-nènè | twuruaghawä | turoaidje | newänemä |
| 8 | (mer) abo thef | enàva me | ${ }^{\text {iburo kàvé }}$ | turrawendsji | kabiàmà | ibudapändji | turobindje | gawirmä |
| 9 | (mer) abo ithin | pendö me | iburo pérdji | turra éndoan | pandjimè | ibudajandoa |  | pendjimä |
| 10 | (mer) abo thonith | wēndö me | iburo jàndo | ketsja nda kawé | jándoemè | ibudamadoa | kitjanta kuwe | jamdomä |
| 11 | (mer) abo merègh | mata me | iburo màdo |  |  |  |  | madomä |
| 12 | mer an thef | törwa me | iburo turò |  |  |  |  | teroamä |
| 13 | mer an thef abo sas | $n \bar{z} / n \overline{1}$ mêbö | nî/nĩ növere |  |  |  |  | $n i$ |
| 14 | mer an thef abo thef | nı̄ enàva | $n i$ kìvé |  |  |  |  | ni-newere |
| 15 | mer an thef abo ithin | nī pendö | nĩ péndji |  |  |  |  | ningkawir |
| 16 | mer an thef abo thonith | nī wēndö | nĩ jàndo |  |  |  |  | nimpendji |
| 17 | mer an thef abo merègh | n̄̄ mata | nĩ màdo |  |  |  |  | ninijamdo |
| 18 19 | töndör töndör abo sas | nī törua taiötarö | nî turò |  |  |  |  | nimado |
| ${ }_{20}^{19}$ | töndör abo sas töndör abo thef | tarö/tarö mëbö tarö enàva | tjĩ növere |  |  |  |  |  |
| 21 | töndör abo ithin | tarö pendö |  |  |  |  |  |  |
| 22 | töndör abo thonith | tarö wēndö |  |  |  |  |  |  |
| 23 | töndörr abo merègh | tarö mata |  |  |  |  |  |  |
| 24 36 | töndör abo mer | tarö törwa |  |  |  |  |  |  |
| 36 40 |  |  | tjü kàvé |  |  |  |  |  |
| 60 |  |  | tjĩ péndji |  |  |  |  |  |
| 72 | nif thef |  |  |  |  |  |  |  |
| 80 100 |  |  | $t j \tilde{\imath}$ jàndo tĩ̃ mádo |  |  |  |  |  |
| 108 | nif ithin |  |  |  |  |  |  |  |
| 144 | nif thonith |  |  |  |  |  |  |  |
| 180 200 | nif merègh |  | tjũ iburo jàndo |  |  |  |  |  |

Figure 1. Map drawn based in information in Menanti and Susanto (2001) and Gordon (2005:801-880). Colours are according to obvious genetic groupings, as follows. Ndom, Kimaama-Riantana, Bulaka River (Yelmek and Maklew), Komolom (Koneraw and Mombum), Marind (Marind, Bian Marind and other languages not shown on map), Yei (Tanas-Bupul and Erambu-Poo), Moraori (Morori), Tonda (Sota, Smärky, Ngkâlmpw and Bädi Kanum, Guntai, Kunja, Blafe, Arammba and Wára) and Nambu (Neme, Nen, Nama, Namat, Namo).


## 3 Conclusion

We have traced the Kanum base-6 numeral system to the Tonda group specifically. We suggest that it arose for counting yams and then "climbed in" as a general purpose counting system. We provide glimpses of evidence for such stages - evidence which is hard to account for otherwise. Whether there is a historical connection with base- 6 systems of the Kolopom languages, near, but not adjacent, to the west, remains an open question. If there is a connection, it is areal rather than genetic, but sufficient evidence for a pre-historic areal connection remains to be amassed. Equally, if not more, puzzling would be the conclusion that there is no historical connection, as base- 6 counting systems are typologically very rare in the world as a whole. At the present state of data availability, we cannot go beyond such general directions, and, since there is no pre-20th century data, we may never be able to reach very deep into history.

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## Chapter VII $\mid$ Rarities in Numeral Systems

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# Rarities in Numeral Systems 

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#### Abstract

We present an extensive survey of rare structural properties in numeral systems in the world's languages, foremostly the question of rare number bases. The survey emphasizes comprehensiveness and status of evidence.


## 1 Introduction

The paper surveys rarities in numeral systems across the world. Space permits us only to look at the most conspicuous kinds of rarities that are featured in the vast set of languages in the world. The study aims at a high level of preciseness as to what counts as a numeral and what counts as rare, and doubtful cases will be treated pre-emptively in footnotes.

## 2 Numerals

### 2.1 What are Numerals?

In this paper, we define numerals as:

1. spoken
2. normed expressions that are used to denote the
3. exact number of objects for an
4. open class of objects in an
5. open class of social situations with
6. the whole speech community in question

With the first point we mean to disregard symbol combination systems, e.g., Roman numerals, that are confined to written communication (but, of course, essentially all of our primary data come from written representations of the spoken language).

The second point serves to exclude expressions that also denote exact numbers, but are not the normal or neutral way to say those numbers, e.g., 'eight-times-nine-and-another-two' for the normal 'seventy-four', but also to demarcate the area where the numeral system ends, which is, when there aren't any normed expressions.

As for the third point, languages usually have a rich set of expressions for inexact quantities, 'a lot', 'few', 'really many', 'about fifty' (but hardly *'about fifty-one') that have relatively high frequency in discourse. These are interesting in themselves but will not be included here because of their different fuzzy nature compared to exact number expressions.

Concerning the fourth point, some languages have special counting systems for a restricted class of objects (e.g., in Wuvulu (Hafford 1999:37-39) for counting coconuts). These can be quite idiosyncratic and since all languages which have exact enumeration must have a means for counting an open class of objects, it is preferable to study that, as it corresponds to a general kind of communicative need of a society.

The reason for the fifth point, the requirement on social situations, is to take a stand on so-called body-tally systems (cf. Lean 1992:2.4-2.6). A body-tallysystem may be defined as follows. Assume a sequence of body parts beginning with the fingers of one hand continuing with some points along the lower and upper arm, reaching one or more points of the head, then ending with the corresponding body-parts on the opposite arm and finally hand. A number $n$ is then denoted by the $n$th body-part-term in the sequence, e.g., 'nose' or 'elbow on the other side'. There are features that distinguish body-tally systems from other counting systems with etymologies from body parts. Non-body-tally systems use only fingers, toes, hands, occasionally eye and head, whereas bodytally systems always use some intermediate points, such as elbow, shoulder or nose, and let them form a sequential order from one side of the body to the other. Typically, body-tally systems are only used in special circumstances, such as bridal price negotiations, and in other cases you would use a different numeral system or not use exact enumeration at all. The information on the social status of the body-tally numeral systems is very incomplete; We can say that for the vast majority we do not have such information, but for those in which we do, the social situation restriction applies. Body-tallying has to be done on a physically present person and to understand what number is referred to the process must be watched, so, for instance, body-tallying numerals would be infelicitous when it is dark. For instance, de Vries (1998) found that bodytally numerals in a Bible translation could not be understood, i.e., were often mis-translated back to Indonesian by bilingual persons. Of course, there could be some other language(s), unknown to us at present, where body-tally numerals can be used in a fully open class of social situations; such a body-tally system would accordingly be included in the study. Body tally systems are attested
in abundance in Papua New Guinea and Indonesian Papua, in a geographically continuous area centered at the Ok family and, even if in decline, are still used today. Although many writers have neglected to mention it, there are also indisputable attestations of long extinct body-tally systems from Kulin (Pama-Nyungan, Australia) varieties in southeast Australia (Howitt 1889:317318) (Howitt 1904:697-703)!

Finally, regarding the sixth point, we are not interested in numeral systems which are particular to some small subsets of the speakers of the language in question (e.g., professional mathematicians) because such systems might not respond to the conditions and needs of the majority of a society.

Numerals provide a good testing bed for patterns across languages given their comparatively clear semantics and modularity. As to numeral semantics, languages may differ as to which quantificational meanings they express/lexicalize, notably in approximate numeration and whether a counted set of objects constitute a group or not, but these matters are minor compared to differences languages show, e.g., in verbal tense/aspect. Likewise, although not universally, numerals tend to have uniform, clearly identifiable, syntactic behaviour within a language. Also, if two languages have exact numeration for a certain range of numbers, one expects the two to give a similar functional load to these expressions, excluding possibilities such as numbers also being used for, say, colours or as metaphors significantly wider in one language or the other. This appears sound also in the light of the only corpus study of numeral frequencies in a language with a restricted numeral system - McGregor (2004:204) which shows that 'one' and 'two' in Gooniyandi (Bunaban, Australia) occur with comparable frequency to 'one' and 'two' in English.

### 2.2 Rareness

In this paper we present cases that are rare, either in that (a) they are present in few languages or in that (b) they are present in few geographical spheres. Most cases are of the (a)-kind, but for example, base-12 systems in northern Nigeria are present in relatively many languages, from several different families, but are confined to just this geographical sphere, so they are counted as rare in the sense of (b) only. Geographically separate instances are likely to be independent, and the bottom line is that we are interested in rare independent innovations - whether or not they have grown genetically or areally onto many languages.

### 2.3 Survey

Lots of data is available in one form or another for numerals. It seems that numerals together with pronouns, kinship terms, body part terms, and other basic vocabulary (sun, water, etc), and perhaps "sketchy" phonological inventory, are the parts of language where there exists empirical data for a really large subset of the world's known languages. One may legitimately ask just how large this subset is when it comes to numerals - for how many languages do we have data
on numerals? Let's say we count about 7000 attested native spoken languages for the world. A definite lower bound is 3880 , since we can produce a list of references to numeral data from 3880 definitely distinct languages. An upper bound is harder to give. We entertain the rather time-consuming methodology of trying to obtain every first-hand descriptive data reference found in any handbook or relevant publication whatsoever. The survey in the present paper is based on the data we have collected so far. We currently have about 13500 references, some describing numeral systems of many languages in the same publication, and, with 7000 languages in the world, many different publications describe the same language. (The fact that often there is more than one independent source for one and the same language helps us to determine the accuracy.) It is impossible at this point to say how many languages the sources account for since they attest dialectal varieties, varieties from the same location but different centuries, partial data, data of varying quality, duplicated data, etc. However, at least one language from every attested language family or isolate is included in the survey (if numeral data is at all attested for the family in question).

In addition to first hand sources, we have also drawn inspiration from the rich existing literature on numerals in general. The subject, in fact, goes back more than 200 years in time - the first major work being the remarkable Aritmetica Delle Nazioni by Hervás y Panduro (1786). Since then, our bibliography counts some 20 PhD :s, over 100 further monographs and $700+$ articles to have appeared. These range from purely descriptive accounts to areal, comparativehistorical, typological, and deep syntactic studies - solely devoted to spoken language numerals as defined above. (The literature on written symbol systems for mathematics is even more voluminous.) However, since most of the literature just re-hashes the same data, the recourse to first-hand sources is essential in order to understand the true diversity in numerals in the world's languages.

## 3 Rarities

### 3.1 Rare Bases

Perhaps the most salient single characteristic of a numeral system is its base, or more correctly speaking, its set of bases. The set of bases of a natural language numeral system may be defined as follows.
the number $n$ is a base iff

1. the next higher base (or the end of the normed expressions) is a multiple of $n$; and
2. a proper majority of the expressions for numbers between $n$ and the next higher base are formed by (a single) addition or subtraction of $n$ or a multiple of $n$ with expressions for numbers smaller than $n$.

This assumes that for any expression the linguist can unambiguously analyze each numeral expression into its constituent parts (or analyze it as consisting of only one part). As an example, for Swedish we would begin by finding the biggest part of the highest normed expression, which according to our own knowledge is miljard $\left(10^{9}\right)$. Thereafter we can find the next lower base by trying divisors $x$ of $10^{9}$ to see if the numbers between $x$ and $10^{9}$ are expressed in the required form. For example, $x=5 \cdot 10^{8}$ is not, because we do not say ${ }^{*}$ en-halvmiljard plus ett (*half-a-billion plus one) or the like for $5 \cdot 10^{8}+1$ or any, let alone a majority, of the numbers between $5 \cdot 10^{8}$ and $10^{9}$. However, 'miljon' $\left(10^{6}\right)$ fulfils the requirements, and, continuing with the same analysis for lower and lower numbers, we arrive at the conclusion that Swedish has $\left\{10,10^{2}, 10^{3}, 10^{6}, 10^{9}\right\}$ as its set of bases.

The definition of base as stated gives unambiguous decisions for formations which are sometimes (and sometimes not) called base by other authors; systematic subtractions, special lexemes for base-multiples, or isolated cases of addition, e.g., only $7=6+1$ but otherwise no additions involving 6 . Examples of such cases and their systematic resolution with our definition are given in Table 1) It is important here to note that there doesn't have to be a monomorphemic word for something that is a base. In the case of Kare, at least if we assume that the numbers above 20 are formed parallel to 30 , then 20 is a base. Further, 10 or 15 are not bases even though the words for them monomorphemic the definition interprets them as special words for multiples of 5 , just like some base-10 systems have monomorphemic words for $20,30, \ldots, 90$.

The expression 'base- $x$ system' will be used to mean that ' $x$ is in the set of bases' for the numeral system in question. Similarly, 'base- $x_{1}-\ldots-x_{n}$ ' system will mean that all of $x_{i}$ is in the set of bases, without any commitment that the $x_{1}, \ldots, x_{n}$ exhaust the set of bases.

## No Base

There are a number of languages for which there is an explicit statement in the descriptive literature that they lack (exact) numerals above one:
Nadëb (Nadahup, Brazil): According to Weir (1984:103-104), the words for 2 and 3 are inexact. The vocabulary of a closely related variety lists completely different words for 1-3 (Schultz 1959) and the study by Münzel (1972) lacks information on numerals (cf. Epps 2006:263). We have not seen the wordlist collected by Natterer (Koch-Grünberg 1906:881), though this might not include numerals anyway.

Pre-contact Jarawara (Arawán, Brazil): According to Dixon (2004:559) and indeed the only other published wordlists for Jarawara (and closely related varieties) show some overlap between forms for 2 , 3 , 'few' and 'many' (Anonby and Anonby 2007:25).
Pre-contact Yuqui (Tupi-Guaraní/Tupí, Bolivia): According to Villafañe (2003:68). As far as we are aware, there are no other published descriptions of this language that include the numerals.

|  | LutuamiKlamath-Modoc, USA(Dixon and Kroeber 1907:673) |  | NyokonBantoid/Atlantic-Congo. Cameroon(Richardson 1957:30) |  | Kare <br> Bantu/Atlantic-Congo, Sudan <br> (Dijkmans 1974:147) |  | Ainu <br> Isolate Japan (Refsing 1986:110) |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |  |  |  |
|  | Analysis | Expression | Analysis | Expression | Analysis | Expression | Analysis | Expression |
| 1 | 1 | nas | 1 | ámò | 1 | emotí | 1 | sine |
| 2 | 2 | lap | 2 | àfóò | 2 | ibili | 2 | tu |
| 3 | 3 | ndan | 3 | átár | 3 | etotu | 3 | re |
| 4 | 4 | umit | 4 | ánnìs | 4 | biu | 4 | ine |
| 5 | 5 | tunip | 5 | átóòr | 5 | etano | 5 | asikne |
| 6 | $5+1$ | nas-ksapt | 6 | át $\int$ ín | $5+1$ | etano na emoti | 10-4 | iwan |
| 7 | $5+2$ | lap-ksapt | $6+1$ | átfán námò | $5+2$ | etano na ibili | 10-3 | arwan |
| 8 | $5+3$ | ndan-ksapt | ? | áyáá nì màn | $5+3$ | etano na etotu | 10-2 | tupesan |
| 9 | 10-1 | nas-xept | $8+1$ | áyáá nì màn námò | $5+4$ | etano na bînu | 10-1 | sinepesan |
| 10 | 10 | te-unip | 10 | àwát | 10 | la-ato | 10 | wan |
| 11 | 10+1 | taunep-anta nas | 10+1 | àwát ámò | 10+1 | laäto na emoti | 10+1 | sine ikasma wan |
| ... | $\ldots$ | ... | $\ldots$ | ... | $\ldots$ | ... | $\ldots$ | ... |
| 15 | $\ldots$ | ... | $\ldots$ | ... | 15 | sanga |  |  |
| 16 | $\ldots$ | $\ldots$ | $\ldots$ | $\ldots$ | $15+1$ | sanga-na-emoti |  |  |
| ... | $\cdots$ | $\cdots$ | $\cdots$ | $\cdots$ | $\ldots$ |  |  |  |
| 20 | 2x10 | lap-eni taunep | 20 | nìt $\int$ én | 2x10 | atumbili | 20 | hot |
| 21 | $2 \times 10+1$ | lap-eni taunep-anta nas | $20+1$ | nìt $\int_{\text {cín }}$ ámò | . . . | ... | $20+1$ | sine ikasma hot |
| $\ldots$ | $\cdots$ | $\cdots$ | $\cdots$ | $\cdots$ | $\cdots$ | . |  |  |
| 30 | $3 \times 10$ | nda-ni taunep | 3 x 10 | àwát átár | $2 \times 10+10$ | atumbili na laato | $20+10$ | wan e tu hot |
| $\ldots$ | . $\ldots$ | ... | ... | $\ldots$ | . | . | .. 2x20 | m tu hot |
| Base |  | 5-10 |  | 10 |  | 5-20 |  | 5-10-20 |

Table 1. Examples of formation types and outcomes of the definition of base (see text).

Canela-Krahô (Jê/Jê-Jabutí, Brazil): According to Green (1997:181). As far as we are aware, there are no other published descriptions of this variety that include the numerals.

Krenák (Aimoré, Brazil): According to a synthesis of earlier data by Loukotka (1955:125-126) which follows observations such as Renault (1903:1111). Even if there were no normed oral expressions, small numbers could be communicated using fingers on the hand (Ehrenreich 1887:41-46).

Parintintin (Tupí-Guaraní/Tupí, Brazil): According to Nimuendajú (1924:240241). Indeed, the larger dictionary by Betts (1981) agrees that the word frequently glossed as 'two' (cf. Sampaio 1997:57-58) actually has an inexact meaning.

Wari’(Chapacura-Wanham, Brazil): According to one vocabulary collected by Hanke (1956). A later, more extensive, description of a variety in the same dialect cluster does show a word for 'two' albeit glossed literally as 'facing each other' (Everett and Kern 1997:452-459). An attempt at documentation of the most closely related language, the moribund Oro Win, failed to uncover any number words (Popky 1999:38).

Chiquitano (Isolate, Bolivia): According to Adam and Henry (1880:19) which is corroborated by d'Orbigny (1839:163) and Clark (1937:118-119,138) and several later attestations of Chiquitano dialects show Spanish Nordenskiöld 1911:232) (Nordenskiöld nd) (Tormo 1993:15,108) or Portuguese (Santana 2005:94) loans for 'two' and above. However, there are also dialects where a native term for 'two' is attested (Montaño Aragón 1989:335-400).
"All" Campa and Machigenga groups (Pre-Andine/Arawak, Peru): According to Wise and Riggle (1979:88). As far as we are aware, published vocabularies (too many to list) show little indication that the words given for 'two' (and sometimes above) are in reality inexact. However, Wise and Riggle (1979) did work with basic mathematics education among these groups and therefore their judgement is arguably deeper.
Culina (Arawán, Peru): According to Wise and Riggle (1979:88). Unfortunately, we have not had access other materials on either Brazilian or Peruvian Kulina to double check the claim.
Arabela (Zaparoan, Peru): According to Wise and Riggle (1979:88), though the later, quite extensive dictionary of Rich (1999) does show distinct expressions for 'two' and 'three'. Possibly, Wise and Riggle (1979) who did work with basic mathematics education looked at these expressions and their meaning more closely.

Achuar (Jivaroan, Ecuador): According to Wise and Riggle (1979:88), though later more extensive descriptions show expressions for 'two' and higher numerals (Fast and Fast 1981:58-59) (Fast et al. 1996). It is possible that expressions for 'two' and higher numerals crystallized as a result of increased
contact with a counting culture (Gnerre 1986) or even reflects normative rather than descriptive usage. Therefore, Wise and Riggle (1979) who did work with basic mathematics, could very well be descriptively more accurate for the traditional state of the language.

Fuyuge (Goilalan, Papua New Guinea): One early description of Fuyuge says that the 'two' word is also used for a small number (Ray 1912:313314). However, there is a word listed as 'three' but no explicit statement to the fact that this, like 'two', also has an inexact meaning. A very small vocabulary, probably collected by the same person lists $1,2,2+1$ and no further comments (Fastre 1920:116), and the later, more modern description by Bradshaw (2007:45) attests a native $1,2,2+1,2+2, \ldots$ system.

Viid (Border, Indonesia): In one wordlist (a.2) of Viid from Senggi (Smits and Voorhoeve 1994:211-212), 'tambla' is listed both with the meaning 2 and 3, but this is not borne out in other early wordlists (Smits and Voorhoeve 1994:211-212) or the more recent (Menanti 2005), which have $3=2+1$.

Gedaged (Oceanic/Austronesian, Papua New Guinea): Nikolaj von MikluchoMaclay, a pioneer researcher on the Rai-coast of Papua New Guinea, reports that (von der Gabelentz and Meyer 1882:503):

Sehr viele Papuas kennen die Zahlwörter ihres eigenen Dialektes nicht. In Mitebog [a village speaking a dialect of Gedaged - HH] fragte ich fünf oder sechs Eingeborene, aber die Angaben waren widersprechend und jedenfalls unrichtig, nur olam (eins) konnte ich als sicher notiren [sic!].

One interpretation of this statement is that there was no normed expression for numerals above one in the lect of Mitebog. A later, longer description of a different dialect shows monomorphemic numerals 1-5 inherited from Austronesian (Dempwolff nd:36-37).

To lack numerals above one means that the normed expressions for the quantities above one are inexact. We may call such systems 1-few-many for the time being. In these languages, it may be possible to communicate a higher exact quantity successfully, perhaps using gestures, context, one-to-one pairings, repetition or a specialized lexical item e.g., 'twin' for a certain kind of exact quantity. However, in these languages, the normed expressions are still 'one', 'a few', 'many', ... when these quantities occur in discourse. In no case does it appear to be possible, or normed, to say few $+1,1+1$ or few + few to designate an exact number, so there is no base.

From the above cases, one certainly gets the impression that there is a thin line between 1-few-many systems and 1-2-many systems. In some cases, different observers on the same language variety differ as to whether the 'two'-word is approximate or exact in meaning. In other cases, the speech community seems to have acquired norms for number expressions over time. One may then conjecture that many more 1-few-many systems would have been found if more
languages had been documented in detail before extensive contact with modern society 1 It is also apparent that questions on this level of granularity are
${ }^{1}$ Further cases may include the following. 1. Aikhenvald and Dixon (1999:358) conjecture that Djeoromitxí (Jabutí/Jê-Jabutí, Brazil) "originally had no numbers" since the word $j e-b o$ for 'two' given by Pires 1992:66) is from a root with the meaning to 'be equal'. However, an etymology for 'two', even if correct (cf. van der Voort 2004:212 and van der Voort 2007: 162) does not automatically mean that there was no original word for 'two', nor that a present meaning of 'two' (Ribeiro 2008:42) is somehow subordinate to the etymological meaning. Also, early attestations of yawo yawo (2+2) for 4 in Loukotka 1963:50) speaks against an inexact meaning for 'two'. 2. Barriga Puente (1998:132,263) reports that Esmeraldeño (Isolate, Ecuador) has a limit of counting at one, based on a misreading of Lehmann (1920:37). There is only one vocabulary of the now extinct Esmeraldeño which has been reprinted a number of times Adelaar 2004:155-161). However, the earliest of these publications (Wolf 1892:528) is clear that the lack of native Esmeraldeño words above one could be due to the memory of the last speaker(s). So we are not in a position to assert that Esmeraldeẽno ever lacked numerals above one. 3. Koch-Grünberg (1928:316) describes numerals in Sapé (Isolate, Venezuela) as 1 'meyakán' and 2 'meyakán' and remarks "Die Kaliána haben nur ein Zahlwort und gebrauchen stets denselben Ausdruck, in dem sie dabei an den Fingern und dann an den Zehen weiterzählen". It's not clear what to make of this, but, in any case, the only other two published vocabularies do show distinct words for lower numerals (de Matallana and de Armellada 1943, Migliazza 1978) and Koch-Grünbergs vocabularies contain other cases of puzzling numeral elicitations (Zerries and Schuster 1974:56). 4. It is hard to know whether the Guayakí variety recorded from two youths by Vogt extended to a whole community of speakers (Vogt 1903:861) and another attestation from roughly the same time appears to give forms for exact 1 and 2 (Mayntzhusen 1920:20), though it may be that these forms are etymologizable Vellard 1935). 5. On the grounds that the present-day numerals can be etymologized to 'that', 'pair/couple', 'few' and 'another', proto-Tupi Schleicher 1998:12-13) may be argued to lack numerals. 6. A vocabulary of Ofaye has 1 hœhá, 2 ñokoádi, 3 ñokoádn 4 ñokoádi (Hanke 1964:29), i.e., 2 is the same as 4. A good guess, following more recent documentation das Dores de Oliveira 2006:109110), is that the 4 in this earlier vocabulary is simply an error of some kind. 7. Bernatzik (1942) claims that Yumbri lacked numerals above one. There is no further material on this variety but the closely related Minor Mlabri (Rischel 1995) has numerals up to three. Bernatzik's account has a sweeping and condescending flavour, and also has other doubtful claims of the same kind, e.g., lack of fiction which does not hold for Minor Mlabri either (cf. Velder 1963:15). Another complicating factor is that he is able to discuss twin births at length with the people he says cannot comprehend any more distinctions than 'one' and 'many'. 8. The oft-repeated claim Parker 1909:85) of lack of numerals in Vedda (Unclassified, Sri Lanka) appears, on closer scrutiny of the underlying sources, to be hearsay Seligmann and Seligmann 1911:33,412). The only thing we can say is that no native term above two is could be collected from the memories of the descendants, which does not necessarily mean that none existed. 9. The first record of the language of Utanata (Asmat-Kamoro/Trans New Guinea, Indonesia) indicates counting inability on the part of the inhabitants (Earl 1837). However, lower numerals are attested in all subsequent descriptions - especially the most extensive piece Drabbe 1953) - and have cognates in other Asmat-Kamoro languages (Galis 1955). Therefore, the counting inability reported probably reflects some kind of misunderstanding in the midst of the very difficult communication circumstances. 10. Grondona 1998:91) conjectures that pre-contact Mocoví (Guaicuruan, Argentina) lacked numerals above one as 2 and above are Spanish loans ("It seems that Mocoví lacked numeral forms, and has borrowed all its numerals from Spanish"). While it is true that Mocoví borrowed 2 and above from Spanish (cf. Gualdieri (1998:211-212) and for the related Pilagá (Vidal 2001:129)), it does not necessarily follow that Mocoví lacked 2 and above, before the borrowing. Older sources do, in fact, consistently attest a specific form for 2, see Koch-Grünberg (1903:112-124) as well as Lafone Quevedo 1893:244) and Lafone Quevedo (1892:410). 11. Paiconeca (Bolivia-Parana/Arawakan, Bolivia) is a poorly attested extinct language of presumed Arawakan affiliation (Montaño Aragón 1989:161-
almost beyond the scope of classical forms of language documentation. Of languages potentially showing 1 -few-many systems or 1-2-many systems only two, Mundurukú (Mundurukú/Tupí, Brazil Pica et al. 2004) and Pirahã (see below), have been subject to investigations approaching standards of experimental psychology.

There are two further languages in the Amazon, Pirahã (Mura-Pirahã, Brazil) and Xilixana (Yanomama, Brazil) that stand apart from the above 1-few-many systems in that they are argued to lack all exact numerals, i.e., there is no normed way to denote an exact quantity even for 'one'.

In Pirahã, there are two words which prototypically mean 'one' and 'a couple' respectively, but it has been checked fairly extensively that their meanings are fuzzy 'one' and 'two' rather than discrete quantities (Everett 2005, 2004, Frank et al. 2008). It is not possible to combine or repeat them to denote higher (inexact?) quantities either (Gordon 2004). The Pirahã have the same cognitive capabilities as other humans and they are able to perform tasks which require discerning exact numeration up to the subitizing limit, i.e. about 3 (Gordon 2004). They just do not have normed expressions even for low quantities, and live their life happily without paying much attention to exact numbers. It does not appear to be possible to express an exact quantity simply by repeating an expression the appropriate number of times, like one can and often does in, e.g., Sanuma (Yanomama, Brazil) for 2 and 3 Borgman 1990:152). If one says "I'll be back after it gets dark and it gets dark again" this might just as well be interpreted as two days or as three days (p.c. Daniel L. Everett 2005). It seems relevant to note that Pirahã grammar lacks singular-plural distinctions of any kind, even in pronouns (p.c. Daniel L. Everett 2008). A wordlist of the only known relative of Pirahã, the extinct Mura languag\& ${ }^{2}$, features words glossed 'one' and 'two' (Nimuendajú 1932, Nimuendajú and do Valle Bentes 1923). The 'one'-word is an obvious cognate to the Pirahã fuzzy one, and the 'two'-word is an obvious loan from some Tupi language.

Xilixana is the language of a group which has been on the Mucujai river at least for the past century. In modern divisions, it is sorted as a dialect of Ninam, also known as Yanam or Central Ninam (superseding Southern Ninam in older

[^28]terminology) (Migliazza 1972). Swain (2000) $3^{3}$ describes Xilixana numerals as not even having an exact 'one':
'one' mõli Note: Means one or a few.
'two' kup; yalukup Note: Means two or a few.
'three' pək Note: Can refer to any number more than two or a few.
John Peters, the first missionary to live among the same group, also describes the same expressions as having inexact value and adduces that "exact numbers were not important" (Peters 1998:52). The closest other Yanomami variety for which there is a grammar is the dialect Shiriana, of the Uraricoera, to the north (Gómez 1990). This describes the numerals 'one' and 'two' as exact, but the author only spent 14 weeks in the field. Also Migliazza (1972:117-118,422), who spent many years in all of the Yanomama territory, describes Shiriana lower numerals as exact in the numerals section of his thesis and, in fact, all other description of Yanomama languages we have been able to consult describe 'one' and 'two' as exact (Ramirez 1994b, a, Zerries and Schuster 1974, Becher 1960, Knobloch 1967, Vinci 1956, Wilbert 1962, de Matallana and de Armellada 1943, Koch-Grünberg 1928, Mattei-Müller 2007). Also, most Yanomama varieties have singular, dual and plural but we do not know the precise status of Xilixana, and if so, if they are inexact as well. However, on one page Migliazza 1972:38) the \#moli word is glossed as 'one, few' (in contrast to pages 117-118 and 422). This is significant because language descriptions rarely claim 'one' and 'few' overlap in meaning, and now three independent observers do it for the same or nearly the same language. Carole Swain was a UFM/MEVA missionary who lived with the Xilixana for very long periods of time in the 70-90s and therefore she is certainly not a superficial observer. The Xilixana were monolingual (except for an occasional captured Dekwana) and uncontacted by modern society up to at least 1957 (Early and Peters 2000).

## Base-3

Base-3 appears to be rarer than base-4. We have found only a few cases $\frac{4}{4}$, some of them somewhat sporadic within their respective dialect cluster:

Ambulas of Wingei (Ndu, Papua New Guinea): An Ambulas dialect survey (Wilson 1976:57) mentions that the variety of Wingei counts in units of three, and the actual forms can be found in Wilson (1989a:16-17). The forms are reproduced in Table 2 Presumably, this is the same case that Laycock (1970) refers to when speaking (without forms given) of base-3-6-24 system(s) in the Ndu family, citing personal communication from

[^29]Anthony Forge. The etymology of the forms reveal that the system is much like a commonplace $5-10-20$ or $5-20$ system except that the hand is seen as having six features! At the time of elicitation only older people knew the indigenous system, whereas the young used Tok Pisin or English for higher numerals. Other, better described, varieties of Ambulas (Wilson 1976, 1980) show no base-3 and comparative evidence shows that the original Ambulas (1-3) and Ndu (1-2) system were restricted (Aikhenvald 2008:595, Laycock 1965:173-174).

Waimirí of Atroarí (North Amazonian Carib/Cariban, Brazil): Base-3 counting could be used up to about 9 according to Green (1997:6-7) , who cites personal communication with Ana Carla de Bruno Santos. However, the more recent grammar by Bruno (2003:140-142) states that Portuguese loans are used above 3 and is silent about a possible base- 3 alternative.

Som (Finisterre-Huon/Trans New Guinea, Papua New Guinea): According to Smith (1988:29) base-3 counting can be used up to about 9. We know of no other description of this variety.

Bine (Eastern Trans-Fly, Papua New Guinea): In at least on vocabulary repoduced in Wolfers (1972:218) and Wolfers (1971:79), a variety of Bine is base- 3 and reaches up to 9 . However, all other attestations of Bine show only a restricted system and/or a body-tally system (Lean 1986d), including the lengthiest description (Fleischmann and Turpeinen 1975: 16). The base-3 vocabulary must therefore be considered somewhat dubious.

Bukiyip (Arapeshan5, Papua New Guinea): Fortune (1942:58-60) describes the Rohwim dialect of Mountain Arapesh to have a base-3 system for counting some objects and a base-4 system for counting other objects, which seems to have reached up to 24 . A later description of an inland Bukiyip (Conrad and Wogiga 1991:73-76) variety shows a conflation of the two systems (with no indication of them being used for different objects). Robert Conrad submitted the base-3 system for the entry on Bukiyip (dialect not indicated) on Numeral Systems of the World's Languages websit ${ }^{[6]}$. Available data on other Arapeshan languages, such as Abu' Arapesh (Nekitel 1985:82-84) and Mufian (Conrad et al. 1978:104), show base-5, at least from 7 and up.

## Base-4

Base-4 systems are attested on four continents:
North America: Some extinct Chumash languages (Chumashan, USA) show original base-4 systems, running up to 32 (Mamet 2005:113-115) (Beeler 1967, 1963, Hughes 1974). Base-4-8 is also documented with the older generation in the now extinct Yuki (Isolate, USA). For Yuki, Kroeber (1925)

[^30]|  | Wingei | Maprik | Wosera-Mamu | Wosera-Kamu-K |
| :---: | :---: | :---: | :---: | :---: |
| 1 | nawurak | nakurak | vétik | vétik |
| 2 | vétik | vétik | vétik | vétik |
| 3 | kupuk | kupuk | kupuk | kupuk |
| 4 | kupukiva | nakwasa/wan vétik wan vétik | vétik vétik | vétik vétik |
| 5 | kupuk'etik | naktaba | taambak | taambak |
| 6 | taabak | naktaba sékét naktaba nakurak |  |  |
| 7 | taabak kaayek | naktaba sékét naktaba vétik |  |  |
| 8 | taabak kaayek vétik | naktaba sékét naktaba kupuk |  |  |
| 9 | taabak kaayek kupik | naktaba sékét naktaba kupuk wan vétik wan vétik |  |  |
| 10 | vétik taaba vétik | taaba vétik |  |  |
| 11 | nawurak taaba vétik | taaba vétik sékérék maan-ba kayék nakurak |  |  |
| 12 | taaba vétik | taaba vétik sékérék maan-ba kayék vétik |  |  |
| 20 |  | maan vétik taava vétik | nakurak mi | nakurak dumi/maan vétik taaba vétik |
| 24 | nawura mi |  |  |  |

Table 2. Numerals in Wingei Ambulas (Wilson 1989a: 16-17), Maprik Ambulas (Wilson 1980), Wosera-Mamu Ambulas from around Serangwandu (Wilson 1989b:15) and Wosera-Kamu-K from around Kunjingini (Wilson 1990:15). Etymologies of roots are as follows \#maa is 'foot, leg', \#taaba is 'hand, arm', \#mi is 'tree' and \#du is 'man'. Apparently, in Wingei counting, the hand is seen to have six features. The etymology of the expresssion nawura mi/nakurak $m i / n a k u r a k$ dumi is not clear but it may have to do with either tree (typologically unusual but matches $m i$ ) or man (typologically very common, but resembles only dumi).
describes how base-4 is related to hand-counting by considering the spaces between the fingers (cf. Hinton 1994) $]^{7}$. The Chumashan languages and Yuki are both in California but quite distantly apart, with Yuki in the north and Chumashan in the south, and other language families intervening.

South America: The extinct Lule (Isolate, Argentina) of Clark (1937:102) and Machoni de Cerdeña (1732:84-86) as well as the poorly attested extinct Charrúa (Charruan, Uruguay) reported in (Ibarra Grasso 1939b: 202) appear to have had base- 4 up to 10 , at which point the system turns into a commonplace 5-10-20 system with hands and feet. It cannot be inferred from the data hand that there was ever true base- 4 system here, beyond 10. A couple of descriptions of a Guaraní variety in Paraguay (TupíGuaraní/Tupi, Paraguay) show base-4 up to 10, but the expressions for numbers above 10 are not shown (Ibarra Grasso 1938:278) (Ibarra Grasso 1939a: 590). Other old and new descriptions of any varieties of Guaraní (too many to list) do not show any traces of base-4. Isolated vocabularies of Mocovi and Toba (Guaicuruan, Argentina) show base-4 up to 8 and 10 respectively (Koch-Grünberg 1903:114-124), but the vast majority of vocabularies for these languages (too many to list) show no trace of this. The extinct Payaguá (Isolat ${ }^{8}$, Paraguay) has one attestation with alternative base-4 forms up to 20 (Koch-Grünberg 1903:114-124). All these cases occur within a relatively small area of South America, but there is otherwise little evidence for an areal connection.

Indonesia/Papua New Guinea: An indeterminate number of languages in the highlands have a variations of a base-4 system (Lean 1986a, c, 1992:13-86,15-59,Ch. 5), where at least one, Kakoli (Hagen/Trans New Guinea, Papua New Guinea) is attested with as base 4-24 (Bowers and Lepi 1975). Kewa (Engan/Trans New Guinea, Papua New Guinea) has several parallel numeral system, one of them being base-4 (Franklin and Franklin 1962) and goes at least up to 20 , and beyond that it may be combined with a body-tally system to form higher numbers in units of four Pumuge 1975). The word for ' 4 ' is 'hand', i.e., four fingers constitute one hand and the thumb is separate. The traditional counting system of Mbowamb (Hagen/Trans New Guinea, Papua New Guinea) near Mt. Hagen has been been described with a fair amount of detail. It is clearly a $2-4-8$ system, for which Vicedom and Tischner (1948:268-270) gives expressions up to 24 , and says the system can be used up to about 80 . Another description seems to indicate that after 20, counting can be done in units of 20 (Strauss 1962:315-318), cf. also Lancy and Strathern (1981). As in Kewa, the base4 is connected with counting the fingers of one hand, the thumb counted separately. The origin of the highland base-4 system(s) has not been

[^31]systematically investigated, but given the geographical proximity and the fact that the Engan and Hagen languages are not closely related, an areal connection seems likely even if this is not directly observable in the forms in question.
On the north coast, around the border between Indonesian Papua and Papua New Guinea, base-4 is also present variously in the Sko languages (most of the data is collected in Lean 1986b), - see Donohue (2008) for a good attestation of 4-12-24 in Skou - as well as 4-24 in Tobati (SarmiJayapura Bay/Austronesian) for which the best attestion is Moolenburgh (1904). Given the proximity of the languages and the fact that they are genetically unrelated, there is almost certainly an areal connection between base-4 in Skou and the Sarmi-Jayapura Bay Oceanic languages.

Africa: An indeterminate number of languages in the northeastern Democratic Republic of the Congo (DRC) have (traces of) a base- 4 system. The first attestation appears to be a Nyali (Bantu, DRC) variety for which Stuhlmann (1894:624) notes that $8=2^{*} 4,9=2 * 4+1,13=12+1,14=12+2$, $16=2 * 8,17=2 * 8+1$ but $20=2 * 10$. Later reports of related Bantu varieties show that there was/is a fully systematic $4-24$ or 4 - 32 underlying these forms van Geluwe 1960, Kalunga Mwela-Ubi 1999, Bokula and Ngandi 1985). Furthermore, thanks to Kutsch Lojenga (1994:353-357), we have a full attestation of almost obsolete Ngiti (Lendu/Central Sudanic, DRC) and Lendu (Lendu/Central Sudanic, DRC) 4-32 systems (p.c. Constance Kutsch Lojenga 2007). Various wordlists attest traces of the same base-4 systems in decay or amalgamation with base-10 and base-20 in closely related Bantu and Central Sudanic languages (Johnston 1922b, Struck 1910, Johnston 1904, Bokula 1970, Harries 1959, Loienga 1994, Schebesta 1966, 1934, Asangama 1983, Czekanowski 1924, Stuhlmann 1917) and unpublished SIL survey lists.

In addition, there are a number of languages which have been claimed to be base- 4 in the literature but which are not base- 4 according to the definition used in this paper. We will mention a few of the most important ones here. The language called Āfúdu (Unassignedg, West Africa) by Koelle (1854) uses some additions with 4 in the numbers below 10 but is decimal in the range 10-20. Bodo and Deuri (Bodo-Garo/Sino-Tibetan, India) have vestiges of base- 4 counting extending higher than 20 and Bai (Bai/Sino-Tibetan, China) is documented with a base-4-16-80 system for shell money in medieval times (Mazaudon 2007). Yiwom (West Chadic A/Afro-Asiatic, Nigeria) has $7-9$ as $4+3,4+4,4+5$ but no other forms are based on 4 (Ibriszimow 1988). de Castelnau (1851a:1013) reports base-4 (actually base-2-4) in Apinayé (Jê/Jê-Jabutí, Brazil) but no actual forms are given (de Castelnau 1851b:270-274) and is likely to be spurious in the absense of corroborating data in this rather well-documented language (too many references to list). Base- 4 for counting special objects is widely

[^32]attested in the Oceanic languages of Melanesia (Kolia 1975, Friederici 1912, Parkinson 1907).

## Base-6

Base-6 systems are attested on Kolopom island (formerly Frederik-HendrikEiland) in southwest Indonesian Papua, as well as in the Kanum and Nambu languages in southern New Guinea around the Indonesian-Papua New Guinea border. Their origins have been discussed extensively (Donohue 2008, Evans 2009, Hammarström 2009, Plank 2009) and need not be repeated here.

In addition, there are a number of languages which have been claimed to be base-6 in the literature but which are not base- 6 according to the definition used in this paper (cf. Plank 2009, Gamble 1980, Beeler 1961, Ibarra Grasso 1939b). A few require comment. One early attestation of Balanta (Northern Atlantic/Atlantic-Congo, Senegal/Guinea Bissau) has additions of 6 for the numbers 7-12 (Koelle 1854). But since we do not know the continuation beyond 12, it is unsure whether the $6:$ s generalize (cf. Wilson 1961a). Also, later attestations give different, non-base-6, forms (Wilson 1961b, Quintina 1961, Fudeman 1999). Similarly, Less Traditional Tiwi (Isolate, Australia) may have formed some numbers in the range 7-10 with 6 (Lee 1987:96-100), but not further.

## Base-8

Northern Pame (Otopamean/Otomanguean, Mexico), the sole case of a base-8 language (attested up to 32) which does not have 4 as a sub-base is presented and discussed in Avelino (2006), though 5-8 have etymologies which involve 5.

## Base-12

Dhivehi (Indo-Aryan/Indo-European, Maldives) has an early attested (Gray 1878) but long extinct base-12 which is attested up to 96 thanks to the efforts of Fritz (2002:107-123) 10 Apart from that case, there are base-12 systems in the Plateau area of northern Nigeria. The first known attestations of such systems 11 come from the famous Polyglotta Africana by Koelle (1854) which includes numerals 1-20 in a number of West African languages and the first proclamation of duodecimality as a system appears to be Schubert (1888). As

[^33]shown in Table 3, we have tried to collect all independent attestations that have been published, or, unpublished but available on the internet ${ }^{12}$ However, not all of them are necessarily independent as this information is not always deducible from the text. It is likely that there are a few more attestations in publications that we do not have access to. For many, if not all, other sources on the same varieties attest base-10 rather than base-12, which means that the base-12 systems are currently under pressure.

[^34]Table 3. Published attestation of base-12 systems in the Plateau area. 12-144 means that the attestation gives forms $\leq 12$, forms $12+\mathrm{x}$, multiples of 12 , and a word for $144 ; 12+$ means forms $\leq 12$ and forms $12+$ x or multiples of 12 ; $\leq 12$ means forms $\leq 12$; " 12 " means that the source simply states that there was a "duodecimal system" but gives no forms; Cont.-10 means an attested 10system contaminated by forms following a "duodecimal system" and Spec.-12 means that some duodecimal connection is speculated. Further half-attestations are as follows. Arago (base-10 in Judd 1923), Kagoma and Agatu were judged "uncertain" by Thomas (1920a). Gwara, a Margi variety (Biu-Mandara A/AfroAsiatic, Nigeria) has monomorphemic 1-10 and forms 11-12 with formations that may include 1 and 2 - a bit like Germanic - but there is otherwise no reason to suspect base-12 counting (Wolff 1975).

| Language | Source | Type | Family | Comment |
| :---: | :---: | :---: | :---: | :---: |
| Ake | Blench 2006a | $\leq 12$ | Plateau |  |
| Afo | Bouquiaux\|1962 | "12" | Plateau |  |
| Afo (Apho) | Schubert\|1888 | "12" | Plateau |  |
| Afo (extinct Afu) | Thomas 1920a | "12" | Plateau |  |
| Afo | Meek\|1925:142-143 | $12+$ | Plateau |  |
| Afo (Eloyi) | Mackay 1964, Armstrong <br> 1983 , | $12+$ | Plateau |  |
| Aten | Blench 2006d | $\leq 12$ | Plateau |  |
| Aten (Ganawuri) | Bouquiaux 1964, 1962 | 12-144 | Plateau |  |
| Aten (Ganawuri) | Meek\|1925: 142-143 | $12+$ | Plateau |  |
| Birom | Bouquiaux 1970 | 12-144 | Plateau |  |
| Birom | Thomas 1920b | "12" | Plateau |  |
| Birom (Tahoss) | Blench 20069 | $\leq 12$ | Plateau |  |
| Che (Rukuba) | Gerhardt\|1987 | Spec.-12 | Plateau | Cites BCCWL. |
| Che (Rukuba) | Blench et al.\|2006 | $\leq 12$ | Plateau |  |
| Eggon | Blench and Hepburn 2006 | $\leq 12$ | Plateau |  |
| Eggon | Gerhardt 1983:47 | "12", | Plateau |  |
| Eggon | Gerhardt\|1987 | "12" | Plateau | Cites Gospel 1935 + Lukas 1952 fieldnotes |
| Eggon | Shimizu\|1975 | " 12 " | Plateau |  |
| Hyam | de Castelnau 18519:59 | $\leq 12$ | Plateau |  |
| Hyam (Jaba-Kwoi) | Meek\| 1931:123 | 12-144 | Plateau | Also base-10 forms |
| Hyam (Jaba) | Bouquiaux 1962 | "12" | Plateau |  |
| Hyam | Thomas 1920b | $\leq 12$ | Plateau |  |
| Hyam | Blench\|2006f | $\leq 12$ | Plateau |  |
| Ikulu | Seitz\| 1993:37-38 | Spec.-12 | Plateau |  |
| Izere (Fobur) | Blench and Kaze 2006 | $\leq 12$ | Plateau |  |
| Izere (Ganang) | Blench\|2006c | $\leq 12$ | Plateau |  |
| Izere (Zarek-Gana) | Gerhardt 1987 | "12", | Plateau | Citing BCCWL |
| Kaningkom | Gerhardt 1987 | "12" | Plateau |  |
| Koro | Thomas 1920b | $12+$ | Plateau |  |
| Koro | Williamson\| 1973: 453 | $12+$ | Plateau |  |
| Koro (Idũ) | Blench 2009a | $12+$ | Plateau |  |
| Koro (Nyankpa) | Thomas 1920b, Gerhardt 2005, Blench 2009b | $12+$ | Plateau |  |
| Koro (Tinor) | Gerhardt\| 7273 | " 12 " | Plateau |  |
| Koro (Tinor) | Blench ${ }^{\text {2009c }}$ | $\leq 12$ | Plateau |  |
| Lungu | Gerhardt\|1987 | " 12 " | Plateau |  |
| Mada | Blench and Kato 2006 | $\leq 12$ | Plateau |  |
| Mada | Thomas 1920a | " 12 " | Plateau |  |
| Mada (S. Mada) | Mathews\|1917 | 12-144 | Plateau |  |
| Ninkyop | Blench ${ }^{\text {2006e }}$ | $\leq 12$ | Plateau |  |
| Ninzam | Mathews\|1917 | 12-144 | Plateau |  |
| Ninzam | Thomas\|1920a | "12" | Plateau |  |
| Nungu | Mathews\|1917 | 12-144 | Plateau |  |
| Nungu | Thomas 1920a | "12", | Plateau |  |
| Rigwe | Bouquiaux 1962 | "12" | Plateau |  |
| Rigwe | Gerhardt 1987 | " 12 " | Plateau |  |
| Rigwe | Gerhardt 1969: 125 ff | $\leq 12$ | Plateau |  |
| Teria (Cara) | Blench 2006b | $\leq 12$ | Plateau |  |
| Teria/Fachara | Meek\| 1925:142-143 | $12+$ | Plateau |  |
| Tesu | Blench 20061 \| h | $\leq 12$ | Plateau |  |
| Tyap (Gworok) | Adwiraah 1989 | " 12 " | Plateau |  |
| Tyap (Gworok) | Gerhardt\|1987 | $\leq 12$ | Plateau | Not confirmed in Gerhardt 1968 |
| Amo | Luzio 1973 | Cont.-10 | E. Kainji |  |
| Gure | Meek 1931:203 | $\leq 12$ | E. Kainji |  |
| Iguta | Shimizu\|1979 | $\stackrel{12+}{ }$ | E. Kainji |  |
| Janji | Meek 1931: 185-187 | $\leq 12$ | E. Kainji | Continued on next page |


| Language | Source | Type | Family | Comment |
| :---: | :---: | :---: | :---: | :---: |
| Janji | Shimizu\|1979 | $\leq 12$ | E. Kainji |  |
| Janji | Bouquiaux 1962 | " 12 " | E. Kainji |  |
| Jere | Shimizu\| 1982 | $\leq 12$ | E. Kainji |  |
| Jere (Boze, Akwẹre clan) | Nengel ${ }^{\text {2004, } 1999}$ | $\leq 12$ | E. Kainji |  |
| Kahugu | Meek \|1931:212 | $\leq 12$ | E. Kainji |  |
| Lemoro | Shimizu\|1979 | $\leq 12$ | E. Kainji | Not Cokobo |
| Piti | Meek\|1931:139 | $12+$ | E. Kainji | Switched to base-10 |
| Piti | Matsushita 1998 | "12" | E. Kainji |  |
| Rop | Meek\|1925: 142-143 | $12+$ | E. Kainji |  |
| Sanga | Shimizu 1979 | $\leq 12$ | E. Kainji |  |
| Dyarim | Blench 2007 | Spec.-12 | W. Chadic | Etymological Connection |
| Gwandara | Shimizu\| 1975 | "12" | W. Chadic | Citing P. Newman p.c |
| Gwandara (Nimbia) | Matsushita\|1998 | 12-144 | W. Chadic |  |
| Mwaghvul | Jungraithmayr 1963 | $12+$ | W. Chadic |  |
| Ron von Daffo | Seibert\|1998 | $12+$ | W. Chadic | Not confirmed in Jungraithmayr 1970 |
| Mumuye | Matsushita\|1998 | "12" | Adamawa | Not Zing Mumuye pace Shimizu 1983 |
| Mama (Kantana) | Gerhardt\|1987 | " 12 " | Jarawan Bantu |  |
| Mama | Thomas 1927 | $\leq 12$ | Jarawan Bantu |  |
| Mama | Mathews\|1917 | 12-144 | Jarawan Bantu |  |
| Mama | Thomas 1920a | " 12 " | Jarawan Bantu |  |

The base-12 systems occur only in languages in the area of Jos plateau of Nigeria, but which belong to different (sub-)families, namely Plateau (AtlanticCongo), East Kainji (Atlantic-Congo), West Chadic (Afro-Asiatic), Adamawa (Atlantic-Congo) and Jarawan Bantu (Atlantic-Congo). A root resembling \#sok for 12, with plausible sound correspondences (Gerhardt reconstructs *suak), is widespread in Plateau, wherefore it is very likely that base-12 is old in Plateau. The same root occurs in Jarawan Bantu and Ron of Daffo, both of which are isolated instance of this root, or indeed base-12, in their respective families, so borrowing from (proto-southwest) Plateau is highly likely (if not certain, as concluded by Maddieson and Williamson 1975:136 and Gerhardt 1997:140-141 for Jarawan Bantu). In East Kainji and the Beromic subgroup of Plateau, a root \#kuri occurs for 12 , which makes a borrowing in either direction likely. Furthermore, \#piri is 12 in Gure and Kahugu (East Kainji) and \#zowa is 12 in Ake and Koro (Plateau) and yet other roots for 12 appear in the remaining West Chadic cases. Since base-12 is so rare in the languages of the world, the variety of non-ancient roots suggest that a base-12 system may be borrowed even without key morphemes. The root for 12 in the alleged Mumuye variety with base-12 allegation is not known.

There are no obvious clues as to the unusual choice of 12 as a base. A few of the base-12 languages in Meek (1931) have hand gestures that often are used accompanying the spoken expression. A combination of fingers and eyes make up 12 in at least one of these cases, but no traces of words meaning eye, hand or finger can be found in the corresponding spoken expressions. On the other hand, although not a base, 12 bears a special position in several modern European languages too, with a special word like 'dozen' and an elevated frequency (Dehaene and Mehler 1992). The reason(s) for this is not well-understood either.

## Base-15

There appears to be only one case of a language attested as base-15, at least for a number of decades, namely Huli (East New Guinea Highlands/Trans New Guinea, Papua New Guinea) of the southern highland fringes. It is clearly an original body-tally system with a cycle of 29 - midway/centerpoint is thus

15 - which under influence from a Tok Pisin base-system turned into base-15 (Cheetham 1978, Lomas 1988).

## Rare Second Bases

Some rarities in the next higher bases after 5,10 or 20 are as follows:
10-40: Pech (Paya/Chibchan, Honduras) as of Conzemius 1928:264-265) and Hawaiian (Oceanic/Austronesian, USA) until it restructured to 10-100 under foreign pressure (von Chamisso 1837, Dwight 1848, Hughes 1982).

5-20-40: Southwestern Pomo (Pomoan, USA) in one attestation (Closs 1986:3541).

10-60: Attested (Drabbe 1952) in Ekagi (Paniai Lakes/Trans New Guinea, Indonesia) and Ntomba (Bantu/Atlantic-Congo, DRC) until it restructured to 10-100 under foreign pressure (Gilliard 1928, 1924).

5-10-20-60: Famously known from the long extinct Sumerian (Isolate, Iraq), see, e.g. Powell (1972).
(5-)10-20-(60/)80: Attested in Mande Monteil 1905, Dombrowski and Dombrowski 1991, Delafosse 1928, Hartner 1943), Dogon (Calame-Griaule 1968), Gur (Carlson 1994, Welmers 1950: 167-169) and Bangi Me (Blench 2005) languages in a relatively small area in West Africa, wherefore an areal connection is almost certain. In the Mande attestations, the systems vary between 60 and 80 as per a certain root that sometimes means 60 and sometimes 80 .

5-25: Gumatj (Anindilyakwa, Australia) is described, with ample examples, to be 5-25 (upto 625). However, one would not usually use exact numbers for counting this high in this language and there is a certain likelihood that the system was extended this high only at the time of elicitation with one single speaker (Harris 1982, Sobek 2005), especially since an earlier attestation, if anything, shows a commonplace vigesimal count (Tindale 1928:128-129). At least one speaker of Biwat (Yuat River, Papua New Guinea) appears to have made the same 5-25 innovation McElvenny 2006), as two other earlier attestations rather show a commonplace 520 system (Haberland and Seyfarth 1974, Mead 1932) 13 . It is remarkable that there is nd $\sqrt{14}$ incontestable attestation of a $5-25$ system that extends to a whole speech community. The contrast with 5-20 systems, which are ubiquitous, reveals much as to the evolution of normed number expression within a community.

[^35]| 1 | ngū | 6 | šū | 11 | tó |
| :--- | :--- | :--- | :--- | :--- | :--- |
| 2 | žú | 7 | žàadù | 12 | rxá |
| 3 | nié | 8 | ší | 13 | šé |
| 4 | ňūúú | 9 | nīà | 14 | rxò |
| 5 | žứ | 10 | tè | 15 | rxộ? |

Table 4. The monomorphemic numerals up to 15 in Chocho of Santa Catarina Ocotlán. 15-19 are formed as $15+1$ etc and 20 is a base (Veerman-Leichsenring 2000:33-34), cf. also Mock (1977:153-154).

## Last Notes

At least two cases of alleged base-11 exist, both of which appear to be mistaken. Pañgwa (Bantu/Atlantic-Congo, Tanzania) is presented with a base-11 vocabulary (Johnston 1922a: 477), but this cannot be corroborated in other attestations (Stirnimann 1983) so it is presumably an error. A fairly early discussion of Maori (Balbi 1826:256-257) likewise claims undecimality, but this was refuted already in the same century (Conant 1896:122-123). One alleged case of counting in 30:s is in Klingenheben (1927:43) but this too has failed to be corroborated later.

### 3.2 Other Rarities

Other than base, there are a few very interesting rarities which we mention below.

## Streak of unanalyzable forms

Several, but not all, of the base-12 languages have monomorphemic words for all of 1-12 as does, e.g., Chalchihuitán Tzotzil (Mayan, Mexico) (Hopkins 1967:16). However, the record streak appears to be $15 \sqrt{15}$, as evidenced in Chocho of Santa Catarina Ocotlán (Popolocan/Oto-Manguean, Mexico) in Table 4. A claim of monomorphemic 1-20 in Munda (subfamily of Austroasiatic, India) appears, on closer scrutiny, to be artificial or unsubstantiated ${ }^{16}$.

[^36]
## Order of Additive Units

As we have seen, all languages which have numerals above 20 form the higher numbers using addition and multiplication of integers (and occasionally subtraction as well multiplication with fractions). Both addition and subtraction are commutative operations so languages are free to change the order of the operands. Not surprisingly, the order or multiplier and multiplicand is usually the same the order of numeral and noun in the language in question. For additive units the situation is more interesting. For expressions where the sum is less than, say, a 100, we find both smaller-precedes-larger and larger-precedessmaller in the languages of the world. A lot of languages have one order for the teens and the opposite order for higher sums. For sums above 100, the situation is quite different. Almost all languages, and a multitude of the cases must be independent, show larger-precedes-smaller order. At least three ancient languages 17 - Classicial Attic Greek, Classical Arabic, Sanskrit (as well as Vedic) - are attested with both orders possible. The only modern languages with invariable smaller-bigger order between additive units in numeral expressions $\geq 100$ appear to be (certain dialects of) Malagasy (Barito/Austronesian, Madagascar), Chuj (Mayan, Guatemala) and Tzotzil (Mayan, Mexico) ${ }^{18}$, see Daval-Markussen et al. (2008) for references.

## Cardinal Dominance?

In natural languages, it appears that cardinal numerals hold a primary position over other kinds of numerals, e.g., distributive numerals, and exact number marking in general, in the sense that the non-cardinals are morphosyntactically derived from the cardinals and that the cardinals run higher. The dominance appears to be exceptionless for all languages which have numerals above 3 , but we will review two intereresting challenges below.

One description of a Great Andamanese variety explicitly says that there are more ordinals than cardinals (Man 1883a:100), or to be more specific, that there are only 2 cardinals but 6 ordinals. But a closer inspection of the forms reveals that the six "ordinals" are not true ordinals. 3-6 do not mean third-sixth but in the middle, the next one, last and so on. They only acquire the fixed ordinal meaning in the context of a game or the like when the number of patricipants is known (Man 1883b:413).

One description (Mathews 1904) of Wuddyāwūrru (West Victoria/PamaNyungan, Australia) says that there are more grammatical numbers (singular, plural, trial, and plural) than cardinals (one, two). This is not contradicted by other sources on the same or related languages (too many too list). However, there is no linguistic data in this case to ascertain that the trial was a true trial (rather than a paucal) and Mathews has described many other Australian langages as having trials where this is questionable (p.c. Barry Blake 2005). We

[^37]will never know for sure whether this language had a true trial or not, since the language is extinct.

## 4 Conclusion

This paper has surveyed rarities for a number of structural properties of numeral systems. We have given full primacy to data presentation rather than interpretation to make the factual status of the data maximally clear. With this, we hope to have set the stage for future generalizations and interpretations of rareness with a high level of empirical validity.

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## Chapter VIII $\mid$ The Status of the Least Documented Language Families in the World

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# The Status of the Least Documented Language Families in the World 

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## 1 Introduction

There are several legitimate reasons for pursuing language documentation, cf. Krauss (2007) for a fuller discussion. Perhaps the most important reason is for the benefit of speaker community itself - see van der Voort (2007) for some clear examples. Another reason is documentation for linguistic theory - through understanding the limits and distribution of diversity of the world's languages we can formulate and prove statements about the nature of language Brenzinger 2007, Hyman 2003, Evans 2009, Harrison 2007). From the latter perspective, it is especially interesting to document the languages which are the most independent from the ones that are already documented, in other words, those which belong to unrelated families. We have conducted a world survey of the documentation of the language families of the world. In this paper we will list all the known least-documented language families of the world, with the aim to inform of their existence and documentational status. The ultimate hope is that this will increase their chances of being documented.

We have used the following criteria for inclusion in the present list.

1. The language family is known through at least a wordlist (i.e., languages known to exist, but for which there is no data, such as the language of 'isolados ${ }^{11}$, are not listed).
2. The language family, at the present knowledge, is not demonstrably related to any other known family.
3. There are no good grounds for concluding that the language is extinct (= does not have fluent speakers).

[^38]4. All languages of the family are poorly documented, in the sense that there is less documentation than a rudimentary grammar sketch, and there is no ongoing documentation of any of its languages.

The listing is summarized in Table 1. In Section 2 we provide full bibliographic data, references, potential links to other families, endangerment status, and history of knowledge in each case. In Section 3 we clarify why a number of unclear cases are not judged to match the above criteria, and are thus dis-listed from the list in Table 1 .

All the judgments as to family membership, i.e., what counts as demonstrably related and so on, were taken by the author based on inspection of all relevant sources. These judgments are more superficial than those of a potential specialist, but unavoidable since there are no active specialists for the bulk of the languages in question. Since there are frequent disagreements among scholars on such matters, the entry for each individual cas ${ }^{2}$ includes an explanation of the comparative situation and the choices taken.

Every languages and language family considered is cited with its iso-6393 three-letter unique identifier for ease of comparison with standard reference works, e.g., the Ethnologue (Lewis 2009). The information in the present paper differs from standard reference works mainly in that the status of documentation is systematically investigated and used as the criteria for inclusion. For example, while the Ethnologue lists a certain amount of references to descriptive data, it does not aim to systematically list all (or the most extensive etc) references, so the status of documentation is not directly deducible from its listings. Other recent reference works, e.g., Brown and Ogilvie (2009), Brown (2006) do have rigid bibliographic listings but do not aim to be complete in their coverage of the language families of the world. The present listing also differs somewhat from general reference works in the genetic classification and speaker numbers. As explained above, we declare the reason for every innovative choice taken as to genetic classification, and give individual references to the relevant comparative-historical literature. For speaker numbers, we have consulted specialist literature wherever possible, and used the Ethnologue (Lewis 2009) figures in the rest of the cases or when there is reason to believe that it holds the most recent information. A final point of difference is that we mention the first appearance in the linguistic literature as an introduction to each language, in order to give a general sense of how accessible the language is and how long it has gone without documentation.

In total, 25 families are listed, all but two of them one-member families, i.e., isolates. In view of the fact that most of the world's language families are very small Hammarström (2007) - roughly half of them even isolates - it is not surprising that the set of the least documented ones is dominated by isolates.

The lack of geographical diversity among the resulting list is striking. The bulk are situated in the lowland rainforest area between the Sobger (Papua, Indonesia) and the Upper Sepik (Papua New Guinea) rivers of the island of New Guinea. A few more on the list are in other remote areas of Papua, Indonesia,

[^39]| Name | Location | iso | Size | Endangerment | Documentation |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Arara do Rio Branco | Brazil | axg? | Isolate? | HE | Short wordlist |
| Awaké | Venezuela | atx | Isolate | HE | Wordlists, some phrases |
| Sapé | Venezuela | spc | Isolate | HE | Wordlists, some phrases |
| Yurí | Colombia | cby? | Isolate | Unknown | Wordlists |
| Kujarge | Chad | vkj | Isolate | Unknown | 200-item wordlist |
| Nihali | India | nll | Isolate | E | Long wordlists, a little text. Possibly more. |
| Shom Pen | Nicobar | sii | Isolate? | Unknown | Wordlists and phrases, but quality unclear |
| Afra | Papua, Indonesia | ulf | Isolate | E | ca 250 words and 15 sentences |
| Lepki | Papua, Indonesia | lpe | Isolate | Unknown | ca 200 words |
| Asaba | PNG | seo | Isolate? | NE | Short wordlist |
| Baiyamo | PNG | ppe | Isolate? | NE | Short wordlist |
| Busa | PNG | bhf | Isolate | Unknown | Short wordlist |
| Dem | Papua, Indonesia | dem | Isolate | NE | Wordlist and some sentences |
| Guriaso | PNG | grx | Isolate | HE | Short wordlist and short grammar notes |
| Kapauri | Papua, Indonesia | khp | Isolate | NE | ca 250 words and 15 sentences |
| Kimki | Papua, Indonesia | sbt | Isolate | NE | ca 250 words and 15 sentences |
| Mawes | Papua, Indonesia | mgk | Isolate | E | ca 250 words and 15 sentences |
| Mor | Papua, Indonesia | moq | Isolate? | HE | Short wordlist, possibly sentences |
| Murkim | Papua, Indonesia | rmh | Isolate | NE | ca 250 words and 15 sentences |
| Namla-Tofanma |  |  | 2-family |  |  |
| -Namla | Papua, Indonesia | naa |  | HE | ca 250 words and 6 sentences |
| -Tofanma | Papua, Indonesia | tlg |  | NE | ca 250 words and 15 sentences |
| Pyu | PNG | pby | Isolate | HE | Short wordlist |
| Sause | Papua, Indonesia | sao | Isolate | Unknown | ca 200 words |
| Tanahmerah Walio | Papua, Indonesia | tcm | Isolate? <br> 4-family | Unknown | Short wordlist |
| -Pei | PNG | ppq |  | Unknown | Short wordlist |
| -Tuwari | PNG | tww |  | Unknown | Short wordlist |
| -Walio | PNG | wla |  | Unknown | Short wordlist |
| -Yawiyo | PNG | ybx |  | Unknown | Short wordlist |
| Yetfa/Biksi | Papua, Indonesia | yet | Isolate | NE | ca 250 words and 15 sentences |

Table 1. HE $=$ Highly Endangered, $\mathrm{E}=$ Endangered, $\mathrm{NE}=$ Not Presently Endangered, Unknown $=$ No recent data (though in all cases, a good guess is that they are endangered.)
namely, Sause between the Tor and the Lakes Plain, Dem in a pocket of the highlands, Mawes on the northern coastline as well as Mor and Tanahmerah in the northeast of the Bomberai peninsula. In contrast, the listed cases from South America come from much more explored areas and no longer maintain their original territory. Kujarge, the only African case, was sighted on the Chad side in the very remote area near the border of Chad, Sudan and the Central African Republic. In India, Nihali is in an accessible location in central India, while Shom Pen requires travel to the Nicobar islands.

## 2 Listings

### 2.1 South America

## Arara do Rio Branco [axg?]

First reported in Moore (2005) as a sidenote, based on an unpublished wordlist collected by Inês Hargreaves.

There is only a short wordlist for which the majority of entries are not Tupí cognates. Cognates for these words have so far not been uncovered in other families, including Arawak, but the search has been limited since the wordlist is not yet published (Souza 2008).

There is only a short unpublished wordlist, now posted on the internet (Hargreaves 2007). This wordlist was re-checked by Souza (2008).

There are were four rememberers left in 2001. In 2008, there were only two (Souza 2008). While this would normally mean that the language is practically extinct, there is great interest in language revivial with the 200 people strong ethnic group (Souza 2008).

## Awaké [atx]

Awaké was first reported by Koch-Grünberg (1928) who also published a vocabulary.

The collected vocabularies bear no significant relations to neighbouring languages (Loukotka 1968, Migliazza 1980, 1983, 1985). In particular, there is no evidence for an Arutani-Sape family, and listings of such a family (Lewis 2009) is merely the result of basketting "left over" languages.

There are short vocabularies and some phrases (Koch-Grünberg 1928, de Matallana and de Armellada 1943, Migliazza 1978), a short unpublished vocabulary (Coppens 1976) and a minuscule amount of analyzed grammar Migliazza 1980, 1983, 1985). On the other hand, there is a fairly extensive ethnographic study (Coppens 1983).

It is not clear how many competent speakers there are at present. Migliazza, with excellent knowledge of the region, counted only 5 speakers among 15 ethnic Awaké in 1964 (Migliazza 1978:135-136, cf. Migliazza 1972:20). The 2001 Venezuela census counts 29 members of the ethnic group (Amodio 2007), but it is not recorded how many of them speak Awaké (rather than Yanam). The situation on the Brazilian side appears to be similar (Lewis 2009, Fabre 2005).

## Sapé [spc]

First reported by Koch-Grünberg (1928) who also published a vocabulary.
The collected vocabularies bear no significant relations to neighbouring languages (Loukotka 1968, Migliazza 1980, 1983, 1985). In particular, there is no evidence for an Arutani-Sape family, and listings of such a family (Lewis 2009) is merely the result of basketting "left over" languages.

There are short vocabularies and some phrases (Koch-Grünberg 1928, de Matallana and de Armellada 1943, Migliazza 1978), a short unpublished vocabulary (Coppens 1976) and a minuscule amount of analyzed grammar Migliazza 1980, 1983, 1985). On the other hand, there is a fairly extensive ethnographic study (Coppens 1983).

It is not clear how many competent speakers there are at present. Migliazza, with excellent knowledge of the region, counted only 5 speakers among 25 ethnic Sapé in 1977 (Migliazza 1978:135-136), though census data has listed a number around 100 for the ethnic group (Fuchs 1967:78-79). The 2001 Venezuela census counts 6 members of the ethnic group (Amodio 2007) which conflicts with a slightly higher figure in Mosonvi (2003:109-110).

## Yurí [cby?]

First reported by Wallace (1853), but no new data has been forthcoming for more than a century.

The vocabularies bear no significant resemblances to any other language in the region (Ortiz 1965, Loukotka 1968).

All materials (only vocabularies) can be found in Ortiz (1965:232-244). An additional wordlist is mentioned in Vidal y Pinell (1970) which may or may not be Yurí.

The language has not been sighted since the 19th century and therefore suspected extinct (cf. Ortiz 1965). However, there are persistent rumours of speakers or uncontacted peoples, though not precisely from the historical territory, who might be the descendendants of the century-old Yurí (Trupp 1974, Patiño Rosselli 2000, Fabre 2005, Vidal y Pinell 1970, Adelaar 2004:164, Landaburu 2000:30). Consequently, the status of endangerment is unknown - it could be extinct just as well as non-endangered. If the entry for Carabayo [cby] turns out to be Yurí, then the number of speakers, is estimated to be 150 from aerial observations (Lewis 2009).

### 2.2 Africa

## Kujarge [vkj]

Kujarge was first reported by Doornbos and Bender (1983:59-60) with a 100word list, and this remains the known sighting of the languag\& $3^{3}$.

The language was classified as Chadic, in the Mubi group, following 1979 personal communication (to Marvin Lionel Bender) from Paul Newman (Doornbos and Bender 1983:76). However, Paul Newman does not remember the precise details of this classification, in particular not whether it was

[^40]based on a 100 -word or 200 -word list (p.c. Sep 2006). When shown the $200-$ word list Paul Newman sees Chadic elements in it but does not want to commit to Kujarge being a Chadic language (p.c. Sep 2006). Low numerals, pronouns etc look very un-Chadic so it is likely that the words in Kujarge shared with Chadic are loans from a Mubi group language.

The only published data is a 100 -word list in Doornbos and Bender (1983) which were taken from 200-word list taken down by Paul Doornbos. The full 200word list has been typed up by Paul Whitehouse and is available to interested linguists.

The number of speakers was estimated to 1000 in Doornbos and Bender (1983:59-60). Nothing further is known about its endangerment status.

### 2.3 Eurasia

## Nihali [nll]

The Nahali ethnic group was first reported in 1868 (van Driem 2001:243-244) but the first language data is from Konow (1906).

It clear that Nahali has heavy overlay from neighbouring Munda, Dravidian and Indo-Aryan languages, but there is core vocabulary that remains distinct. There have been many attempts, old and new, to relate this chunk of vocabulary to other families, cf., a special issue of Mother Tongue in 1996, but so far there is no convincing case of for a relation (Shafer 1940, Kuiper 1962, 1966, van Driem 2001:242-253).

Published data on Nahali includes long wordlists, a little text and tiny amounts of grammar (Mundlay 1996, Bhattacharya 1957, Konow 1906).

Speaker numbers generally range between 1000 and 2000 (Lewis 2009), most bilinguals, though it is possible that there are also a few monolinguals (van Driem 2001:252). No further information on the endangerment status is known to the present author.

## Shom Pen [sii]

The first linguistic data was collected in 1876 (Man 1886:432).
Shom Pen has been assumed as a Mon-Khmer language in the Nicobar group, but recently Blench (2007a) has argued convincingly that this affiliation is unjustified.

There is an old short wordlist (Man 1886) along with some data on counting (Temple 1907) as well as a more recent larger collection of words and short phrases (Chattopadhyay and Mukhopadhyay 2003), though there are question marks for the quality (Blench 2007a). There is also a very brief ethnographic study (Rizvi 1990).

Lewis (2009) gives a speaker number of 400 (from 2004) while Chattopadhyay and Mukhopadhyay (2003:3) estimate some 300 speakers and
an East Chadic language (Jungraithmavr 2004).
the general conditions indicate that the language is being transmitted to children.

### 2.4 Papua

## Afra [ulf]

First reported (with wordlist) as Oeskoe by Galis (1956) whose information remained the only source for almost half a century.

Voorhoeve (1971) has Afra (under the name Usku) as "unclassified", by which he means that no significant lexical relations are found with its neighbours, or, in other words, a language isolate. In Voorhoeve (1975a), however, it is classified as Trans New Guinea, but no evidence or arguments were ever adduced. Hammarström (2008b) finds any link to Trans New Guinea premature.

Published wordlists are collected in Smits and Voorhoeve (1994). There is also an SIL Indonesia survey report to appear which contains 250 words and 15 sentences (Im and Lebold 2006). There is also a brief anthropological report (Dumatubun and Wanane 1989).

At present, there are about 115 speakers but the language is not immediately in danger. However, the younger generation is just as strong in Indonesian as in Afra (Im and Lebold 2006) which points to a weakeningen position of the vernacular.

## Asaba [seo]

The Asaba language was probably first reported (under the name Suarmin) by Healey (1964:108).

Typological arguments are not sufficient to conclude a Leonard Schultze family with Walio (Laycock and Z'Graggen 1975). The lexical evidence does not show any conclusive genetic relationship either, be it inside or outside Leonard Schultze (Conrad and Dye 1975), with Sepik-Hill (as suggested in Lewis 2009), or with Baiyamo (as Papi) (Conrad and Lewis 1988). However, a higher figure $(29 \%$ ) of Baiyamo-Asabo (as Papi-Duranmin) lexicostatistical relations was quoted by Laycock and Z'Graggen (1975:753), before the later superseding lower figure (10\%) of (Conrad and Lewis 1988:259), and some lexical data collected recently by anthropologists does contain matches between the two. It remains to be worked out whether these are loans or indicative of a genetic relationship.

There are some very brief notes on grammar in Laycock and Z'Graggen (1975). There are extensive anthropological studies on the people (Lohmann 2000, Little 2008).

There are about 180 speakers (Little 2008:2) and the language is still being transmitted to children (p.c. Roger Lohmann 2009).

## Baiyamo [ppe]

Baiyamo was first reported by Laycock (1973) as Papi (a village name).

Typological arguments are not sufficient to conclude a Leonard Schultze family with Walio (Laycock and Z'Graggen 1975). The lexical evidence does not show any conclusive genetic relationship either, be it inside or outside Leonard Schultze (Conrad and Dye 1975), with Sepik-Hill (as suggested in Lewis 2009), or with Asaba (as Duranmin) (Conrad and Lewis 1988). However, a higher figure ( $29 \%$ ) of Baiyamo-Asabo (as Papi-Duranmin) lexicostatistical relations was quoted by Laycock and Z'Graggen (1975:753), before the later superseding lower figure (10\%) of (Conrad and Lewis 1988:259), and some lexical data collected recently by anthropologists does contain matches between the two. It remains to be worked out whether these are loans or indicative of a genetic relationship.

There is a wordlist in Conrad and Dye (1975) and some very brief notes in Laycock and Z'Graggen (1975:752-753).

Lewis (2009) cites a speaker number of 70 . However, the language is still being transmitted to children (p.c. Jack Kennedy 2009).

## Busa [bhf]

Busa was first reported by Loving and Bass (1964).
Busa lexicon bears no significant relations to any other language in the region (Laycock 1975a, Conrad and Dye 1975).

There is a wordlist in Conrad and Dye (1975) and some very brief notes on grammar in Laycock 1975a).

Lewis (2009) cites 240 (2000 census) speakers. In 1980, Busa was spoken by 238 people, and, though Tok Pisin usage was growing, Busa was not endangered (Graham 1981).

## Guriaso [grx]

Guriaso was first reported in 1983 as a new language and named after a central village, Guriaso Baron 1983:27). Previously, Guriaso and a few smaller villages were thought to speak (a dialect of) Kwomtari.

It was subsequently grouped with Kwomtari on very low cognate counts (3\%-13\%) and shared typological features Baron 1983:27-29). In my judgment of the same data, these resemblances can just as well be explained by chance.

The only data (basic lexical and grammatical data) appears to be the 1983 unpublished SIL Survey (Baron 1983) and five numerals in Lean (1986).

The most recent data on speaker numbers is 160 (2003 SIL) as of Lewis (2009), but the language is endangered (p.c. Ian Tupper, SIL-PNG 2007).

## Dem [dem]

The first data from Dem appears in Le Roux (1950) which remains the only source of information about the language.

Dem was grouped with neighboring highland languages based on lexicostastistical counts (Larson 1977), but the the cognation judgments involving Dem
are warped in that a match is judged if at least one segment matches, which obviously gives inconsistent sound correspondences. The lexicostatistic argument for relatedness is the only one offered so far, and apart from probable borrowings, I cannot find any cognates in vocabulary or morphology.

A quite extensive wordlist as well as sentences can be found in (Le Roux 1950). There is also a wordlist in (Stokhof 1983:219-221).

Lewis (2009) cites 1000 speakers ( 1987 SIL) and the language is still strong in the community (p.c. Mark Donohue Aug 2008).

## Kapauri [khp]

Published information (including wordlist) on Kapauri appears first in Voorhoeve (1971).

Voorhoeve (1971) grouped Kapauri with the Kaure languages based on some lexical correspondeces. However, a newer evaluation of the lexical relationships sheds doubt on a genetic relation between the Kaure languages and Kapauri (Rumaropen 2006).

Wordlists of Kapauri (as Narau) are collected in (Smits and Voorhoeve 1994). There 250 words and 15 sentences will appear in an SIL Indonesia survey report (Rumaropen 2006), which also mentions translated bible portions.

The number of native speakers is approximately 200, and the language is in good transmission to the younger generation. At present, Kapauri is not an endangered language (Rumaropen 2006).

## Kimki [sbt]

A tiny 11-word list of what is probably Kimki (Hammarström 2008c) was taken up as early as 1914 (Langeler 1915) but this wordlist has lingered in the unknown. Otherwise, references to Kimki go back no earlier than to 1978 in unpublished SIL Indonesia survey mss (Silzer and Heikkinen 1984, Silzer and Heikkinen-Clouse 1991).

The language is listed as "unclassified" (Silzer and Heikkinen 1984 , Silzer and Heikkinen-Clouse 1991) until between 1996 and 2000 when Grimes (2000) groups it with neighbouring Yetfa-Biksi. However, the lexical evidence is not sufficient for concluding a genetic relation between the two (Hammarström 2008b).

The only substantial data is an unpublished 250 word list and 15 sentences in an SIL survey report to appear (Rumaropen 2004) 5

At this time, Kimki is being transmitted to children, and thus not an endangered language (Rumaropen 2004).

[^41]
## Lepki [lpe]

A tiny 15 -word list of what is probably Lepki (Hammarström 2008c) was taken up as early as 1914 (Langeler 1915) but this wordlist has lingered in the unknown. Otherwise, Lepki is first listed in Silzer and Heikkinen-Clouse (1991) presumably deriving from Doriot (1991).

Wherever it appears, the language is listed as "unclassified" (Lewis 2009, Silzer and Heikkinen-Clouse 1991). The label isolate is more appropriate as the wordlist shows no significant relation(s) with any of the neighbouring languages.

There is an unpublished hurriedly taken up wordlist by Donohue (no date) and a few songs plus a short wordlist contained in an unpublished anthropological report (Andersen 2007). Doriot (1991) also refers to another unpublished wordlist.

Lewis (2009) cites 530 speakers (1991 SIL). Andersen (2007) counts exactly 328 Lepki speakers and records clan membership of each one. Though there is no investigation of language shift, one may suspect that Lepki is under pressure from Ketengban and Indonesian in recently founded villages which have attracted many Lepki (Andersen 2007).

## Mawes [mgk]

The language was first reported as early as (Robidé van der Aa 1879:112) but without accompanying data. Likewise, van der Leeden (1954) noted as separate identity of the language, but no actual language data surfaced.

At some point, the language was classified as a Tor language (Lewis 2009), probably on geographical/cultural grounds (cf. Voorhoeve 1975b:60) but already van der Leeden (1954) had noted its distinctness from Tor. Judging from recent and older lexical data (see below for sources), the there is little basis for classifying Mawes with Tor, nor with neighbouring languages (Wambaliau 2006).

A wordlist was published in Smits and Voorhoeve (1994) and numerals can be found in Galis (1955). 250 words and 15 sentences will appear in an SIL Indonesia survey report (Wambaliau 2006).

Though the speaker number is not low (ca 850), Mawes is under pressure from Indonesian and can be considered an endangered language Wambaliau 2006).

## Mor (of Bomberai) [moq]

As far as we are aware, the language was first reported by Anceaux (1958) and this remains the only source of information on the language.

Evidence for inclusion in Trans New Guinea is weak (Voorhoeve 1975a: 431), both lexically and pronominally.

A wordlist can be found in Smits and Voorhoeve (1998) and judging from the note (note 34 p 18) there and comments in Anceaux (1958), Anceaux collected grammatical data as well. We searched the Anceaux Nachlass for these grammatical data 24 June 2008 at KITLV manuscripts Or 615, especially anvulling 4-23 but we could locate only wordlists for Bomberai Mor. There are
unpublished wordlists and some grammatical data from an SIL Indonesia survey in 19836 , but exactly how much is not clear (p.c. Gilles Gravelle).

Lewis (2009) cites a figure of 25 speakers with Stephen Wurm 2000 given as the source. Since there is no record of Wurm having collected independent data for this region, the figure was presumably taken over from an earlier source, possibly an earlier Ethnologue edition. The present author has not had access to any other information, such as the 1983 survey data. 7

## Murkim [rmh]

Murkim was first reported in Silzer and Heikkinen-Clouse (1991).
Murkim is usually listed as an unclassified language (Silzer and Heikkinen-Clouse 1991, Lewis 2009). There are some lexical matches with neighbouring languages, but they look more like loans than the outcome of genetic inheritance (Hammarström 2008b).

The only data is 250 words and 15 sentences from an SIL survey not yet published (Wambaliau 2004).

At this time, Murkim is being transmitted to children, and thus not an endangered language (Wambaliau 2004).

## Namla-Tofanma [naa,tlg]

Tofanma was first reported (with wordlist) by Galis (1956) whose information remained the only source for almost half a century. Namla was known to Galis (1956), Voorhoeve (1971) as well as Anceaux (nd) as a separate language. Since there was no published or unpublished wordlists or other language data to be found from these authors, the language failed to appear in subsequent listings. Much later, Doriot (1991) "re-discovered" the language and took up a wordlist, but since neither the wordlist or the survey was published the language still failed to appear in listings. Therefore, Namla was re-discovered "again" by chance in an SIL Indonesia survey more than a decade later (Lee 2005).

The only known data indicates that Namla and Tofanma are genetically related, because there are good matches in the basic lexicon, which are arguably not loans (Hammarström 2008b). Voorhoeve (1971) has Tofanma as "unclassified", by which he means that no significant lexical relations are found with its neighbours, or, in other words, a language isolate. In Voorhoeve (1975a), however, it is classified as Trans New Guinea, but no evidence or arguments were ever adduced. Hammarström (2008b) finds any link to Trans New Guinea premature.

Published wordlists for Tofanma are collected in Smits and Voorhoeve (1994) and there is also a 250 -word list and 15 sentences in a survey report to appear (Wambaliau 2005). The only data of Namla is 250 words and 8 sentences from

[^42]an SIL survey not yet published (Lee 2005) and an unpublished wordlist by Doriot (1991).

At present, Tofanma ( 251 speakers) is still being learnt by children, and so is not an endangered language (Wambaliau 2005). Namla speaker numbers are 25 speakers in Galis (1956), 27 in Anceaux notebooks (n.d.), 36 in Lee (2005). All speakers are bilingual in Tofanma, the young generation is more frequently using Indonesian and the children are not learning the Namla language fluently. Therefore, Namla is a highly endangered language.

## Pyu [pby]

Pyu was first reported in the literature by Laycock (1972).
Pyu was grouped in the Kwomtari-Baibai-Pyu phylum, but no real evidence was ever presented (Laycock 1975b). There are no significant lexical links with neighbouring languages (Conrad and Dve 1975).

There are two short wordlists (Conrad and Dye 1975, Laycock 1972) and a sentence or two on grammar in Laycock (1975b:854).

Lewis (2009) cites a speaker number of 100 (2000 census) and more recent information suggests that the language is highly endangered. According to a 1992 report by Arjen Lock, the language is only spoken in the village of Biake 2 with its hamlets (north of the Sepik River and just east of the PNG Indonesian border), together with an unlocated village on the bend of the Sepik within Indonesian territory. According to Lock's informant (who came from Biake 2), "people who are over 30 years and older are bilingual in Abau and [Pyu]. The children are claimed to lack fluency in both Abau and [Pyu]. They prefer to communicate in Tok Pisin." Although Lock's data did not come from observations in the language area, it seems very plausible that the language is highly endangered (p.c. Ian Tupper SIL-PNG Sep 2008).

## Sause [sao]

Probably the first mention of Sause as a separate language is (Voorhoeve 1975b:45) based on Anceaux's collection of wordlists.

At some point, presumably on geographical grounds, the language started to be listed as a Tor language (Lewis 2009), but the lexical data available does not support this.

The only published data is a wordlist in Smits and Voorhoeve (1994). Mark Donohue has collected a minuscule unpublished wordlist from a transient speaker (p.c. Aug 2008).

Lewis (2009) cites 250 speakers. Nothing further is known to the present author about the endangerment status of Sause.

## Tanahmerah (of Bomberai) [tcm]

As far as we can tell, the language was first reported by Galis (1955).
Links with Mairasi are unconvincing lexically and pronominally (Voorhoeve 1975a: 424-431), at least for the given data.

There are some very scanty notes on grammar in (Voorhoeve 1975a:424431) and numerals in Galis (1960). There are very short wordlists Galis (1955), Anceaux (1958) though a slightly longer one appears in Smits and Voorhoeve (1998) and has a note on p 18 that makes it clear that there was additional grammatical data collected by Anceaux. We searched the Anceaux Nachlass for these grammatical data 24 June 2008 at KITLV manuscripts Or 615, especially anvulling 4-23 but we could not locate anything beyond wordlists for Bomberai Tanahmerah. It is likely that Lloyd Peckham, an SIL member working with the nearby Mairasi languages, has newer data on the Tanahmerah (p.c. Mark Donohue Aug 2008). There are unpublished wordlists and some grammatical data from an SIL Indonesia survey in 19838, but exactly how much is not clear (p.c. Gilles Gravelle).

Lewis (2009) cites 500 (SIL 1978) speakers. The present author has not had access to any other information. The present author has not had access to any other information, such as the 1983 survey data ${ }^{9}$

## Walio [ppq,tww,wla, ybx]

The Walio languages were probably first reported by Healey (1964:108).
Typological arguments are not sufficient to conclude a Leonard Schultze family with Baiyamo (as Papi) Laycock and Z'Graggen 1975:752-753) Laycock 1973:32-33). The lexical evidence does not show any conclusive genetic relationship either, be it inside or outside Leonard Schultze (Conrad and Dve 1975, Conrad and Lewis 1988).

There are published wordlists (Conrad and Dye 1975, Conrad and Lewis 1988), numerals in Lean (1986) and some very minimal notes on grammar in Laycock and Z'Graggen (1975:752-753) and Laycock (1973:32-33).

Lewis (2009) cites speaker numbers of 50-360 emanating from the 2000 census. No further information on endangerment status is known to the present author.

## Yetfa/Biksi [yet]

Biksi was first reported in the literature by Laycock (1972), who had met with transients from Papua, Indonesia [then West Irian] while doing fieldwork on the Papuan [then Australian] side in 1970. Yetfa is mentioned for the first time in the 2nd edition of the Index of Irian Jaya languages (Silzer and Heikkinen-Clouse 1991) as an unclassified language - without any references to data - but the information presumably derives from Doriot (1991) who trekked in parts of the Yetfa-speaking area in April-May 1991. Some time between the 14th edition of the Ethnologue (Grimes 2000) and the 15th (Gordon 2005), it was realised that Yetfa and Biksi are so close as to be regarded as one language.

[^43]Biksi (by implication Biksi-Yetfa) was placed in the Sepik group languages by Lavcock and Z'Graggen (1975:740-741) and this has often been repeated since (Lewis 2009). Biksi-Yetfa was not considered by Foley in his re-assessment of the Sepik family for lack of data (Foley 2005:126-127). The lexical matches adduced by Laycock to various Sepik are sporadic, and look more like loans or chance resemblance than the outcome of genetic inheritance (Hammarström 2008b). The lexical relations were also investigated independently by Conrad and Dye (1975:19) who found that Biksi shared no more than $4 \%$ probable cognates with any of the vicinity languages to the east, including Abelam 10 (This lexical comparison includes numerals but no demonstratives or pronouns.) For the alleged connection with Kimki as in, e.g., Lewis (2009) see Kimki below.

Scanty notes on grammar can be found in (Laycock and Z'Graggen 1975:740741) and short wordlists are published in Laycock (1972), Conrad and Dye (1975). An unpublished SIL Indonesia survey contains Yetfa 250-wordlists from five locations and 15 sentences (Kim 2006). There are further unpublished wordlists from several locations collected by Doriot (1991). Missionaries (SIL or UFM) in the area may have further unpublished materials from the past decade, the extent of which is not known to the present author.

At this time, Yetfa is still being transmitted to children and so is not an endangered language (Kim 2006).

## 3 Dis-listed and Unclear Cases

### 3.1 South America

Quite a lot of data, perhaps enough for a basic grammar sketch, was collected by Tastevin on Katawixi [xat] (dos Anjos 2005, Adelaar 2007), and this data makes a good case that Katawixi is related to Harakmbut, Katukina or both (Adelaar 2007).

The Máku language [iso-639-3 code lacking] isolate (Migliazza 1985) is reasonably well-documented in accessible documents (see Maciel 1991, Migliazza 1966 and references therein) and enough data for a 300-page grammar has been collected (p.c. Raoul Zamponi 2006). Also, the language is extinct as the last speaker died sometime between 2000 and 2002 (p.c. Raoul Zamponi 2006).

The isolate Taruma [iso-639-3 code lacking] was believed to be extinct but the last speakers have been located by Eithne Carlin who is actively working with the speakers to document it (p.c. Williem Adelaar 2009).

The Mako [wpc] languag 11 , is known only from a little more than 24 words

[^44](see Loukotka (1949:56-57) and de Humboldt (1825:V7:155-157)) taken up a century or longer ago. This vocabulary shows considerable divergence from Piaroa, and does not seem close enough to be a dialect of it, but with so little data it is hard to say. More recent reports speak of a small ethnic group Mako living among the Piaroa who speak a variety mutually intelligible with Mako (Kaplan 1975, Migliazza 1985, Krute 1988). It could then be either that a) the Mako language as recorded by Vráz and Koch-Grünberg a century ago is extinct and different from what the ethnic Mako among the Piaroa speak in this century, or b) that the the Mako language as recorded by Vráz and Koch-Grünberg is the same as that of the ethnic Mako and that the perceived difference is due to imperfections of elicitation, analysis and data sparsity (cf. Fuchs 1967, Mosonyi and Mosonyi 2000).

### 3.2 Africa

Oropom [iso-639-3 code lacking] of Uganda (Wilson 1970) is probably not a genuine language (Fleming 1987:203), and even if so, it is both extinct and has too little non-Nilotic elements to be considered an isolate (Souag 2004).

The Mpra ( = Mpre) [iso-639-3 code lacking] language in Ghana has lexical items with cognates in Atlantic-Congo as well as lexical items without plausible cognates (Goody 1963). Regardless of the genetic status of the language, the language is practically extinct (Blench 2007b).

A number of language families often subsumed under "Nilo-Saharan" have documentational status bordering that of a grammar sketch. We list the most unclear cases (only the most extensive data collections are mentioned):

Shabo [sbf]: There is a grammar sketch, though admittedly brief (Teferra 1991) and the languages is being documented by Tyler Schnoebelen (Stanford University).

Temeinan [teq,keg]: A phonological description of These (Yip 2004) as well as collections by Stevenson (Blench 2006) give the impression that enough data for a sketch has been collected.

Daju [byg,djc,daj,dau,njl]: There is also a forthcoming grammar and dictionary of Daju-Eref by Pierre Palayer (p.c. Pascal Boyeldieu 2007).

Eastern Jebel [soh,xel,zmo,tbi]: Enough data for a sketch has been collected (Stirtz 2006).

Tama [mgb,sjg,tma]: Two old, admittedly brief, sketches are available (Lukas 1938, 1933) and there are some very brief grammar notes on Miisiirii in Edgar (1989). Gerrit Dimmendaal (Cologne University) has field data on Tama from the 2000s, sufficient for a grammar sketch.

The Nuba mountains outlier language Warnang [wrn] is counted here as a divergent Heiban language (Schadeberg 1981) though this matter is not entirely

[^45]clear (partly due to paucity of data). The language has only been sighted once and one can suspect it is extinct or highly endangered by political turmoil in the past few decades (p.c. Thilo Schadeberg 2007).

Robin Thelwall collected a fair amount of grammatical data on Tegem/Lafofa [laf] (p.c. May 2008).

There are good reasons to believe that substantial amounts of data have been collected for the Mao [myf,gza,hoz,sze] languages (Yimam 2007), and there is an unpublished rudimentary Ganza grammar sketch (Hammarström 2008a).

Stefan Elders collected enough data on Bangeri Me [dba] for (more than) a grammar sketch (cf. Elders 2006) before he died, and this is posted online at http://www.dogonlanguages.org/ (accessed 29 Sept 2008).

Jalaa [cet] is now presumably extinct (Kleinewillinghöfer 2001).
Smith (1897) mentions Dūmē [iso-639-3 code lacking], along with a tiny vocabulary, which is not obviously related to any of the neighbouring languages. Later surveys of the region have failed to find any trace of Dūmē and have therefore regarded the original information as suspect Jensen 1952:5758, Haberland and Jensen 1959). In any case, if it is genuine, Dūmē must be presumed extinct.

### 3.3 Eurasia

Jiamao [jio] has recently been suggested as a language isolate with heavy Hlai overlay (Norquest 2007), but the suggested residual vocabulary is not large enough in the opinion of the present author.

### 3.4 Papua

There is too little data on Kehu to say whether it is to be considered an isolate or related to some other language(s) as the only known wordlist contains, for example, neither numerals nor pronouns (Whitehouse nd).

The present author has had no access to data on Kembra [xkw] (Doriot 1991) and cannot vouch for its status either as isolate or related to some other language(s).

The present author has had no access to data on Yerakai [yra] Laycock 1973 ) and cannot vouch for its status either as isolate or related to some other language(s).

The present author has had not access to substantial data on the MongolLangam [lnm,mgt,yla] languages (Laycock 1973) and cannot vouch for their status either as a small family or related to some other language(s).

The present author has had no access to substantial data on Dibiyaso [dby], Doso [dol] and Turumsa [tqm] (Tupper 2007) and cannot vouch for their status either as a stand-alone family ${ }^{12}$

[^46]Foau [flh] and Diebroud [tbp] are related to the Lakes Plain languages (Clouse 1997) though not in an obvious way (p.c. Mark Donohue 2008).

The Eastern Pauwasi languages Zorop [wfg] and Emem [enr] are now understood to be genetically related to Karkar-Yuri [yuj], an insight probably due originally to Tim Usher (Whitehouse 2006). Therefore, since there are extensive materials on Karkar-Yuri (Price 1987, Price et al. 1994, Rigden no date) the family counts as reasonably well-documented. (There are some good lexical cognates that suggest that the Western Pauwasi languages Tebi [dmu] and Towei [ttn] form a bona fide family with the Eastern Pauwasi languages and Karkar-Yuri, but it is not impossible that the links are loans and that we are dealing with two small families with a lot of interaction (Hammarström 2008b)).

Mark Donohue has collected enough data for sketches of Abinomn [bsa], Bayono-Awbono [awh,byl], Powle-Ma [msl], Tanglapui [swt] (of the KolanaTanglapui family/subfamily), Masep [mvs], Elseng [mrf], Moraori [mok], Yoke [yki] and Damal [uhn] (p.c. Mark Donohue 2008).

Grammar sketches or other materials enough for a sketch have been collected by SIL members or others for the following language families (only the most extensive data collections are mentioned):

Pele-Ata [ata]: There is a dictionary (Hashimoto 2008) as well as an unpublished 'Ata grammar essentials' in the SIL (Ukarumpa) archives. Tatsuya Yanagida (Australian National University) is writing a PhD thesis on the language (Yanagida 2004).

Kol [kol]: There are unpublished manuscripts by Stellan and Eivor Lindrud (Akerson and Moeckel 1992) and a New Testament translation soon due for press (p.c. Stellan Lindrud 2006).

Pahoturi [kit,idi]: There is also an unpublished rudimentary (20-page) grammar sketch of Idi in the SIL archives (No Author Stated nd) and the raw data collected by Wurm in 1966 and 1970 may include enough for a grammar sketch (Wurm 1971).

Waia [knv]: There is an unpublished grammar (2004, 394 pages) in the SIL archives (p.c. Tim Schlatter 2006). Translations of the New Testament have appeared in both the Aramia river (No Author Stated 2006a) and Fly river dialects (No Author Stated 2006b).

Awin-Pa [awi,ppt]: In addition to bible text data, there is now an (otherwise unpublished) extensive grammar sketch of Kamula posted online (Routamaa 1994).

Somahai [mmb,mqf]: Martha Reimer has collected a large amount of data om Momuna, of which a little has been published (Reimer 1986).

Konda-Yahadian [knd,ner]: Enough data for a rudimentary grammar sketch has been collected by SIL Indonesia members (Berry and Berry 1987).

Porome [prm]: Martin Steer (Australian National University) is writing a PhD thesis on the language.

Yuat [bwm,buv,cga,kql,myd,mvk]: There are unpublished notes in the Mead/Fortune fieldnotes (McDowell 1991:23) and James McElvenny (Sydney University) did two months of fieldwork on Mudukumo and has written up a draft grammar sketch (p.c. James McElvenny 2008).

Tirio [aob,bmz,mcc,aup,wei]: An unpublished SIL survey from the 2000s has collected sociolinguistic, lexical and grammatical data (p.c. Ian Tupper 2007). The raw data collected by Wurm in 1966 and 1970 may include enough for a grammar sketch (Wurm 1971). (Ray 1923:360) mentions a Tirio grammar manuscript by the Reverend Riley of unknown size and location ${ }^{13}$.

Yalë [nce]: There is an unpublished grammar sketch by SIL missionaries (Campbell and Campbell 1987).

Kayagar [aqm,kyt,tcg]: Unpublished short grammar sketches are referenced in Silzer and Heikkinen-Clouse (1991).

Arafundi [afd,afk,afp]: There are notes on Arafundi in the writings of William Foley (Foley 2006), who presumably has extensive fieldnotes. There is also an SIL survey report from 2005 (p.c. Ian Tupper 2005).

Suki [sui]: There is a New Testament translation (Bidri et al. 1981).
Gogodala [aac,ggw,wrv]: There is a New Testament translation Partridge 1981).

Amto-Musan [amt,mmp]: Linda Krieg et al. of the New Tribes Mission is in the process of translating the bible into Siawi ( $=$ Musan) and there is so far unpublished phonemic and grammar sketch write-ups (p.c. Linda Krieg 2007).

Piawi [tmd,pnn]: There is an unpublished grammar sketch of Pinai (Melliger 2000) as well as published grammar aspects of Haruai (e.g., Comrie 1991).

## 4 Conclusion

We have conducted a world survey of the documentation of the language families of the world. In this paper we have listed all the known least documented language families of the world which are not yet known to be extinct. Borderline cases, unclear cases and cases for which there exists little-known data, frequently unpublished, are also listed. This we hope will be useful in setting priorities for documentational fieldwork, in particular for those documentational efforts which have understanding of linguistic diversity as an underlying goal.
${ }^{13}$ I could not find any further clues about the Tirio grammar manuscript in the Nachlass of Sidney H. Ray as SOAS Library (Aug 2008).

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[^0]:    ${ }^{1} 785066$ tokens/running words versus 12999 unique words/types (King James 1977).
    2 Because of this, most such implementations have so far not been released to the public domain and have sometimes been kept in formats with poor portability, but there is in principle no reason why it should continue to be so, cf. Forsberg (2007).

[^1]:    ${ }^{1}$ Website http://www.cis.hut.fi/morphochallenge2009/ accessed 10 September 2009.

[^2]:    2 Though, this is still far superior to the cascade of thresholds advised by the other early pioneer, Andreev (1965).

[^3]:    ${ }^{3}$ As most approaches define their task as capturing the set of legal morphological forms, their goal should be to compress $W$, but see Goldwater (2007:53-59) for arguments for compressing $C$.

[^4]:    ${ }^{4}$ There would also have been practical problems in doing justice as many descriptions of existing systems hide information on parameter tweaking. Online systems we have found do not allow uploading the training/test set we use, which is crucial in order to assess language-dependentness.

[^5]:    5 http://odur.let.rug.nl/~vannoord/TextCat/competitors.html accessed the 25th of May 2005.

    6 http://www.xrce.xerox.com/competencies/content-analysis/tools/guesser accessed 20 Jan 2007.

[^6]:    7 According to http://www.google.com/help/basics.html accessed 20 March 2006.

[^7]:    ${ }^{8}$ The next edition is the 2009 one http://www.cis.hut.fi/morphochallenge2009/accessed 1 May 2009.

[^8]:    ${ }^{9}$ Cf. the journal/newsletter Language Archives News http://www.mpi.nl/LAN/

[^9]:    10 Three examples from three continents are Alsea (isolate; North America) has a text collection from 1920 (Frachtenberg 1920), Uduk (Koman; Africa) has a New Testament translation from 1963 (Sudan Interior Mission 1963) and Tabo (isolate; Oceania) has a New Testament translation from 2006 (No Author Stated 2006b a).

[^10]:    11 There is actually at least one known suffix in Mpiemo, a plural imperative plural imperative suffix, but it does not occur in the (narrative) texts.

[^11]:    ${ }^{1}$ For other choices of terminology see Streiter et al. (2006:2-3).
    ${ }^{2}$ According to a popular article Weaving a Web of linguistic diversity, http://www.guardian.co.uk/GWeekly/Story/0,3939,427939,00.html 2001-01-25, retrieved 2006-09-12, this number is about 1000 . Though it is not clear how this figure was computed.

[^12]:    ${ }^{3}$ In addition to extinct languages, there are important exceptions, such as Hausa, Swahili and Indonesian, where the L2-economy appears to make up a major fraction.
    ${ }^{4}$ Of course, the language-dialect divisions are debatable. We will assume the Ethnologue divisions for the present paper (Lewis 2009).

[^13]:    ${ }^{5}$ If such had been included on the basis of their title or the like, a much wider range of languages would have been encountered (see Wedekind and Wedekind 2009, Wedekind 2008, Wedekind et al. 1983, Adegbola 2009, Ridings and Mavhu 2002, Maphosa 2002 for some examples known to the present author).

[^14]:    ${ }^{5}$ Penalty weights set to 1 for deletion, insertion and substitution alike.

[^15]:    ${ }^{6}$ For example, the very wide coverage database worldcat (http://www.worldcat.org/) does not index individual articles and has insufficient language annotation; sometimes no annotation or useless categories such as 'other' or 'Papuan'. The SIL Bibliography (http://www.ethnologue.com/bibliography.asp) is well-annotated but contains only work produced by the SIL. (SIL has, however, worked on very many languages, but not all publications of the de-centralized SIL organization are listed in the so-called SIL Bibliography.)
    7 Those entries which are natively written with a different alphabet always also have a transliteration or translation (or both) into ascii characters.

[^16]:    ${ }^{8}$ This overlap at first appears surprisingly low. Part of the discrepancy is due to the fact that many references in the WALS database are in fact to secondary sources, which are not intended to be covered at all in the on-going project of listing. Another reason for the discrepancy is due to a de-prioritization of better-known languages as well as dictionaries (as opposed to grammars) in the on-going project. Eventually, all unique references will of course be merged.

[^17]:    $\overline{9}$ In a few cases they were forced unique, e.g., when two families X , Y were listed as having subgroups called Eastern (or the like), the corresponding group names were forced to Eastern-X and Eastern-Y respectively.

[^18]:    ${ }^{1}$ Of course, it is easy to think of examples where $A$ and $B$ are closely related and speakers of $A$ tend to understand $B$ but not the other way round. For the sake of an example. take Jamaican Creole and Oxford English. But in most (all?) such cases this is because the $A$ speakers have been exposed to $B$ a lot more, and not purely because of their knowledge of $A$. I see no reason to differentiate this situation from that where $A$ are $B$ aren't closely related, and speakers of $A$ know $B$ as well, but not vice versa.
    2 See however Hockett 1958:321-330) for an embryo to the approach taken in this paper (whose views recollected by e.g., Heine and Köhler 1981:1-3). Note also that the matter is not discussed in the most recent encyclopaedia entry on dialect chains (Heap 2006).

[^19]:    ${ }^{3}$ Comrie affirms in a personal email (9 Sept 2005) that the quoted paragraph concerns only this particular definition, and the statements therein that may look as if they quantify also over other intuitive definitions based on the MI, should not be so interpreted.

[^20]:    ${ }^{4}$ For readers not familiar with graphs, a graph can be thought of as a set of points ("vertices") in a two-dimensional space and an arbitrary set of lines ("edges") between pairs of points. More information can be found in any introductory book on discrete mathematics.

[^21]:    ${ }^{5}$ In fact, it is $S(n, 1)+S(n, 2)+\ldots+S(n, n)$, where $S$ denotes the Stirling numbers of the second kind. See e.g. Stanley 1997:33) for more information.

[^22]:    ${ }^{1}$ The following relevant unpublished data was inaccessible to the author: Data on TransFly languages collected by Wurm in 1966 and 1970, data on Trans-Fly languages collected by Capell for his survey of the South Pacific 1950s and on, data on Trans-Fly languages collected by Nicholas Evans in the 2000s, A. P. Lyons's journals held at National Cultural Council at Port Moresby, the archives of Francis Edgar Williams, held at the National Archives of Papua New Guinea. On the other hand, the archives of Sidney H. Ray, who published a lot of missionary and patrol mss vocabularies of Papuan languages, at SOAS Library in London (consulted August 2008) did not contain any further data on Trans-Fly languages than was published.
    2 An occasional variety attests an incipient base-5 system, i.e., $1,2,2+1,2+2,5,5+1,5+2,5+2+1,5+2+2$ (Nevermann 1942).
    ${ }^{3}$ We use \# in contrast to * to mark hypothetical forms that stem from phonologically inadequate transcriptions and lack the rigour normally associated with the ${ }^{*}$-symbol.

[^23]:    ${ }^{4}$ Save for possible Marind incursions, which, in any case, could not be the source for elaborate counting, since elaborate counting is not attested in Marind (Wirz 1922).

[^24]:    5 Leont'ev 1974:68-69)'s claim that also Kati is base-6 is erroneous, as Kati, like other Ok languages, has a body-tally system (Galis 1955).

[^25]:    6 This claim, on a worldwide scale, has good explanatory power (though not exceptionless) but is beyond the scope of this commentary (Hammarström 2008).
    7 Lean (1986: 48) discloses that it is "uncertain whether the system shown .. is the standard one used for everyday purposes or a special one used for counting yams which are grouped in sextets for this purpose".
    8 The prediction is not entirely vacuous; e.g., Meek (1931) attests hand gesture counting which uses hands and eyes - a closed fist covering one eye making 6.

[^26]:    9 SIL Indonesia surveyed Kimaam district in August 2001 but the vocabularies from this survey had not been typed up as of writing this (p.c. Randy Lebold Feb 2008).
    ${ }^{10}$ In fact, unknown to Kluge, the word durua also means 'leg' (Drabbe 1949:15).

[^27]:    11 Nevermind that an etymology for '6' as 'upper arm' or 'leg' would be unparallelled anywhere else in the world, since nearly the same is true for base- 6 systems.
    12 I searched hard for any evidence of a similar yam counting connection for the base- 6 systems at Kolopom in missionary manuscripts at KITLV archives, but found nothing, either pro or contra.

[^28]:    173). The naturalist d'Orbigny (1839:191) travelled through the area in the 19th century and is the only source for numerals in the language. Since this is the only source, we can neither confirm or deny his report of lack of numerals:

    Il n'y a, dans cette langue, aucun système de numération, qu'y remplacent à peine quelques termes de comparaison, eux-mêmes, très-bornés.
    . 12. In all descriptive publications, Khoedam (Khoe/Khoe-Kwadi, Namibia) |úí and |áḿ are glossed as 'one' and 'two' respectively, but closer inspection reveals that these are really meanings accustomed to linguistic elicitation, and 'singleness' and 'dualness' are more appropriate glossings. There is a subtle difference between 'dualness' and 'twoness' in that dualness implies an association between the items in question. So |ám children would mean twins rather than two children. If this difference is deemed significant, then there was no word for 'two' in traditional Khoedam (Brenzinger 2009).
    ${ }^{2}$ We regret that we have not been able to access two relevant-looking publications on the Mura language Hanke 1950, 1952).

[^29]:    ${ }^{3}$ Carole Swain has also submitted the same information for the Ninam entry for the Numeral Systems of the World's Languages website at http://lingweb.eva.mpg.de/numeral/Ninam.htm, accessed 1 July 2009.
    4 Ross and Paul (1978:60) give expressions for 1-8 in Waskia (Adelbert Range/Trans New Guinea, Papua New Guinea) with the structure $1,2,2+1,2+2,2+2+1,(2+1)+(2+1),(2+1)+(2+1)+1,(2+1)+(2+1)+2, \quad$ that is, $6-8$ are formed with additions based on $(2+1)+(2+1)$ for 6 . This comes close, but does not count as base- 3 according to the definition used in this paper.

[^30]:    ${ }^{6}$ Shown at http://lingweb.eva.mpg.de/numeral/Bukiyip.htm accessed 1 July 2009.

[^31]:    $\overline{7}$ I wish to thank Peter Bakker for highlighting this reference to me.
    8 Payaguá, though poorly attested, is often counted as related to (at least) the Guaicuruan languages (Viegas Barros 2004) but we do not think the evidence is conclusive.

[^32]:    9 This language has not yet been identified with any modern variety (p.c. Jouni Filip Maho 2004, p.c. Roger Blench 2009).

[^33]:    10 With some speculative etymologizing, Chepang (Mahakiranti/Sino-Tibetan, Nepal) may have had 12 atoms and duodecimal counting up to 50 , for a counting system associated with hunting (Caughlev 1988, 1972, Hale 1973). One synopsis of Brúnkajk (Talamancan/Chibchan, Costa Rica) says that "también se cuenta por medio de docenas" Arrovo Soto 1972:32), but it is not clear on what this statement is based. It is not corroborated by a ten or so other descriptions of Brúnkajk, and it was not normed anyway, so it does not count as a base- 12 system. In a modern description of Kinikinau (Bolivia-Parana/Arawakan, Brazil) higher numbers may be expressed using (dúzias) dozens (de Carvalho Couto 2005:51), but this does not appear to be normed for exact enumeration of quantities that are not exact multiplies of twelve.
    ${ }^{11}$ However, vocabularies including monomorphemic 1-12 are listed for Hyam (there called 'Java') a few years earlier (de Castelnau 1851d:59).

[^34]:    ${ }^{12}$ We wish to thank Roger Blench for help with sorting out various Plateau language identifications and classification questions.

[^35]:    ${ }^{13}$ I wish to thank James McElvenny for access to archival material on Biwat.
    14 The extinct Saraveka has 'five hands' attested for 25 but no numerals 20-24 nor above 25 are recorded (de Créqui-Montfort and Rivet 1913). The 5-25-50 counting system in Kikongo (Bantu/Atlantic-Congo, DRC) referred to in Schmidl (1915:181) was for counting pearls only (Laman 1968, 1912, 1936).

[^36]:    ${ }^{15}$ I wish to thank Thomas Hanke for bringing this case to my attention. 16 Sharma 2003:63) claims that

    We may say Munda speakers are the earliest known people who practised this system of counting which had monomorphemic units of counting upto twenty.
    but gives no source and no forms. Monomorphemic 1-20 forms cannot be found in the monograph on Munda numerals by Zide (1978) nor in any published description of Kharia or any other Munda language we have been able to consult. Nevertheless, a recent unpublished description of Kharia (Peterson 2006:138-139), a set of monomorphemic 11-19 are recorded as alternative forms alongside a set of composite forms. Peterson notes, however, that the monomorphemic forms were given to him by youths who all confirmed that they had be taught them in school (and themselves used Sadani loans for the numbers in question). Further inquiries by Peterson with experienced local teachers also point towards an "artificial" origin of the 11-19 forms (p.c. John Peterson 2008).

[^37]:    17 A modern example may be the recently innovated Palikúr (North Arawak/Arawak, BrazilGuyana) numeral system, but it is not fully clear what the norms are (Green 1994, Launey 2003).

    18 I wish to thank Aymeric Daval Rasmussen for bringing the Mayan cases to my attention.

[^38]:    ${ }^{1}$ See Hammarström (2007) for some listings of these.

[^39]:    ${ }^{2}$ We do this also for the unclear and dis-listed cases wherever relevant.

[^40]:    ${ }^{3}$ Names similar to Kujarge occur in Lebeuf (1959:116) and MacMichael (1918:45) as well but without any language data and seemingly designating a different group or caste than Doornbos' Kujarge.
    ${ }^{4}$ Also, the remark "I am assuming that [...] Doornbos' Kujarke is Newman's Birgit, 1977:6." (Doornbos and Bender 1983:76) suggests that the classification is (partly) the result of a confused language identity. Comparing the actual language data shows that Newman's Birgit is not the same language as Doornbos' Kujarge and Newman's Birgit is definetely

[^41]:    5 Doriot (1991) refers to an unpublished wordlist of Kimki from Mot, but Mot is listed in survey maps as Murkim speaking (Wambaliau 2004).

[^42]:    ${ }^{6}$ I wish to thank Mark Donohue for bringing my attention to this survey.
    7 However, the unpublished survey report Roland Walker and Michael Werner 1978 Bomberai Survey Report MS, SIL Indonesia contains no original information as the survey team did not travel to the Mor area (p.c. Roland Walker Aug 2008).

[^43]:    ${ }^{8}$ I wish to thank Mark Donohue for bringing my attention to this survey.
    ${ }^{9}$ However, the unpublished survey report Roland Walker and Michael Werner 1978 Bomberai Survey Report MS, SIL Indonesia contains no original information as the survey team did not travel to the Tanahmerah area (p.c. Roland Walker Aug 2008).

[^44]:    10 The exaxt languages in question are Yerakai ( $0 \%$ ), Chenapian ( $0 \%$ ), Bahinemo ( $1 \%$ ), Washkuk (1\%), Yessan-Mayo (4\%), Abelam (1\%), Namie (0\%), Abau (0\%), May River Iwam (1\%), Musan (0\%), Amto (1\%), Rocky Peak (0\%), Ama (0\%), Nimo (1\%), Bo (0\%), Iteri $(0 \%)$, Owiniga ( $2 \%$ ), Woswari ( $0 \%$ ), Walio ( $0 \%$ ), Paupe ( $0 \%$ ), South Mianmin ( $0 \%$ ), Nagatman (0\%), Busan (1\%), Pyu (1\%).
    11 As Nimuendaiú 1950:171-172) reminds us, there are no less than six distinct languages/ethnic groups so far referred to with the resemblant form \#maku. The Mako language discussed here is the one defined by the vocabularies furnished by Vráz, Koch-

[^45]:    Grünberg (Loukotka 1949:56-57) and de Humboldt (1825: V7:155-157).

[^46]:    $\overline{12}$ Doso and Turumsa has $61 \%$ lexicostatistical similarity and Turumsa and Dibiyaso has $19 \%$ which, pace known caveats, indicates that the three form a small (sub-)family (p.c. Ian Tupper Sep 2008).

